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Interim Report

Heat and Momentum Transfer to Internal  
Turbulent Flow of Helium-Argon Mixtures  
in Circular Tubes

by Paul E. Pickett

CONVECTIVE HEAT TRANSFER FOR SHIP PROPULSION

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Interim Report

HEAT AND MOMENTUM TRANSFER TO  
INTERNAL, TURBULENT FLOW OF HELIUM-ARGON  
MIXTURES IN CIRCULAR TUBES

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## ABSTRACT

The results of an experimental investigation of friction and heat transfer parameters for turbulent flow of helium-argon mixtures in smooth, electrically heated, circular tubes are presented. Experimental results are compared to existing experimental correlations and to analytical results. Results of air and helium from the same experimental apparatus are included for comparison.

In this experiment helium-argon mixtures with molecular weights between 15.3 and 29.7 are used, <sup>He-A</sup> ~~this range resulted~~ in Prandtl numbers between 0.42 and 0.49. Inlet Reynolds numbers range from 31200 to 102000, maximum wall temperatures from 392 to 828°K, maximum wall-to-bulk temperature ratios to 1.82, maximum wall heat flux values to 511 KW/m<sup>2</sup>, and pressures from 469 to 967KPa, (4.7 to 9.7 atmospheres).

Existing experimental correlations, developed using gases with Prandtl numbers of approximately 0.7, are compared to the measured friction and heat transfer results. Adiabatic friction factors and friction factors with heat addition are predicted within ±4 and ±10 percent, respectively. Nusselt numbers for fully developed, constant property conditions are predicted within ±5.0 percent. An empirical equation that correlates the helium-argon data within ±15 percent, and includes entrance and variable

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property effects is presented.

Using a recently developed technique that compares numerically calculated and measured constant property Nusselt numbers, turbulent Prandtl numbers in the wall region for helium-argon mixtures are determined. The validity of using these turbulent Prandtl numbers in a variable property numerical analysis is examined. The variation of turbulent Prandtl number with respect to Reynolds number and molecular Prandtl number is also inspected.

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## NOMENCLATURE

$a$ ,	exponent used to account for temperature variation of viscosity;
$a_i$ ,	array of system parameters;
$A'$ ,	calibration constant for the laminar flow element;
$A_{cs}$ ,	cross sectional area of tube;
$b$ ,	exponent used to account for temperature variation of conductivity;
$B'$ ,	calibration constant for the laminar flow element;
$c$ ,	velocity of sound;
$c_p$ ,	specific heat at constant pressure;
$D$ ,	inside diameter;
$E$ ,	voltage drop;
$g$ ,	gravitational constant;
$g_c$ ,	dimensional conversion factor;
$G$ ,	mass flow rate per unit area;
$h$ ,	heat transfer coefficient;
$i$ ,	enthalpy per unit mass;
$k$ ,	force constant in Lennard-Jones (6-12) potential;
$K$ ,	thermal conductivity;
$L$ ,	length between pressure taps in laminar flow element;
$\ell$ ,	mixing length;
$\dot{m}$ ,	mass flow rate;
$\hat{M}$ ,	molal mass;

$\Delta P$ , pressure drop;  
 $P$ , power;  
 $q$ , heat transfer rate;  
 $q'$ , heat transfer rate per unit length;  
 $q''$ , heat flux;  
 $Q$ , volume flow rate;  
 $r$ , radius;  
 $R$ , gas constant for a particular gas;  
 $R'$ , resistance per unit length;  
 $R$ , universal gas constant;  
 $T$ , temperature;  
 $u$ , velocity in axial direction;  
 $x$ , axial distance from start of heating;  
 $y$ , radial distance from wall;  
 $Y_1$ , array of measured values;  
 $Z$ , a calculated quantity.

Greek symbols

$\alpha$ , thermal diffusivity,  $K/c_p \rho$ ;  
 $\epsilon$ , force constant in Lennard-Jones potential;  
 $\epsilon_H$ , eddy diffusivity for heat;  
 $\epsilon_M$ , eddy diffusivity for momentum;  
 $\gamma$ , ratio of specific heats,  $c_p/c_v$ ;  
 $\kappa$ , von Karman constant  
 0.4;  
 $\mu$ , absolute viscosity;  
 $\nu$ , kinematic viscosity;

$\rho$ , density;  
 $\sigma$ , variance or standard deviation;  
 $\tau$ , shear stress.

#### Non-dimensional parameters

$f$ , friction factor,  $2g_c\rho\tau_w/G^2$ ;  
 $Gr$ , Grashof number based on wall heat flux,  
 $gD^4q_w''/(\nu^2\mu c_p T)_i$ ;  
 $M$  Mach number,  $j/c$   
 $Nu$ , Nusselt number,  $hD/K$ ;  
 $Pr$ , Prandtl number,  $c_p\mu/K$ ;  
 $q^+$ , heat flux parameter,  $q_w''/(Gc_{p,i}T_i)$ ;  
 $Re$ , Reynolds number,  $GD/\mu$ ;  
 $y^+$ , wall distance parameter,  $y(g_c\tau_w\rho)^{1/2}/\nu$ ;  
 $y_\ell^+$  empirical constant in van Driest mixing length  
 model, 26.

#### Subscripts

$b$ , evaluated at bulk temperature;  
 $cond$ , heat conduction;  
 $cp$ , constant property condition;  
 $DB$ , Dittus-Boelter;  
 $gen$ , heat generation;  
 $i$ , inlet; an index;  
 $Max$ , maximum;  
 $ref$ , reference;  
 $t$ , turbulent;  
 $VD$ , van Driest;  
 $w$ , wall;  
 $Xe$ , xenon;  
 $\infty$ , environment conditions.

## INTRODUCTION

The closed Brayton cycle using inert gases as working fluids has been considered for use in many current applications. The Navy has investigated its use for undersea and surface ship propulsion. NASA has examined it for future space missions requiring relatively large amounts of electric power (100 - 500 Kw) [1,2,3,4]. Binary mixtures of helium and heavier inert gases, such as argon or xenon, have been considered as possible working fluids in these closed Brayton systems. The increase in density, due to the heavier inert gas, reduces the size of the compressor and turbine. The thermal conductivity of the binary mixture is lower than that of helium, thus causing an increase in the size of the heat exchangers. At an intermediate molecular weight an optimum can be attained.

Fig. 1 illustrates the relative heat transfer of helium-argon and helium-xenon mixtures compared to the pure gases and air. The relative heat transfer coefficients were calculated using the Dittus-Boelter type relation

$$h = 0.021 \text{ Re}^{0.8} \text{ Pr}^{0.4} (K/D) \quad (1)$$

and were normalized with respect to the lowest value. The geometry and mass flux were kept constant. This resulted in a relative heat transfer coefficient of the form

$$h/h_{\text{Xe}} = (c_p \mu_{\text{Xe}} / c_p \mu)^{0.4} (K/K_{\text{Xe}})^{0.6}. \quad (2)$$

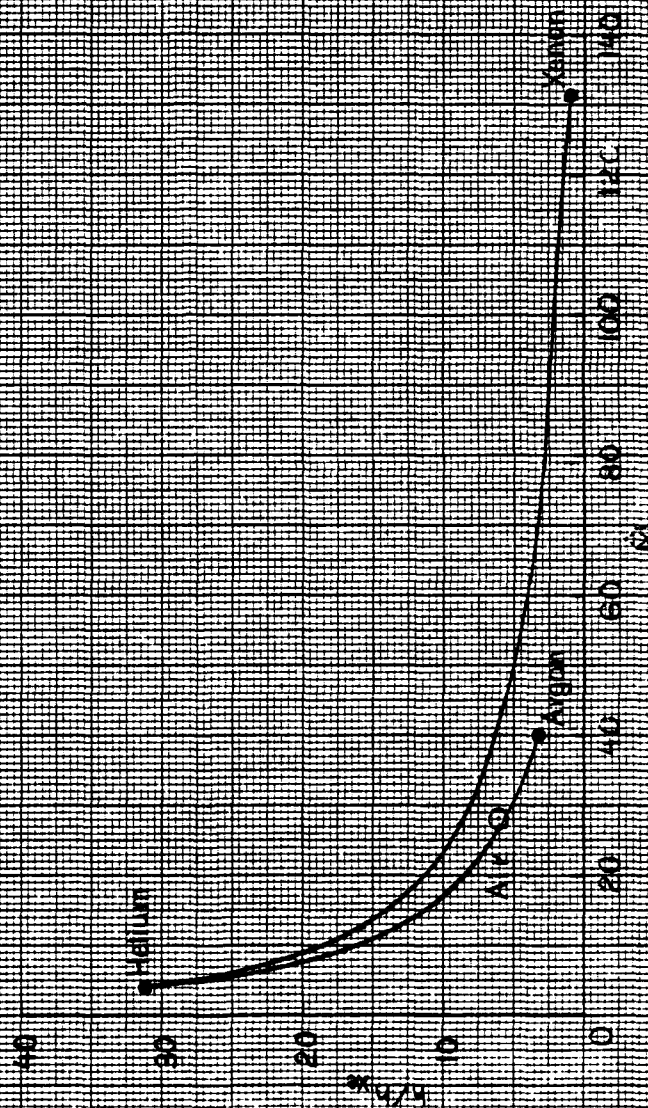


Fig. 1. Relative heat transfer coefficients of mixtures of helium, argon and helium-xenon compared to air and the pure gases, helium, argon, and xenon. Properties were taken at 860K and 101KPa.

All properties were taken at 860K and 101KPa. Vanco [4] performed a similar analysis, but kept the geometry and molal flow rate constant, which gave quite different curves. Examination of Fig. 1 shows why helium-xenon is the prime candidate for a working fluid in the closed Brayton cycle. Helium-argon has been investigated initially due to expense and convenience of experimental apparatus.

The purpose of this research was to determine, for turbulent flow in tubes, the momentum and heat transfer characteristics of helium-argon mixtures. No basic momentum and heat transfer experimental work for fluids with Prandtl numbers between 0.1 and 0.67 presently exists in the literature. Until recently, it was thought that no fluids existed in this Prandtl number range [5,6]. The mixtures of helium and heavier inert gases fill this void, having Prandtl numbers between 0.25 and 0.67. Fig. 2 shows the variation of molecular Prandtl number,  $Pr$ , as a function of molecular weight and temperature for helium-argon and helium-xenon [7]. It can be seen that the Prandtl number varies little with temperature.

Experimental correlations, such as equation 1, were developed using air ( $Pr \approx 0.7$ ) and helium ( $Pr = 0.67$ ). Extension of similar experimental correlations for calculating adiabatic friction factors, average friction factors with heat addition, Nusselt numbers at constant property

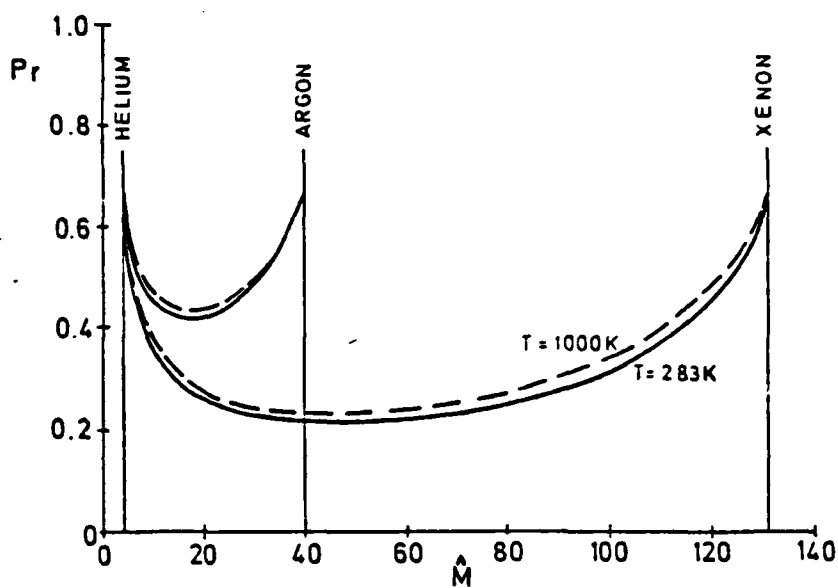


Fig. 2. Variation of Prandtl number with respect to molecular weight for helium-argon and helium-xenon.



conditions, and Nusselt numbers with variable property and thermal entry effects included were examined in this study using helium-argon mixtures. Mixtures at molecular weights of approximately 15 ( $Pr = 0.42$ ), 27 ( $Pr = 0.46$ ), and 30 ( $Pr = 0.49$ ) were used. For comparison, experiments with air and helium were also performed. Experimental studies similar to this one, except using air, helium, or hydrogen include those by Perkins and Worsøe-Schmidt [8], McEligot and Magee [9], Taylor [10], and Dalle Donne and Bowditch [11].

In many analyses that predict turbulent heat transfer results, the value of the turbulent Prandtl number is needed [12]. The turbulent Prandtl number,  $Pr_t$ , is defined as the ratio of eddy diffusivity of momentum and eddy diffusivity of heat,  $\epsilon_M/\epsilon_H$ . The eddy diffusivities are defined by the transport relationships,

$$\begin{aligned} \tau/\rho &= (\nu + \epsilon_M) \frac{\partial u}{\partial y} \\ q''/\rho c_p &= -(\alpha + \epsilon_H) \frac{\partial T}{\partial y} \end{aligned} \quad (3)$$

and are used to account for the additional momentum and heat transport caused by turbulent mixing.

Much work has been done, both analytical and experimental, to develop methods to predict  $Pr_t$ . As of yet, no generally accepted method exists. Reynolds [13] examined more than thirty ways that have been developed to determine  $Pr_t$ . For more background information his review can be consulted. Quarmby and Quirk [14] demonstrated the wide

range of  $Pr_t$  values that are predicted by different analyses and measured data. For air and other common gases, they showed that different methods predict  $Pr_t$  near the wall from 0.5 to infinity.

Due to large uncertainties [15], experimental measurements haven't clarified the discrepancies. The measurements have indicated that  $Pr_t$  is a function of  $Pr$ , position in the flow, and turbulence intensity [13]. It has been generally observed that  $Pr_t$  increases as the wall is approached, and that the relationship between  $Pr_t$  and  $Pr$  is [12,13]

$$Pr_t \lesssim 1 \text{ for } Pr \gtrsim 1 \text{ unless } Pr \sim 1. \quad (4)$$

A recent technique, developed by McEligot, Pickett, and Taylor [16], determines  $Pr_t$  in the wall region by comparing the experimentally measured and numerically calculated axial variation of Nusselt number. The Nusselt numbers are calculated for the constant properties condition, and the measured Nusselt numbers are extrapolated to a constant properties condition. The technique was used in this investigation to determine  $Pr_t$  in the wall region for mixtures of helium-argon. By comparing  $Pr_t$  for helium-argon mixtures with results for air [16], the variation of  $Pr_t$  as a function of  $Pr$  was examined. The variation of  $Pr_t$  as a function of Reynolds number was also examined.

Relatively high heating rates could possibly occur

in the heater tubes of the closed Brayton cycle. These high heating rates cause significant variation of properties, and the constant properties idealization becomes invalid. To calculate bulk Nusselt numbers of helium-argon mixtures at these conditions, the  $Pr_t$  determined for constant properties was used in a numerical analysis in which the properties were allowed to vary. To validate using  $Pr_t$  determined for constant property conditions in a variable properties analysis, calculated and measured bulk Nusselt numbers were compared. By examining this comparison, the possibility that the helium and argon had separated, due to the Soret effect [17], was examined.

## GAS PROPERTIES

The properties needed for this study were the compressibility, viscosity, thermal conductivity, specific heat, enthalpy, speed of sound, and gas constant. The properties of air have been studied extensively, and tables listing these properties are readily available. The Tables of the Thermal Properties of Gases [18] were used in this investigation. The properties of helium and helium-argon mixtures were calculated theoretically. For all of the gases, the viscosity and thermal conductivity were assumed to be independent of pressure.

The helium and helium-argon mixtures were assumed to be ideal gases, thus making the compressibility equal to a constant value of one. This is a reasonable assumption for the range of pressures (101.3 - 967.3KPa) and temperatures (294 - 828°K) used in this experiment. Since helium and argon are monatomic, and the temperatures used in this study were not too great, the equation [19]

$$c_p = (5/2) R \quad (5)$$

was used to calculate the specific heat. The specific heat was assumed to be constant, and the gas constant was calculated from the relation

$$R = R/\hat{M}. \quad (6)$$

Using the ideal gas and constant specific heat assumptions, simple equations for the enthalpy and speed of sound can

be derived [20]

$$i = c_p (T - T_{\text{ref}}) \quad (7)$$

$$c = \sqrt{\gamma R T} = \sqrt{5/3 R T} \quad (8)$$

$T_{\text{ref}}$  is an arbitrary reference temperature. From the assumptions already mentioned, the ratio of specific heats,  $\gamma$ , becomes a constant value of 5/3.

The viscosity and thermal conductivity of the helium and helium-argon mixtures were calculated using the Lennard-Jones (6-12) potential in the Chapman-Enskog kinetic theory [17]. The predicted properties were compared with experimental measurements.

The force constants,  $\epsilon/k$  and  $\sigma$ , suggested by Hirschfelder, Curtiss and Bird [17] were tried originally. The predicted properties were compared with the experimental values only for the range of temperatures used in this study. The predicted helium viscosities were five percent below the experimental measurements of Dawe and Smith [21] and Kalelkar and Kestin [22]. The predicted thermal conductivities of helium agreed within one percent of the measurements by Saxena and Saxena [23], but were five percent below the values calculated from experimental viscosity measurements of Kalelkar and Kestin [22]. The predicted viscosities of helium-argon mixtures at 870°K were three to five percent below the measured values of Kalelkar and Kestin [22]. The predicted thermal conductivities of helium-argon mixtures at 790°K were five to

nine percent below the measured values of the Thermophysical Properties Research Center [24], and the measured values of von Ubisch repeated by Gandhi and Saxena [25].

In an attempt to get better agreement between predicted and measured values, force constants suggested by DiPippo and Kestin [26] were tried. With these force constants, the predicted viscosities of both helium and helium-argon agreed within one percent of the measured values mentioned in the previous paragraph. The predicted thermal conductivities of helium agreed within one percent of the values of Kalelkar and Kestin [22], but were five percent above the measurements of Saxena and Saxena [23]. The predicted thermal conductivities of helium-argon were essentially unchanged. Since the agreement between the predicted and measured viscosities was improved, and the agreement between the predicted and measured thermal conductivities remained approximately the same, the force constants suggested by DiPippo and Kestin [26] were used. The calculated properties of helium and the helium-argon mixtures used in this investigation are listed in Appendix A.

The properties were inserted in tabular form in the numerical programs that reduced the experimental friction and heat transfer measurements. In the numerical program used to predict heat transfer results, the properties were inserted in equation form. The ideal gas law was used, the specific heat was assumed constant, and the variation

of viscosity and thermal conductivity with temperature was accounted for with the following relations.

$$\mu/\mu_{\text{ref}} = (T/T_{\text{ref}})^a \quad (9)$$

$$K/K_{\text{ref}} = (T/T_{\text{ref}})^b \quad (10)$$

As discussed by McEligot, Taylor, and Durst [7], the exponent "a" ranges from 0.7 to 0.8, and the exponent "b" ranges from 0.7 to 0.75 for the inert gases and their mixtures. The exponents, "a" and "b", of air for the range of temperatures in this study are 0.67 and 0.81, respectively. Thus, the viscosity and thermal conductivity of air, helium, and helium-argon vary with temperature in approximately the same manner.

For the present study the following values of the exponents were used for the mixtures:

$$\text{at } \hat{M} = 15.83, \quad a = 0.745 \text{ and } b = 0.718$$

$$\text{at } \hat{M} = 27.53, \quad a = 0.772 \text{ and } b = 0.741.$$

## EXPERIMENTAL APPARATUS AND PROCEDURE

The experimental apparatus, arrangement, and procedure was similar to that used by Perkins, Schade, and McEligot [27]. Only differences in the two experiments will be noted here. Instead of a square duct, a circular tube made of Hastelloy-X was used as a test section. The tube had an inside diameter of 0.312 cm. and a wall thickness of 0.056 cm. The test section consisted of a heated section 98 diameters in length preceded by an unheated section 92 diameters in length. The unheated section ensured that the velocity profile was fully developed at the inlet of the heated section. For attachment of the a.c. power cables, stainless steel electrodes were brazed at the upper and lower ends of the heated section. Two pressure taps were used. One was located in the lower electrode and the other 8.0 diameters below the upper electrode. Sixteen premium grade chromel-alumel thermocouples (0.013 cm. diameter) were spot welded to the heated section of the tube using the parallel junction suggested by Moen [28].

In addition to the power supply used by Perkins et al. [27], an a.c. Lincoln welder was used in order to reach the high temperatures at the larger Reynolds numbers used in this experiment. To measure the higher flow rates, the positive displacement meter was replaced by a Meriam



laminar flow element. The latter was calibrated to measure the flow rate within  $\pm 1.5$  percent. Heise gages, inclined water manometers, and vertical mercury or water manometers were used to measure static pressure and pressure drop.

A vacuum external environment was not used in this experiment. The test section was completely enclosed with a heat shield that restricted the convective air currents and helped stabilize the heat loss from the tube to the environment.

The experimental procedure was slightly different than that used by Perkins et al. [27]. The "radiating thermocouple conduction error", discussed by Hess [29], was not exactly appropriate since the test section was surrounded by air at atmospheric pressure. Instead a correlation for natural convection from small wires was introduced, in addition to radiation, as detailed in Appendix E. The heat loss from the tube to the environment was determined using the method described by Campbell and Perkins [30].

To reduce the heat transfer data the same computer program that was used by Perkins et al. [27], was employed in this study, but was modified for use with a circular tube. The basics of this computer program are described

in other reports [30,31,32]. Table 1 summarizes the range of variables covered in this investigation. A more detailed discussion of the experiment is contained in Appendix B. A list of the experimental data is contained Appendix D.

TABLE 1 .  
Range of Variables in  
the Present Experiment

	Air	Helium	Helium-Argon
Experimental runs	25	4	28
Molecular weight	28.97	4.003	15.30 - 29.70
Inlet bulk Reynolds number	32900 - 100000	30200	31200 - 102000
Exit bulk Reynolds number	19900 - 89000	18400 - 26600	17000 - 68000
Inlet bulk Prandtl number	0.719	0.667	0.419 - 0.486
Exit bulk Prandtl number	0.682 - 0.708	0.667	0.426 - 0.495
Maximum $T_w/T_b$	1.90	1.75	1.82
Maximum $T_w$ ( $^{\circ}\text{K}$ )	817	789	828
Maximum $q^+$	0.0027	0.0027	0.0032
Maximum $\text{Gr}/\text{Re}_1^2$	$8.90 \times 10^{-5}$	$4.84 \times 10^{-5}$	$3.22 \times 10^{-3}$
Maximum Mach number	0.26	0.25	0.33
$x/D$ for local bulk Nusselt numbers	2.1 - 82.0	2.1 - 82.0	2.1 - 82.0

## EXPERIMENTAL RESULTS

### Friction Results

Adiabatic friction factors were measured before each series of heated runs. These were compared to other researcher's results, and were also used as a check of the pressure, mixture molecular weight, and flow rate measurements. The method described by Shapiro [33] was used to calculate the adiabatic friction factors. The measured friction factors were compared to the experimental correlation of Drew, Koo, and McAdams [34],

$$f = 0.0014 + 0.125 \text{ Re}^{-0.32}. \quad (11)$$

This correlation is for turbulent flow in tubes, and was used because of its simplicity and close agreement with the Kármán-Nikuradse relation. Fig. 3 shows the measured friction factor divided by that calculated from equation (11) plotted as a function of Reynolds number. Air and helium data points are included for comparison. All the measured friction factors are within  $\pm 4.0$  percent of equation (11), and 76 percent are within  $\pm 2.0$  percent.

Since only two pressure taps were used, local friction factors could not be determined for experiments with heat addition. Average friction factors were determined in the manner of Humble, Lowdermilk, and Desmon [35]. The average friction factors were compared to an experimental correlation suggested by Taylor [36]. This correlation is for

turbulent flow in tubes with heat addition.

$$f = (0.0014 + 0.125 \text{Re}_w^{-0.32}) (T_w/T_b)^{-0.5} \quad (12)$$

This relation is similar to equation (11), but the bulk Reynolds number is replaced by the modified wall Reynolds number. The term  $(T_w/T_b)^{-0.5}$  is included to account for variation of properties with temperature. Equation (12) was used by Taylor to correlate average friction coefficients measured by several different people. It predicted most of the data within  $\pm 10$  percent.

Fig. 4 shows the average friction factors with heat addition as measured in this investigation. The friction coefficients are divided by equation (12) and plotted as a function of modified wall Reynolds number. Again, helium and air are included for comparison. All of the data is predicted to within  $\pm 10$  percent by equation (12) and 84 percent is predicted to within  $\pm 4.0$  percent.

#### Heat Transfer Results

To determine the effects of the lower helium-argon Prandtl number on the heat transfer results, the variation of properties with temperature, and the entrance effects were minimized. The entrance effects were minimized by considering primarily the results at which fully developed conditions existed ( $x/D > 20$ ). A method described by Malina and Sparrow [37] was used to approach the constant properties idealization.

For the method described by Malina and Sparrow, a

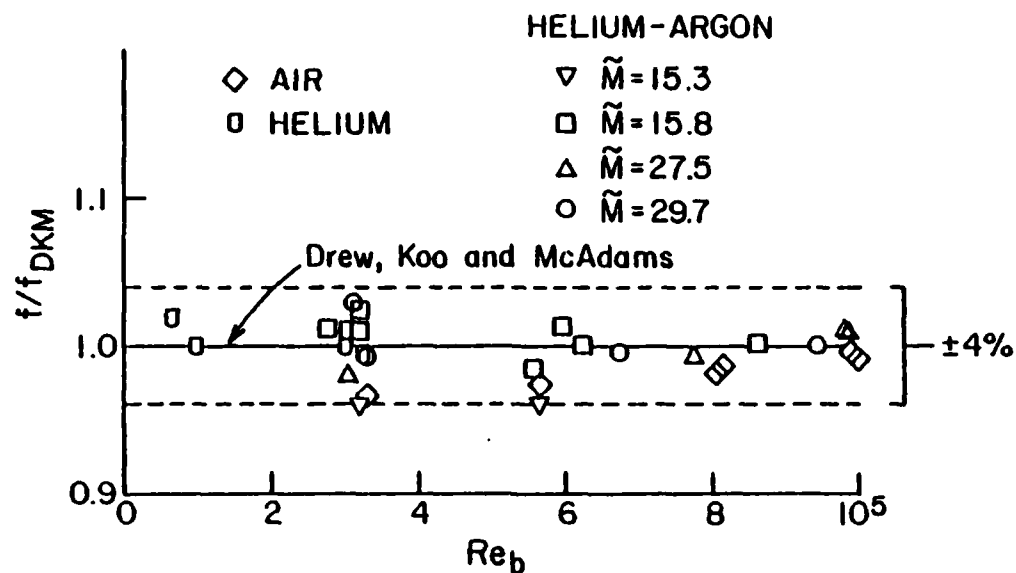


Figure 3. Comparison of Adiabatic Friction Factors to Drew, Koo and McAdams Correlation for Air, Helium and Helium-Argon Mixtures.

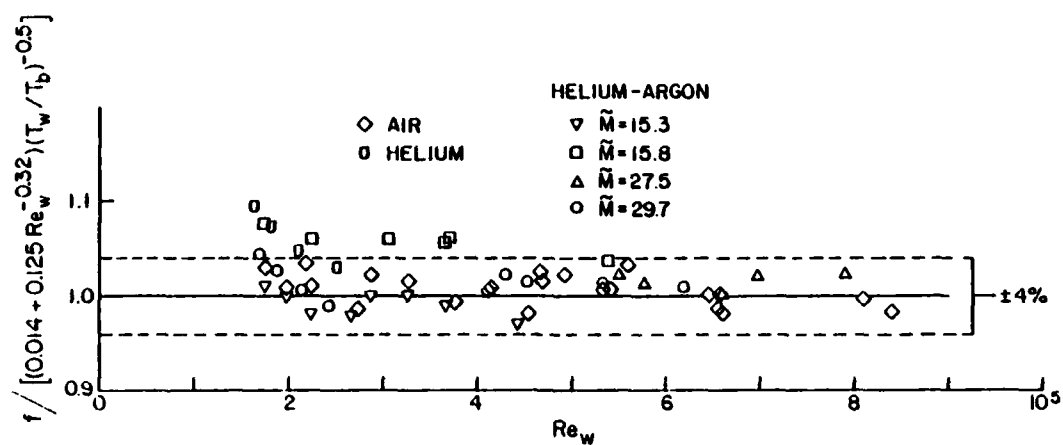


Figure 4. Comparison of Average Friction Factors to Taylor Variable Properties Correlation for Air, Helium and Helium-Argon Mixtures.

fixed inlet Reynolds number is maintained while the wall-to-bulk temperature difference is varied. At a particular axial location, the ratio of experimentally determined bulk Nusselt number to a Dittus-Boelter type correlation is plotted as a function of the difference between wall and bulk temperature. Extrapolation to a difference of zero between the wall and bulk temperature gives a ratio that can be directly used to calculate a constant property Nusselt number,  $Nu_{cp}$ . Since the ratio of bulk Nusselt number to a Dittus-Boelter type correlation partially eliminates any effects caused by small deviations of the Reynolds number, these deviations should be kept as small as possible.

The procedure described in the previous paragraph is demonstrated in Fig. 5 for a helium-argon mixture with a molecular weight of 15.30, inlet Reynolds number of 55200, and inlet Prandtl number of 0.419. Extrapolation for four different axial locations is shown. For this investigation the Dittus-Boelter type correlation used was (equation 1 rearranged)

$$Nu_{DB} = 0.021 Re^{0.8} Pr^{0.4}. \quad (13)$$

For a sequence of runs at a nominal inlet Reynolds number, all individual runs had inlet Reynolds numbers within 1.8 percent of the nominal value.

The dashed lines in Fig. 5 show how the error in the constant property Nusselt number was estimated. This

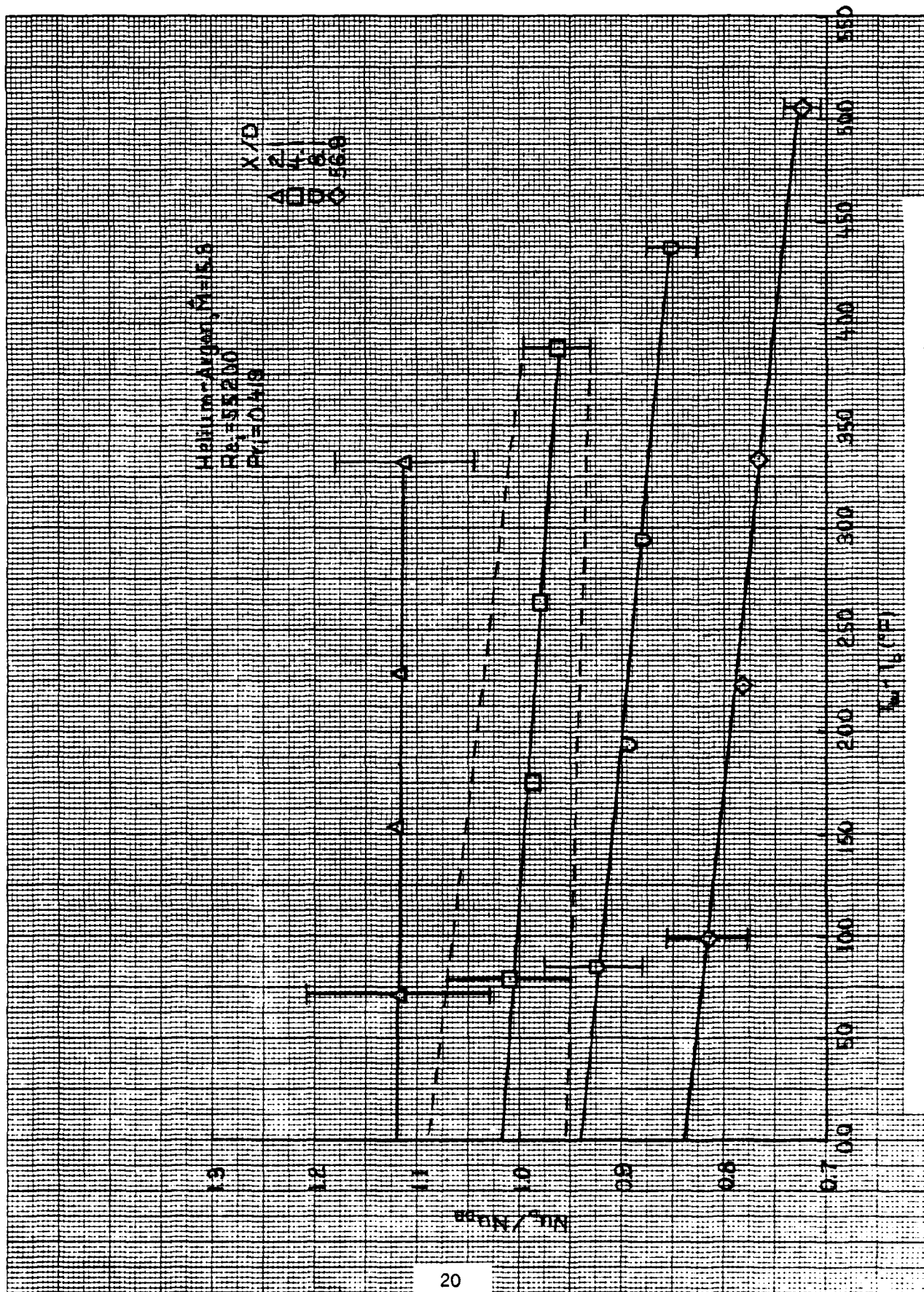


Fig. 5. Technique for determining constant property Nusselt numbers.



technique was used by Reynolds, Swearingen, and McEligot [38]. The error in this investigation varied from  $\pm 9$  percent at small  $x/D$  to  $\pm 5.4$  percent at large  $x/D$ . The dominant uncertainty in the Nusselt number is due to uncertainty in the wall-to-bulk temperature difference. This difference is small in the entrance region, thus causing a large error in the Nusselt number. At large  $x/D$ , the flow is fully developed and the wall-to-bulk temperature difference is relatively constant. The error in the Nusselt number becomes a minimum, and then increases with increasing  $x/D$  due to greater uncertainty in the bulk temperature. Appendix C describes the method used for calculating error in the measured Nusselt number.

For fully developed conditions ( $x/D > 20$ ), with air or helium as the experimental fluid, the ratio  $Nu_{cp}/Nu_{DB}$  varied from 0.94 to 1.00. No dependence on Reynolds number was noticed for the Reynolds number range used in this experiment. For fully developed conditions, with helium-argon mixtures as the experimental fluid, the ratio  $Nu_{cp}/Nu_{DB}$  varied from 0.83 to 0.93. For a helium-argon mixture at a molecular weight of 15.30, inlet Reynolds number of 55200, and  $x/D$  value of 56.9, Fig. 5 shows the ratio  $Nu_{cp}/Nu_{DB}$  to be approximately 0.84. From these results, it was determined that the Dittus-Boelter type equation (equation 13) did not predict correct Nusselt numbers for

the Prandtl number range between 0.42 and 0.50.

A correlation suggested by Kays [39] predicted the constant property Nusselt numbers of the helium-argon mixtures within  $\pm 6.0$  percent.

$$Nu = 0.022 Re^{0.8} Pr^{0.6} \quad (14)$$

This equation was recommended for fluids with Prandtl numbers between 0.5 and 1.0, constant properties, a constant heat flux boundary condition, and fully developed turbulent flow. If the coefficient of this equation is changed to 0.021, and the Prandtl number exponent adjusted so that approximately equivalent results are obtained, the resulting equation is

$$Nu = 0.021 Re^{0.8} Pr^{0.55} \quad (15)$$

This equation shows that the exponent of the Prandtl number in equation (13) should be changed from 0.4 to 0.55 in order to accurately predict the constant property Nusselt numbers of the helium-argon mixtures. Fig. 6 shows the constant property Nusselt number divided by equation (15) plotted as a function of Prandtl number for the mixtures. Results are plotted for three Prandtl numbers, four Reynolds numbers, and axial positions at which the flow was fully developed. From the figure it can be seen that equation (15) predicts the constant property Nusselt numbers within  $\pm 5.0$  percent. At a Reynolds number of 32000, a small effect of the Prandtl number varying between 0.419 and 0.486 can be noticed.

A dependence on Reynolds number was observed for the

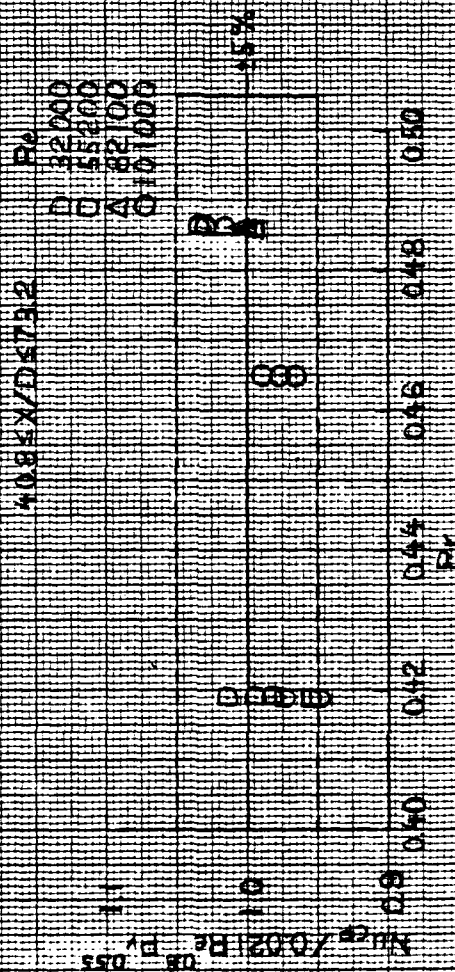


Fig. 6. Comparison of constant property Nusselt numbers to equation 15 for fully developed conditions of helium-argon mixtures.

helium-argon mixtures. Since the effect on the constant property Nusselt number was about equivalent to the error in the constant property Nusselt number, only general trends can be discussed. Two trends were observed (Fig. 6). For a particular Prandtl number the ratio of  $Nu_{cp}$  divided by equation (15) decreased as the Reynolds number increased, and this effect became more pronounced as the Prandtl number decreased.

To account for the variation of properties and entrance effects in this investigation, the correction factors suggested by Magee [40] were used.

$$[(T_w/T_b)^{-0.4} + 0.6D/x] \quad (16)$$

The term  $(T_w/T_b)^{-0.4}$  accounts for the variation of properties, and the term  $0.6D/x$  accounts for the entrance effects. If these correction factors are applied to equation (13), the resulting equation is

$$Nu_b = 0.021 Re_b^{0.8} Pr_b^{0.4} [(T_w/T_b)^{-0.4} + 0.6D/x]. \quad (17)$$

For  $x/D$  between 2.1 and 81.6 this equation predicted all of the present measured Nusselt numbers for air and helium within  $\pm 15$  percent and 97 percent of the Nusselt numbers within  $\pm 10$  percent.

If the correction factors (16) are applied to equation (15) the resulting relation is

$$Nu_b = 0.021 Re_b^{0.8} Pr_b^{0.55} [(T_w/T_b)^{-0.4} + 0.6D/x]. \quad (18)$$

This equation predicted the helium-argon Nusselt numbers in the fully developed region within  $\pm 13$  percent, but

underpredicted the Nusselt numbers in the entrance region by as much as 22 percent. To have the same type of accuracy with the helium-argon data that was obtained with the air and helium data changes to the correlation were necessary.

As previously discussed, the transport properties of helium-argon vary with temperature in approximately the same manner as those of air and helium. For this reason the term  $(T_w/T_b)^{-0.4}$  was retained as a reasonably accurate correction factor for the variation of properties. Kays [39] discusses the effect of different Prandtl numbers in the thermal entrance region of circular tubes. He shows that as the Prandtl number decreases, the effect of the entrance region on the Nusselt number is more pronounced. Because of this, the coefficient in the term  $0.6D/x$  of equation (18) was changed. Since helium-argon has a lower Prandtl number than air, one would expect the coefficient to have a larger value than 0.6. Different values for the coefficient of the entrance effects term were used in equation (18), and compared to the experimentally determined bulk Nusselt numbers of helium-argon. From this comparison it was determined that a value of 0.85 worked best for the coefficient of the entrance effects term. The complete correlation, accounting for entrance effects and variation of properties is

$$Nu_b = 0.021 Re_b^{0.8} Pr_b^{0.55} [(T_w/T_b)^{-0.4} + 0.85D/x]. \quad (19)$$

For  $x/D$  between 2.1 and 81.6 this equation predicted all

of the measured bulk Nusselt numbers for helium-argon within  $\pm 15$  percent and 92 percent within  $\pm 10$  percent.

Measured bulk Nusselt numbers divided by equation (19) are plotted on Fig. 7 as a function of  $x/D$ . For clarity, only results from four helium-argon experimental runs were plotted. The data plotted are from experimental runs that include the complete range of experimental variables for the helium-argon mixtures. The greatest difference between the experimental data and equation (19) occurred at high heating rates in the  $x/D$  range between 4.0 and 16.0. In this range equation (19) underpredicted the measured Nusselt numbers by 5 to 15 percent.

Few correlations for gases with Prandtl numbers between 0.1 and 0.67 presently exist in the literature. Sleicher and Rouse [41] suggest a correlation for Prandtl numbers between 0.1 and  $10^5$ , and Reynolds numbers between  $10^4$  and  $10^6$ . The correlation is for fully developed conditions, and accounts for property variation.

$$\begin{aligned} \text{Nu}_b &= 5 + 0.015 \text{Re}_f^m \text{Pr}_w^n \\ m &= 0.88 - 0.24/(4 + \text{Pr}_w) \\ n &= 1/3 + 0.5 \exp(-0.6 \text{Pr}_w) \end{aligned} \quad (20)$$

For the helium-argon mixtures, this equation predicted Nusselt numbers that were 15 to 40 percent lower than the Nusselt numbers measured in the fully developed region of this investigation. Equation (19) correlated the data more accurately.

Molecular Weight	Inlet Reb	Outlet Reb	Prb	$q^+$ Max	$(T_w/T_b)_{Max}$
D 15.30	54800	36200	0.419	0.0019	1.54
□ 15.83	80600	60900	0.419	0.0012	1.39
Δ 27.53	101000	87500	0.465	0.0005	1.19
○ 29.70	31200	17000	0.486	0.0032	1.78

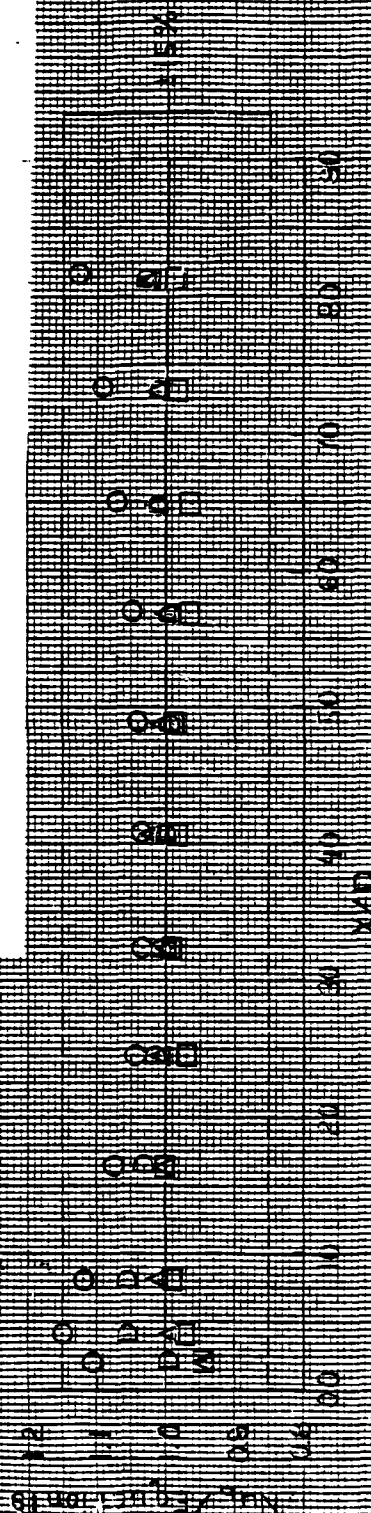


Fig. 7. Comparison of local bulk Nusselt numbers to equation 19 for helium-argon mixtures.

## NUMERICAL ANALYSIS

### Procedure for Determining the Turbulent Prandtl Number

To determine  $Pr_t$  for helium-argon mixtures, the numerical method of Bankston and McEligot [42] was used in conjunction with the technique developed by McEligot, Pickett, and Taylor [16]. The numerical method uses finite control volume approximations. It was developed to solve the coupled, partial differential, axisymmetric, boundary layer equations; but can also be used for constant property conditions which uncouples the boundary layer equations. The boundary conditions are the no-slip and impermeable-wall conditions, the inlet conditions, and the wall heat flux.

The technique of McEligot et al. [16] uses the axial variation of the Nusselt number to determine  $Pr_t$  in the wall region. By examination of the simplified energy equation,

$$u \frac{\partial T}{\partial x} = 1/r \frac{\partial}{\partial r} [r(\alpha + \epsilon_M/Pr_t) \frac{\partial T}{\partial r}] \quad (21)$$

they showed that the functional dependence of the Nusselt number is

$$Nu = Nu \{x, u(r), \epsilon_M(r), Pr_t\}. \quad (22)$$

The energy equation was simplified from the general form by using the following assumptions: the axisymmetric boundary layer approximations, hydrodynamic fully developed flow, steady flow at low velocities, and constant fluid



properties. By using one of the semi-empirical relationships for  $\epsilon_M(r)$  to determine the velocity profile,  $u(r)$ , they obtained the result  $Nu = Nu \{x, Pr_t\}$ . They inverted this relationship to obtain  $Pr_t = Pr_t \{Nu(x)\}$ . If  $Pr_t$  is considered one-dimensional, comparison of experimental measurements of  $Nu(x)$  with calculated values of  $Nu(x)$  can be used to determine  $Pr_t(r)$ . McEligot et al. [16] pointed out that direct inversion would be difficult, and iterative use of the numerical procedure described in the previous paragraph was used. The radial variation of the turbulent Prandtl number was assumed to be

$$P_r = Pr_{t,w} + \frac{d(Pr_t)}{d(y/r_w)} (y/r_w). \quad (23)$$

The results of McEligot et al. [16] showed that a change of  $Pr_t$  in the wall region from 1 to  $\frac{1}{2}$  caused changes of 30 to 45 percent in  $Nu(x)$ , whereas a change of  $Pr_t$  in the core only caused small changes. For air at a Reynolds number of 44500 and a Prandtl number of 0.72 they determined that

$$Pr_{t,w} = 0.9 \pm 0.1 \text{ and } \frac{d(Pr_t)}{d(y/r_w)} = 0. \quad (24)$$

The typical errors of the experimentally measured Nusselt numbers did not allow calculation of  $\frac{d(Pr_t)}{d(y/r_w)}$ .

To determine  $\epsilon_M(r)$  in this investigation, the van Driest mixing length model [43] was used in conjunction with the

Reichardt middle law [54].

$$\begin{aligned} \ell_{VD} &= \kappa y [1 - \exp(-y^+/y_\ell^+)] \\ \epsilon_{VD} &= \ell_{VD}^2 \frac{\partial u}{\partial y} \text{ and } \epsilon_M = \epsilon_{VD} \cdot (2 - \frac{Y}{r_w}) \cdot [1 + 2(\frac{r}{r_w})^2] / 6 \end{aligned} \quad (25)$$

The values of  $\kappa$  and  $y_\ell^+$  were 0.4 and 26, respectively.

With these constants, the predicted friction factors agreed within one percent of equation (11) for the range of Reynolds numbers used in this study. In this study, as in the study by McEligot et al. [16], the errors in the experimentally measured Nusselt numbers did not allow calculation of  $\frac{d(Pr_t)}{d(y/r_w)}$ . The inlet Reynolds number, inlet Prandtl number, constant properties condition, wall heat flux variation, and different values of  $Pr_t$  were used as input to the numerical procedure. For the first three diameters, the experimental axial wall heat flux variation resembled an exponential approach to a constant value as  $x$  increased. For the remaining length, the wall heat flux was constant within two percent. The same axial variation of wall heat flux was used for all of the constant property numerical calculations.

From the numerical analysis the axial variation of  $Nu_{cp}$  was calculated. By comparing graphs of the experimentally measured  $Nu_{cp}$  and the calculated  $Nu_{cp}$  (examples in Fig. 8),  $Pr_{t,w}$  for helium-argon mixtures was determined. The variation of  $Pr_{t,w}$  with respect to Reynolds number was examined by comparing  $Nu_{cp}$  at different Reynolds numbers,

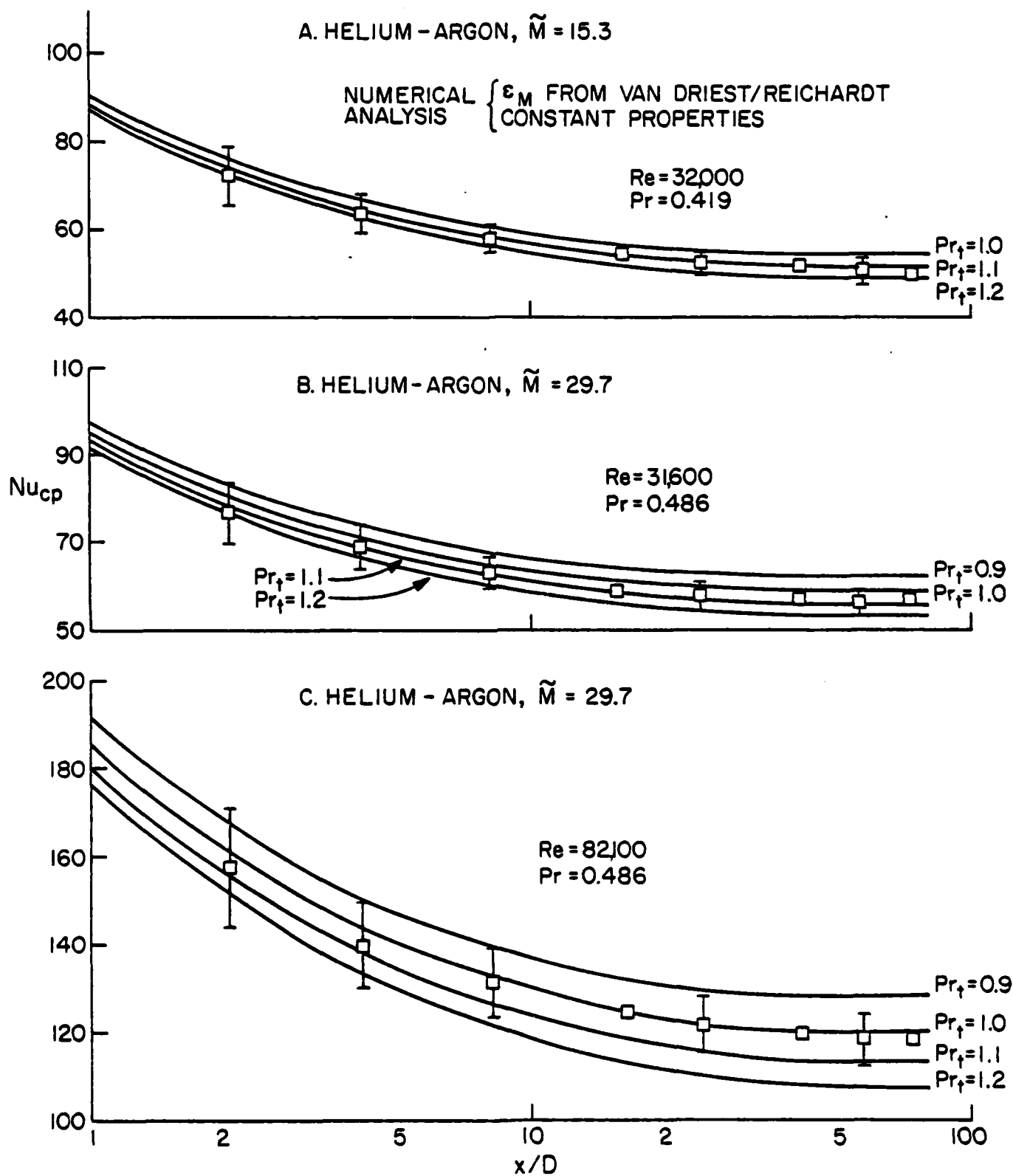


Figure 8. Examples of the Comparisons Between Measured  $Nu_{cp}(x)$  and Predicted  $Nu(x)$  as Used to Deduce  $Pr_{tw}$  for Constant Properties.

but the same Prandtl number. The variation of  $Pr_{t,w}$  with respect to Prandtl number was examined by comparing  $Nu_{cp}$  at different Prandtl numbers, but the same Reynolds number.

#### Procedure for Studying High Heating Rates

As mentioned in the Introduction, relatively high heating rates could possibly occur in the heater tubes of the closed Brayton cycle. To calculate  $Nu_b$  for helium-argon mixtures at these high heating rates, the numerical method of Bankston and McEligot [42], discussed in the previous section, was used. Properties were allowed to vary, and the relations (9,10) discussed in the Gas Properties section were used. The simple van Driest/Reichardt model eqn. (25), and  $Pr_{t,w}$  determined for helium-argon at constant property conditions were incorporated. No radial variation of  $Pr_t$  was included, thus,  $Pr_t = Pr_{t,w}$ . The axial variation of wall heat flux was similar to the one used for the constant property calculations, but was modified slightly for each experimental run to agree with the wall heat flux variation determined from the experimental measurements.

The axial variation of measured  $Nu_b$  from two helium-argon experimental runs was compared to the calculated axial variation of  $Nu_b$ . From a series of runs with approximately equivalent inlet Reynolds and Prandtl numbers, the runs with the highest and lowest heating rate were

chosen. Since the  $Pr_t$  used was for constant properties, one would expect agreement of measured and calculated  $Nu_b$  at the low heating rate. If the measured and calculated  $Nu_b$  at the high heating rate agreed, this would validate the use of  $Pr_t$  determined from constant property conditions for conditions in which properties varied significantly. If the results at the high heating rate did not agree, this might indicate that either,  $Pr_t$  determined for constant properties could not be used for variable property conditions, or that some other phenomenon, such as the Soret effect, was acting.

#### Turbulent Prandtl Number Results and Discussion

Fig. 8 illustrates examples of the comparisons between measured  $Nu_{cp}$  and calculated  $Nu_{cp}$  used to determine  $Pr_{t,w}$ . Examples for three Reynolds numbers and two Prandtl numbers are shown. Curves of the calculated  $Nu_{cp}$  are included at four different  $Pr_t$  (0.9, 1.0, 1.1, 1.2). Brackets indicating the experimental error of the measured  $Nu_{cp}$  are also included. Because of the large error in the immediate thermal entry, only results for  $x/D$  greater than eight were used to determine  $Pr_{t,w}$ .

Fig. 8a shows the measured and calculated  $Nu_{cp}$  for a helium-argon mixture with a molecular weight of 15.30, Prandtl number of 0.419, and Reynolds number of 32000. By examining results of similar graphs,  $Pr_{t,w}$  was determined to be  $1.1 \pm 0.1$  for helium-argon mixtures with molecular

weights of approximately 15, Prandtl numbers of 0.42, and Reynolds numbers between 32000 and 55200. The measured and calculated  $Nu_{cp}$  are shown in Fig. 8b and 8c for a helium-argon mixture at a molecular weight of 29.70, Prandtl number of 0.486, and Reynolds numbers of 31600 and 82100. From results of similar graphs,  $Pr_{t,w}$  was determined to be  $1.0 \pm 0.1$  for helium-argon mixtures with molecular weights between 27 and 30, Prandtl numbers between 0.46 and 0.49, and Reynolds numbers between 31600 and 102000.

The effect of Reynolds number on  $Pr_{t,w}$  can be examined qualitatively using the results in Fig. 8b and 8c. These results are for the same Prandtl number ( $Pr = 0.486$ ), but Reynolds numbers of 31600 and 82100. For  $x/D$  greater than eight, and at the low Reynolds number, the measured  $Nu_{cp}$  are slightly below the calculated  $Nu_{cp}$  for a  $Pr_{t,w}$  of 1.0. At the high Reynolds number and same axial length, the measured  $Nu_{cp}$  are slightly above the calculated  $Nu_{cp}$  for a  $Pr_{t,w}$  of 1.0. For the stated conditions, it appears that  $Pr_{t,w}$  has a weak dependence on Reynolds number, and decreases slightly as the Reynolds number increases.

The effect of molecular Prandtl number on  $Pr_{t,w}$  can be examined using the results from Fig. 8a and 8c summarized in Table 2. The results (24) of McEligot, Pickett and Taylor [16] for air may also be used since the mixture results appear to show that  $Pr_{t,w}$  varies only slightly with Reynolds number.

Table 2. Variation of  $Pr_{t,w}$  with respect to Prandtl number.

Gas	Molecular Weight	Prandtl Number	$Pr_{t,w}$	Reynolds Number
Helium-argon	15.30	0.419	$1.1 \pm 0.1$	32000
Helium-argon	29.70	0.486	$1.0 \pm 0.1$	31600
Air	28.97	0.72	$0.9 \pm 0.1$	44500

For the range of Prandtl numbers in Table 2,  $Pr_{t,w}$  has a relatively strong dependence on Prandtl number and decreases as Prandtl number increases. This dependence agrees with that (equation 4) noted by Reynolds [13].

#### High Heating Rate Results and Discussion

Fig. 9 shows the results of the measured and calculated axial variation of  $Nu_b$  for the two experimental runs that were investigated. The two runs were for a helium-argon mixture at a molecular weight of 29.70, inlet Prandtl number of 0.486, inlet Reynolds numbers of 32000 and 31200, and maximum heating rates of  $q^+ = 0.0006$  and  $q^+ = 0.0032$ . Since at a  $Pr_t$  value of 1.0, the measured  $Nu_{cp}$  in Fig. 8b were slightly below the calculated  $Nu_{cp}$ , a  $Pr_t$  value of 1.02 was used. The constants, "a" and "b" in equations (9) and (10) were 0.772 and 0.741, respectively. For both heating rates, the calculated axial variation of  $Nu_b$  in Fig. 9 agreed with the measured axial variation of  $Nu_b$ , within the accuracy of the measured values. From this example, it appears that  $Pr_{t,w}$  determined from constant property results can be used to calculate  $Nu_b$  for variable property conditions with heating rates up to,  $q^+ = 0.0032$ .

At high heating rates a large temperature gradient exists from the wall to the centerline of the tube. At

sufficiently high heating rates, the possibility of separation of the helium and argon due to the Soret effect arises. If separation did occur,  $Nu_b$  at a particular axial location would be expected to change since pure helium or argon have higher Prandtl numbers than helium-argon mixtures. For the high heating experimental run in Fig. 9, the largest wall-to-bulk temperature ratios occur in the axial range,  $8.1 < x/D < 16.4$ . In this axial range, the measured  $Nu_b$  do fall slightly above the calculated  $Nu_b$ , but this can not necessarily be attributed to the Soret effect, since the calculated  $Nu_b$  are within the experimental accuracies of the measured  $Nu_b$ .

The effect of high heating on the axial variation of  $Nu_b$  can be examined by comparing the low and high heating rate results in Fig. 9. Since the thermal conductivity and viscosity of helium-argon increase as the temperature increases (equations 9,10), this causes  $Nu_b$  for high heat flux conditions to be lower than  $Nu_b$  for low heat flux conditions. In the immediate thermal entrance region ( $x/D < 5$ ), the small rise in bulk gas temperature has not caused significant bulk property variation, and the  $Nu_b$  for the two heating rates are approximately the same. In the fully developed region, the large rise in bulk gas temperature has caused large property variations, and  $Nu_b$  are quite different. At  $x/D = 57$ ,  $Nu_b$  for  $q_{Max}^+ = 0.0032$  is 29 percent lower than  $Nu_b$  for  $q_{Max}^+ = 0.0006$ .



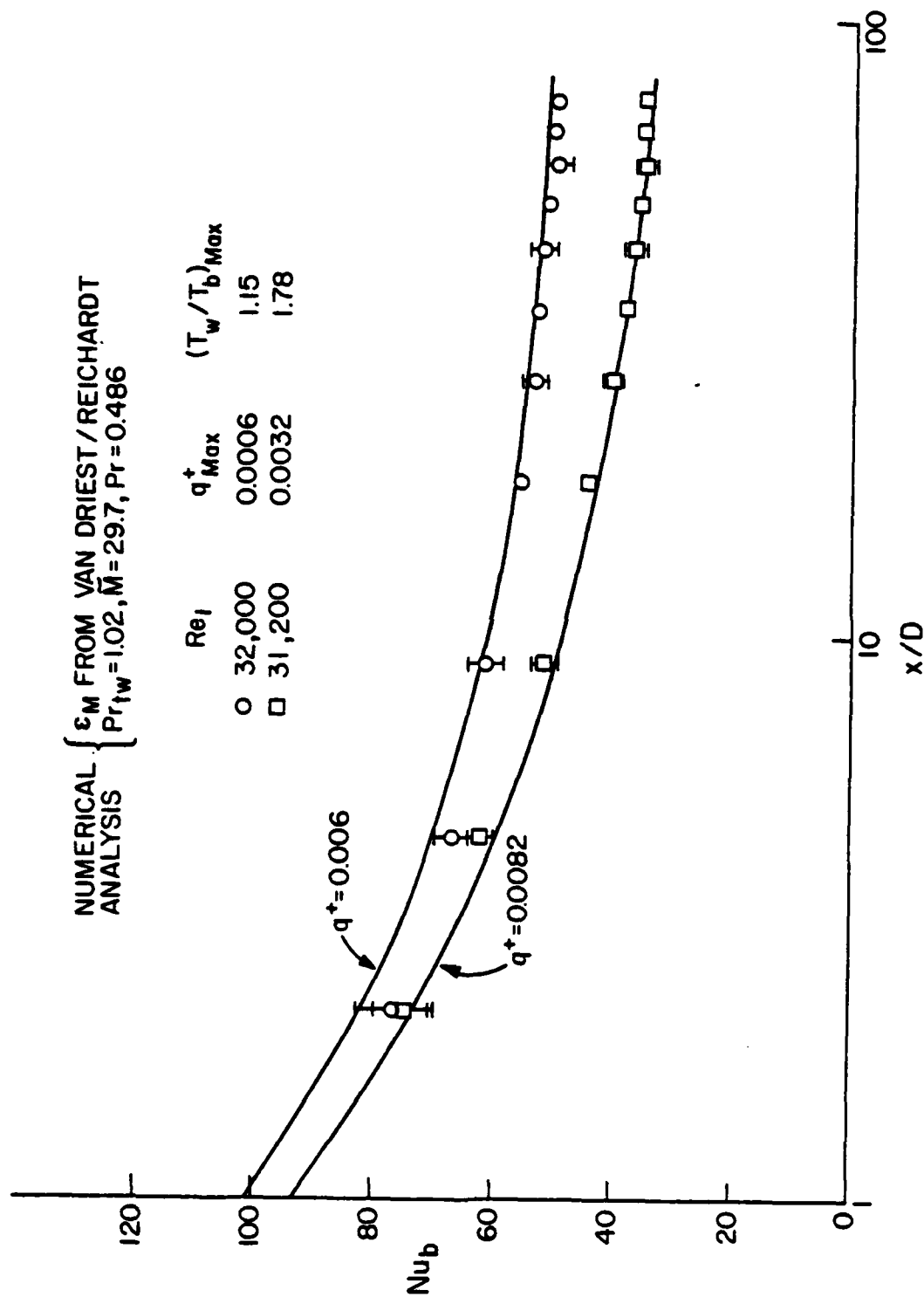


Figure 9. Comparison of Data to Numerical Predictions Accounting for Transport Property Variation.

## CONCLUSIONS

The object of this investigation was to study the momentum and heat transfer characteristics for turbulent flow of helium-argon mixtures in tubes. Experimental results were compared to existing experimental correlations, and to results from a numerical analysis. From this investigation the following conclusions have been made:

1. Existing experimental correlations, such as the Drew, Koo, and McAdams relation [34],

$$f = 0.0014 + 0.125 \text{ Re}^{-0.32}$$

predict the helium-argon adiabatic friction factors within  $\pm 4.0$  percent for turbulent flow in tubes with Reynolds numbers between 31200 and 102000.

2. A correlation suggested by Taylor [36],

$$f = (0.0014 + 0.125 \text{ Re}_w^{-0.32}) (T_w/T_b)^{-0.5}$$

predicts average friction factors within  $\pm 10$  percent for heated turbulent flow of helium-argon mixtures in tubes with inlet Reynolds numbers between 31200 and 102000.

3. Dittus-Boelter type correlations developed from air and helium experimental data

$$\text{Nu} = 0.021 \text{ Re}^{0.8} \text{ Pr}^{0.4}$$

overpredict helium-argon Nusselt numbers for constant property, fully developed conditions by as much as 17 percent. An equation of similar form,

$$Nu = 0.021 Re^{0.8} Pr^{0.55}$$

but with the exponent of the Prandtl number changed to 0.55 predicts constant property Nusselt numbers of helium-argon mixtures within  $\pm 5.0$  percent. The range of Prandtl numbers was between 0.419 and 0.486, and the range of Reynolds numbers was between 31200 and 102000.

4. For the same range of Reynolds numbers and Prandtl numbers, the entrance and properties variation effects can be accounted for by using the equation

$$Nu_b = 0.021 Re_b^{0.8} Pr_b^{0.55} [(T_w/T_b)^{-0.4} + 0.85 D/x].$$

This equation predicted the bulk Nusselt numbers of helium-argon mixtures within  $\pm 15$  percent for  $x/D$  between 2.1 and 81.6 and a maximum wall-to-bulk temperature ratio of 1.82.

5. For helium-argon mixtures with molecular weights between 14 and 20, Prandtl numbers of 0.42, Reynolds numbers between 32000 and 55000, and constant property conditions the turbulent Prandtl number in the wall region,  $Pr_{t,w}$  was determined to be  $1.1 \pm 0.1$ .

6. For helium-argon mixtures with molecular weights between 27 and 30, Prandtl numbers between 0.46 and 0.49, Reynolds numbers between 32000 and 102000, and constant property conditions  $Pr_{t,w}$  was determined to be  $1.0 \pm 0.1$ .

7. For Reynolds numbers between 30000 and 100000,  $Pr_{t,w}$  is a weak function of Reynolds number. For the Prandtl number range between 0.42 and 0.72,  $Pr_{t,w}$  is

a strong function of Prandtl number, and decreases as Prandtl number increases.

8. At maximum wall heating rates of  $q^+ = 0.0032$  ( $(T_w/T_b)_{\text{Max}} = 1.78$ ),  $Pr_{t,w}$  determined from constant property conditions can be used in a variable properties numerical analysis to calculate  $Nu_b(x)$ . For the particular experimental run studied ( $Re_i = 31200$ ,  $Pr_i = 0.486$ ,  $Pr_{t,w} = Pr_t = 1.02$ ), calculated  $Nu_b(x)$  agreed with measured  $Nu_b(x)$ , within the accuracy of the measured values. No separation of the helium-argon mixture was apparent.

APPENDICES

# APPENDIX A. Gas Properties

Helium

Molecular Weight = 4.0026

Specific Heat at Constant Pressure = 1.24036 BTU/LB-R

Temperature (F)	Viscosity (LB/FT-HR)	Conductivity (BTU/HR-FT-F)	Sound Velocity (FT/SEC)
40.00000	4.5339250E-02	8.4353958E-02	3.2161071E+03
70.00000	4.7348801E-02	8.8092741E-02	3.3112430E+03
100.00000	4.9301672E-02	9.1726070E-02	3.4037209E+03
130.00000	5.1202696E-02	9.5262937E-02	3.4937318E+03
160.00000	5.3056299E-02	9.8711577E-02	3.5815203E+03
190.00000	5.4866529E-02	1.0207952E-01	3.6671887E+03
220.00000	5.6637084E-02	1.0537365E-01	3.7509011E+03
250.00000	5.8371342E-02	1.0860025E-01	3.8327355E+03
280.00000	6.0072394E-02	1.1176507E-01	3.9129567E+03
310.00000	6.1743066E-02	1.1487336E-01	3.9915180E+03
340.00000	6.3361257E-02	1.1835159E-01	4.0685526E+03
370.00000	6.5192576E-02	1.2129120E-01	4.1441751E+03
400.00000	6.6752529E-02	1.2419350E-01	4.2184325E+03
430.00000	6.8293346E-02	1.2706020E-01	4.2914052E+03
460.00000	6.9813863E-02	1.2989286E-01	4.3631376E+03
490.00000	7.1320879E-02	1.3269294E-01	4.4337490E+03
520.00000	7.2809100E-02	1.3546179E-01	4.5032339E+03
550.00000	7.4281207E-02	1.3820065E-01	4.5716629E+03
580.00000	7.5737823E-02	1.4091070E-01	4.6390826E+03
610.00000	7.7179543E-02	1.4359302E-01	4.7055364E+03
640.00000	7.8606903E-02	1.4624864E-01	4.7710647E+03
670.00000	8.0020435E-02	1.4887852E-01	4.8357051E+03
700.00000	8.1420607E-02	1.5148355E-01	4.8994928E+03
730.00000	8.2807879E-02	1.5406458E-01	4.9624606E+03
760.00000	8.4182578E-02	1.5662240E-01	5.0246394E+03
790.00000	8.5545409E-02	1.5915777E-01	5.0860581E+03
820.00000	8.6894453E-02	1.6167140E-01	5.1467439E+03
850.00000	8.8236173E-02	1.6416395E-01	5.2067224E+03
880.00000	8.9564910E-02	1.6663608E-01	5.2660179E+03
910.00000	9.0882989E-02	1.6908837E-01	5.3246530E+03
940.00000	9.2190718E-02	1.7152141E-01	5.3826495E+03
970.00000	9.3488391E-02	1.7393574E-01	5.4400277E+03
1000.00000	9.4776287E-02	1.7633188E-01	5.4968070E+03
1030.00000	9.6054671E-02	1.7871032E-01	5.5530057E+03
1060.00000	9.7323797E-02	1.8107153E-01	5.6086414E+03
1090.00000	9.8583908E-02	1.8341538E-01	5.6637306E+03
1120.00000	9.9835234E-02	1.8574400E-01	5.7182390E+03
1150.00000	1.0107800E-01	1.8805625E-01	5.7723319E+03
1180.00000	1.0231241E-01	1.9035238E-01	5.8258734E+03
1210.00000	1.0353867E-01	1.9263435E-01	5.8789273E+03
1240.00000	1.0475693E-01	1.9490102E-01	5.9315068E+03
1270.00000	1.0596752E-01	1.9715323E-01	5.9836242E+03
1300.00000	1.0717704E-01	1.9939133E-01	6.0352215E+03

Helium cont.

Temperature (F)	Enthalpy (BTU/LB)
40.00000	6.1979399E+02
70.00000	6.5700470E+02
100.00000	6.9421541E+02
130.00000	7.3142612E+02
160.00000	7.6863683E+02
190.00000	8.0584754E+02
220.00000	8.4305825E+02
250.00000	8.8026896E+02
280.00000	9.1747967E+02
310.00000	9.5469038E+02
340.00000	9.9190109E+02
370.00000	1.0291118E+03
400.00000	1.0663225E+03
430.00000	1.1035332E+03
460.00000	1.1407439E+03
490.00000	1.1779546E+03
520.00000	1.2151654E+03
550.00000	1.2523761E+03
580.00000	1.2895868E+03
610.00000	1.3267975E+03
640.00000	1.3640082E+03
670.00000	1.4012189E+03
700.00000	1.4384296E+03
730.00000	1.4756403E+03
760.00000	1.5128510E+03
790.00000	1.5500617E+03
820.00000	1.5872725E+03
850.00000	1.6244832E+03
880.00000	1.6616939E+03
910.00000	1.6989046E+03
940.00000	1.7361153E+03
970.00000	1.7733260E+03
1000.00000	1.8105367E+03
1030.00000	1.8477474E+03
1060.00000	1.8849581E+03
1090.00000	1.9221689E+03
1120.00000	1.9593796E+03
1150.00000	1.9965903E+03
1180.00000	2.0338010E+03
1210.00000	2.0710117E+03
1240.00000	2.1082224E+03
1270.00000	2.1454331E+03
1300.00000	2.1826438E+03

# Helium-Argon

Molecular Weight = 15.30

Specific Heat at Constant Pressure = 0.32449 BTU/LB-R

Temperature (F)	Viscosity (LB/FT-HR)	Conductivity (BTU/HR-FT-F)	Sound Velocity (FT/SEC)
40.00000	5.2301378E-02	4.0625810E-02	1.6449620E+03
70.00000	5.4834472E-02	4.2473701E-02	1.6936218E+03
100.00000	5.7302310E-02	4.4276174E-02	1.7409220E+03
130.00000	5.9708821E-02	4.6036461E-02	1.7869707E+03
160.00000	6.2057765E-02	4.7757544E-02	1.8318622E+03
190.00000	6.4352726E-02	4.9442169E-02	1.8755795E+03
220.00000	6.6597095E-02	5.1082872E-02	1.9184964E+03
250.00000	6.8794071E-02	5.2711988E-02	1.9603783E+03
280.00000	7.0946667E-02	5.4301672E-02	2.0013840E+03
310.00000	7.3057709E-02	5.5863917E-02	2.0415362E+03
340.00000	7.5119226E-02	5.7479805E-02	2.0809727E+03
370.00000	7.7215247E-02	5.8979570E-02	2.1196467E+03
400.00000	7.9207939E-02	6.0458070E-02	2.1576276E+03
430.00000	8.1169245E-02	6.1916424E-02	2.1949314E+03
460.00000	8.3100948E-02	6.3355610E-02	2.2316510E+03
490.00000	8.5004721E-02	6.4776608E-02	2.2677568E+03
520.00000	8.6886213E-02	6.6180270E-02	2.3032967E+03
550.00000	8.8734662E-02	6.7567427E-02	2.3382965E+03
580.00000	9.0719862E-02	6.9036491E-02	2.3727301E+03
610.00000	9.2501848E-02	7.0372762E-02	2.4067396E+03
640.00000	9.4263621E-02	7.1695393E-02	2.4402858E+03
670.00000	9.6006740E-02	7.3005294E-02	2.4733478E+03
700.00000	9.7731343E-02	7.4302920E-02	2.5059737E+03
730.00000	9.9438497E-02	7.5588637E-02	2.5381302E+03
760.00000	1.0112277E-01	7.6863031E-02	2.5699332E+03
790.00000	1.0280286E-01	7.8126300E-02	2.6013374E+03
820.00000	1.0446140E-01	7.9374864E-02	2.6324367E+03
850.00000	1.0610497E-01	8.0621064E-02	2.6631143E+03
880.00000	1.0773613E-01	8.1853224E-02	2.6934425E+03
910.00000	1.0934943E-01	8.3075648E-02	2.7234330E+03
940.00000	1.1103629E-01	8.4303934E-02	2.7530968E+03
970.00000	1.1268272E-01	8.5506316E-02	2.7824444E+03
1000.00000	1.1422746E-01	8.6699873E-02	2.8114836E+03
1030.00000	1.1578082E-01	8.7884858E-02	2.8402299E+03
1060.00000	1.1732311E-01	8.9051480E-02	2.8686863E+03
1090.00000	1.1885461E-01	9.0229963E-02	2.8968531E+03
1120.00000	1.2037559E-01	9.1350511E-02	2.9247584E+03
1150.00000	1.2188632E-01	9.2543323E-02	2.9524100E+03
1180.00000	1.2333700E-01	9.3688548E-02	2.9797953E+03
1210.00000	1.2487803E-01	9.4826487E-02	3.0069311E+03
1240.00000	1.2635947E-01	9.5957105E-02	3.0338242E+03
1270.00000	1.2783161E-01	9.7080576E-02	3.0604310E+03
1300.00000	1.2929465E-01	9.8197693E-02	3.0869076E+03



Helium-Argon, M = 15.30 cont.

Temperature (F)	Enthalpy (BTU/LB)
40.00000	1.6214297E+02
70.00000	1.7187758E+02
100.00000	1.8161220E+02
130.00000	1.9134681E+02
160.00000	2.0108142E+02
190.00000	2.1081604E+02
220.00000	2.2055065E+02
250.00000	2.3028527E+02
280.00000	2.4001988E+02
310.00000	2.4975449E+02
340.00000	2.5948911E+02
370.00000	2.6922372E+02
400.00000	2.7895833E+02
430.00000	2.8869295E+02
460.00000	2.9842756E+02
490.00000	3.0816217E+02
520.00000	3.1789679E+02
550.00000	3.2763140E+02
580.00000	3.3736602E+02
610.00000	3.4710063E+02
640.00000	3.5683524E+02
670.00000	3.6656986E+02
700.00000	3.7630447E+02
730.00000	3.8603908E+02
760.00000	3.9577370E+02
790.00000	4.0550831E+02
820.00000	4.1524292E+02
850.00000	4.2497754E+02
880.00000	4.3471215E+02
910.00000	4.4444677E+02
940.00000	4.5418138E+02
970.00000	4.6391599E+02
1000.00000	4.7365061E+02
1030.00000	4.8338522E+02
1060.00000	4.9311983E+02
1090.00000	5.0285445E+02
1120.00000	5.1258906E+02
1150.00000	5.2232367E+02
1180.00000	5.3205829E+02
1210.00000	5.4179290E+02
1240.00000	5.5152752E+02
1270.00000	5.6126213E+02
1300.00000	5.7099674E+02

# Helium-Argon

Molecular Weight = 15.83

Specific Heat at Constant Pressure = 0.31362 BTU/LB-R

Temperature (F)	Viscosity (LB/FT-HR)	Conductivity (BTU/HR-FT-F)	Sound Velocity (FT/SEC)
40.00000	5.2384618E-02	3.9396159E-02	1.6171303E+03
70.00000	5.4928517E-02	4.1190434E-02	1.6650286E+03
100.00000	5.7407116E-02	4.2940783E-02	1.7115303E+03
130.00000	5.9824291E-02	4.4650306E-02	1.7568015E+03
160.00000	6.2183763E-02	4.6321867E-02	1.8009351E+03
190.00000	6.4489079E-02	4.7958105E-02	1.8440127E+03
220.00000	6.6743604E-02	4.9561496E-02	1.8861067E+03
250.00000	6.8950516E-02	5.1134167E-02	1.9272815E+03
280.00000	7.1112809E-02	5.2678312E-02	1.9675349E+03
310.00000	7.3233298E-02	5.4195807E-02	2.0070987E+03
340.00000	7.5337014E-02	5.5761774E-02	2.0458399E+03
370.00000	7.7405684E-02	5.7219141E-02	2.0838609E+03
400.00000	7.9407606E-02	5.8655777E-02	2.1212006E+03
430.00000	8.1377829E-02	6.0072747E-02	2.1579943E+03
460.00000	8.3318152E-02	6.1471042E-02	2.1939743E+03
490.00000	8.5230263E-02	6.2851597E-02	2.2294706E+03
520.00000	8.7115747E-02	6.4215242E-02	2.2644104E+03
550.00000	8.8976092E-02	6.5562812E-02	2.2988193E+03
580.00000	9.0964336E-02	6.6942407E-02	2.3327207E+03
610.00000	9.2757737E-02	6.8289597E-02	2.3661364E+03
640.00000	9.4527012E-02	6.9573938E-02	2.3990867E+03
670.00000	9.6277033E-02	7.0845900E-02	2.4315706E+03
700.00000	9.8000596E-02	7.2105926E-02	2.4636656E+03
730.00000	9.9722451E-02	7.3354433E-02	2.4953284E+03
760.00000	1.0141931E-01	7.4591815E-02	2.5265345E+03
790.00000	1.0309984E-01	7.5818442E-02	2.5574783E+03
820.00000	1.0478467E-01	7.7034655E-02	2.5879938E+03
850.00000	1.0641441E-01	7.8240817E-02	2.6181532E+03
880.00000	1.0804964E-01	7.9437212E-02	2.6479694E+03
910.00000	1.0967089E-01	8.0624150E-02	2.6774236E+03
940.00000	1.1142182E-01	8.1818356E-02	2.7066166E+03
970.00000	1.1300326E-01	8.2985697E-02	2.7354687E+03
1000.00000	1.1457297E-01	8.4144452E-02	2.7640196E+03
1030.00000	1.1613127E-01	8.5294890E-02	2.7922787E+03
1060.00000	1.1767846E-01	8.6437221E-02	2.8202546E+03
1090.00000	1.1921483E-01	8.7571654E-02	2.8479557E+03
1120.00000	1.2074066E-01	8.8698389E-02	2.8753399E+03
1150.00000	1.2225620E-01	8.9817619E-02	2.9025648E+03
1180.00000	1.2376172E-01	9.0929526E-02	2.9294877E+03
1210.00000	1.2525745E-01	9.2034297E-02	2.9561654E+03
1240.00000	1.2674362E-01	9.3132070E-02	2.9826045E+03
1270.00000	1.2822046E-01	9.4223037E-02	3.0088113E+03
1300.00000	1.2968818E-01	9.5307343E-02	3.0347917E+03

Helium-Argon, M = 15.83 cont.

Temperature (F)	Enthalpy (BTU/LB)
40.00000	1.5671430E+02
70.00000	1.6612300E+02
100.00000	1.7553169E+02
130.00000	1.8494038E+02
160.00000	1.9434907E+02
190.00000	2.0375776E+02
220.00000	2.1316645E+02
250.00000	2.2257515E+02
280.00000	2.3198384E+02
310.00000	2.4139253E+02
340.00000	2.5080122E+02
370.00000	2.6020991E+02
400.00000	2.6961860E+02
430.00000	2.7902730E+02
460.00000	2.8843599E+02
490.00000	2.9784468E+02
520.00000	3.0725337E+02
550.00000	3.1666206E+02
580.00000	3.2607075E+02
610.00000	3.3547944E+02
640.00000	3.4488814E+02
670.00000	3.5429683E+02
700.00000	3.6370552E+02
730.00000	3.7311421E+02
760.00000	3.8252290E+02
790.00000	3.9193159E+02
820.00000	4.0134028E+02
850.00000	4.1074897E+02
880.00000	4.2015766E+02
910.00000	4.2956635E+02
940.00000	4.3897504E+02
970.00000	4.4838373E+02
1000.00000	4.5779242E+02
1030.00000	4.6720111E+02
1060.00000	4.7660980E+02
1090.00000	4.8501849E+02
1120.00000	4.9442718E+02
1150.00000	5.0383587E+02
1180.00000	5.1324456E+02
1210.00000	5.2265325E+02
1240.00000	5.3206194E+02
1270.00000	5.4147063E+02
1300.00000	5.5087932E+02

# Helium-Argon

Molecular Weight = 27.53

Specific Heat at Constant Pressure = 0.18034 BTU/LB-R

Temperature (F)	Viscosity (LB/FT-HR)	Conductivity (BTU/HR-FT-F)	Sound Velocity (FT/SEC)
40.00000	5.2563842E-02	2.0434522E-02	1.2263050E+03
70.00000	5.5227557E-02	2.1402132E-02	1.2625304E+03
100.00000	5.7827260E-02	2.2347336E-02	1.2978423E+03
130.00000	6.0365859E-02	2.3271434E-02	1.3321712E+03
160.00000	6.2846258E-02	2.4175647E-02	1.3656374E+03
190.00000	6.5271322E-02	2.5061130E-02	1.3983029E+03
220.00000	6.7643847E-02	2.5928965E-02	1.4302225E+03
250.00000	6.9966537E-02	2.6780169E-02	1.4614451E+03
280.00000	7.2241997E-02	2.7615636E-02	1.4920145E+03
310.00000	7.4472722E-02	2.8436438E-02	1.5219700E+03
340.00000	7.6670221E-02	2.9253647E-02	1.5513471E+03
370.00000	7.8817021E-02	3.0045581E-02	1.5801783E+03
400.00000	8.0926015E-02	3.0825225E-02	1.6084927E+03
430.00000	8.2999207E-02	3.1593220E-02	1.6363173E+03
460.00000	8.5038497E-02	3.2350167E-02	1.6636765E+03
490.00000	8.7045687E-02	3.3096632E-02	1.6905331E+03
520.00000	8.9022441E-02	3.3833145E-02	1.7170378E+03
550.00000	9.0970492E-02	3.4560205E-02	1.7431738E+03
580.00000	9.2984234E-02	3.5334411E-02	1.7688370E+03
610.00000	9.4864927E-02	3.6032088E-02	1.7942259E+03
640.00000	9.6721845E-02	3.6722244E-02	1.8192119E+03
670.00000	9.8556091E-02	3.7405190E-02	1.8438544E+03
700.00000	1.0036871E-01	3.8081200E-02	1.8681317E+03
730.00000	1.0216070E-01	3.8750575E-02	1.8921914E+03
760.00000	1.0393329E-01	3.9413547E-02	1.9159002E+03
790.00000	1.0568648E-01	4.0070366E-02	1.9393192E+03
820.00000	1.0742201E-01	4.0721264E-02	1.9624588E+03
850.00000	1.0914040E-01	4.1366460E-02	1.9853287E+03
880.00000	1.1084239E-01	4.2006162E-02	2.0079381E+03
910.00000	1.1252671E-01	4.2640566E-02	2.0302957E+03
940.00000	1.1450619E-01	4.3315536E-02	2.0524098E+03
970.00000	1.1613465E-01	4.3935632E-02	2.0742382E+03
1000.00000	1.1775107E-01	4.4551214E-02	2.0959382E+03
1030.00000	1.1935579E-01	4.5162402E-02	2.1173569E+03
1060.00000	1.2094912E-01	4.5769313E-02	2.1385308E+03
1090.00000	1.2253134E-01	4.6372057E-02	2.1595364E+03
1120.00000	1.2410274E-01	4.6970738E-02	2.1803396E+03
1150.00000	1.2566359E-01	4.7565458E-02	2.2009961E+03
1180.00000	1.2721415E-01	4.8156313E-02	2.2214116E+03
1210.00000	1.2875466E-01	4.8743396E-02	2.2415411E+03
1240.00000	1.3028537E-01	4.9326736E-02	2.2616897E+03
1270.00000	1.3180649E-01	4.9906596E-02	2.2815021E+03
1300.00000	1.3331826E-01	5.0482880E-02	2.3012529E+03

Helium-Argon, M = 27.53 cont.

Temperature (F)	Enthalpy (BTU/LB)
40.000000	9.0112148E+01
70.000000	9.5522231E+01
100.000000	1.0093231E+02
130.000000	1.0634240E+02
160.000000	1.1175248E+02
190.000000	1.1716256E+02
220.000000	1.2257265E+02
250.000000	1.2798273E+02
280.000000	1.3339281E+02
310.000000	1.3880290E+02
340.000000	1.4421298E+02
370.000000	1.4962306E+02
400.000000	1.5503315E+02
430.000000	1.6044323E+02
460.000000	1.6585331E+02
490.000000	1.7126340E+02
520.000000	1.7667348E+02
550.000000	1.8208356E+02
580.000000	1.8749364E+02
610.000000	1.9290373E+02
640.000000	1.9831381E+02
670.000000	2.0372389E+02
700.000000	2.0913398E+02
730.000000	2.1454406E+02
760.000000	2.1995414E+02
790.000000	2.2536423E+02
820.000000	2.3077431E+02
850.000000	2.3618439E+02
880.000000	2.4159448E+02
910.000000	2.4700456E+02
940.000000	2.5241464E+02
970.000000	2.5782473E+02
1000.000000	2.6323481E+02
1030.000000	2.6864489E+02
1060.000000	2.7405497E+02
1090.000000	2.7946506E+02
1120.000000	2.8487514E+02
1150.000000	2.9028522E+02
1180.000000	2.9569531E+02
1210.000000	3.0110539E+02
1240.000000	3.0651547E+02
1270.000000	3.1192556E+02
1300.000000	3.1733564E+02

## Helium-Argon

Molecular Weight = 29.70

Specific Heat at Constant Pressure = 0.16716 BTU/LB-R

Temperature (F)	Viscosity (LB/FT-HR)	Conductivity (BTU/HR-FT-F)	Sound Velocity (FT/SEC)
40.00000	5.2418661E-02	1.5071935E-02	1.1806560E+03
70.00000	5.5089766E-02	1.8936920E-02	1.2155311E+03
100.00000	5.7697317E-02	1.9781952E-02	1.2495304E+03
130.00000	6.0244079E-02	2.0608217E-02	1.2825314E+03
160.00000	6.2732833E-02	2.1416666E-02	1.3148018E+03
190.00000	6.5166339E-02	2.2208326E-02	1.3462513E+03
220.00000	6.7547299E-02	2.2984125E-02	1.3769927E+03
250.00000	6.9878341E-02	2.3744946E-02	1.4070430E+03
280.00000	7.2162005E-02	2.4491622E-02	1.4364745E+03
310.00000	7.4400728E-02	2.5224934E-02	1.4653149E+03
340.00000	7.6602596E-02	2.5952050E-02	1.4935385E+03
370.00000	7.8757404E-02	2.6659758E-02	1.5213564E+03
400.00000	8.0874035E-02	2.7356255E-02	1.5486168E+03
430.00000	8.2954484E-02	2.8042132E-02	1.5754056E+03
460.00000	8.5000641E-02	2.8717435E-02	1.6017465E+03
490.00000	8.7014303E-02	2.9384180E-02	1.6275511E+03
520.00000	8.8997171E-02	3.0041350E-02	1.6531695E+03
550.00000	9.0950857E-02	3.0689903E-02	1.6782302E+03
580.00000	9.2853308E-02	3.1376522E-02	1.7030405E+03
610.00000	9.4841908E-02	3.1999398E-02	1.7274352E+03
640.00000	9.6705728E-02	3.2615263E-02	1.7514321E+03
670.00000	9.8546407E-02	3.3224512E-02	1.7752220E+03
700.00000	1.0036503E-01	3.3827417E-02	1.7986349E+03
730.00000	1.0216262E-01	3.4424234E-02	1.8217549E+03
760.00000	1.0394016E-01	3.5015209E-02	1.8445812E+03
790.00000	1.0569856E-01	3.5600570E-02	1.8671254E+03
820.00000	1.0743871E-01	3.6180539E-02	1.8894266E+03
850.00000	1.0916143E-01	3.6755321E-02	1.9114352E+03
880.00000	1.1086752E-01	3.7325114E-02	1.9331329E+03
910.00000	1.1255773E-01	3.7890104E-02	1.9547183E+03
940.00000	1.1426435E-01	3.8502097E-02	1.9760392E+03
970.00000	1.1619396E-01	3.9053187E-02	1.9970732E+03
1000.00000	1.1781154E-01	3.9600244E-02	2.0179173E+03
1030.00000	1.1941741E-01	4.0143436E-02	2.0385482E+03
1060.00000	1.2101187E-01	4.0682804E-02	2.0589725E+03
1090.00000	1.2259524E-01	4.1218466E-02	2.0791361E+03
1120.00000	1.2416778E-01	4.1750517E-02	2.0992249E+03
1150.00000	1.2572976E-01	4.2279046E-02	2.1190544E+03
1180.00000	1.2728145E-01	4.2804138E-02	2.1387199E+03
1210.00000	1.2882309E-01	4.3325877E-02	2.1581364E+03
1240.00000	1.3035492E-01	4.3844340E-02	2.1774987E+03
1270.00000	1.3187716E-01	4.4359603E-02	2.1966314E+03
1300.00000	1.3339004E-01	4.4871734E-02	2.2155388E+03

Helium-Argon, M = 29.70 cont.

Temperature (F)	Enthalpy (BTU/LB)
40.00000	8.3528196E+01
70.00000	8.8542997E+01
100.00000	9.3557798E+01
130.00000	9.8572599E+01
160.00000	1.0358740E+02
190.00000	1.0850220E+02
220.00000	1.1361700E+02
250.00000	1.1863140E+02
280.00000	1.2364660E+02
310.00000	1.2856141E+02
340.00000	1.3357621E+02
370.00000	1.3859101E+02
400.00000	1.4370581E+02
430.00000	1.4872051E+02
460.00000	1.5373541E+02
490.00000	1.5875021E+02
520.00000	1.6376501E+02
550.00000	1.6877981E+02
580.00000	1.7379461E+02
610.00000	1.7880941E+02
640.00000	1.8382422E+02
670.00000	1.8883902E+02
700.00000	1.9385382E+02
730.00000	1.9886862E+02
760.00000	2.0388342E+02
790.00000	2.0889822E+02
820.00000	2.1391302E+02
850.00000	2.1892782E+02
880.00000	2.2394262E+02
910.00000	2.2895742E+02
940.00000	2.3397222E+02
970.00000	2.3898702E+02
1000.00000	2.4400183E+02
1030.00000	2.4901663E+02
1060.00000	2.5403143E+02
1090.00000	2.5904623E+02
1120.00000	2.6406103E+02
1150.00000	2.6907583E+02
1180.00000	2.7409063E+02
1210.00000	2.7910543E+02
1240.00000	2.8412024E+02
1270.00000	2.8913504E+02
1300.00000	2.9414984E+02

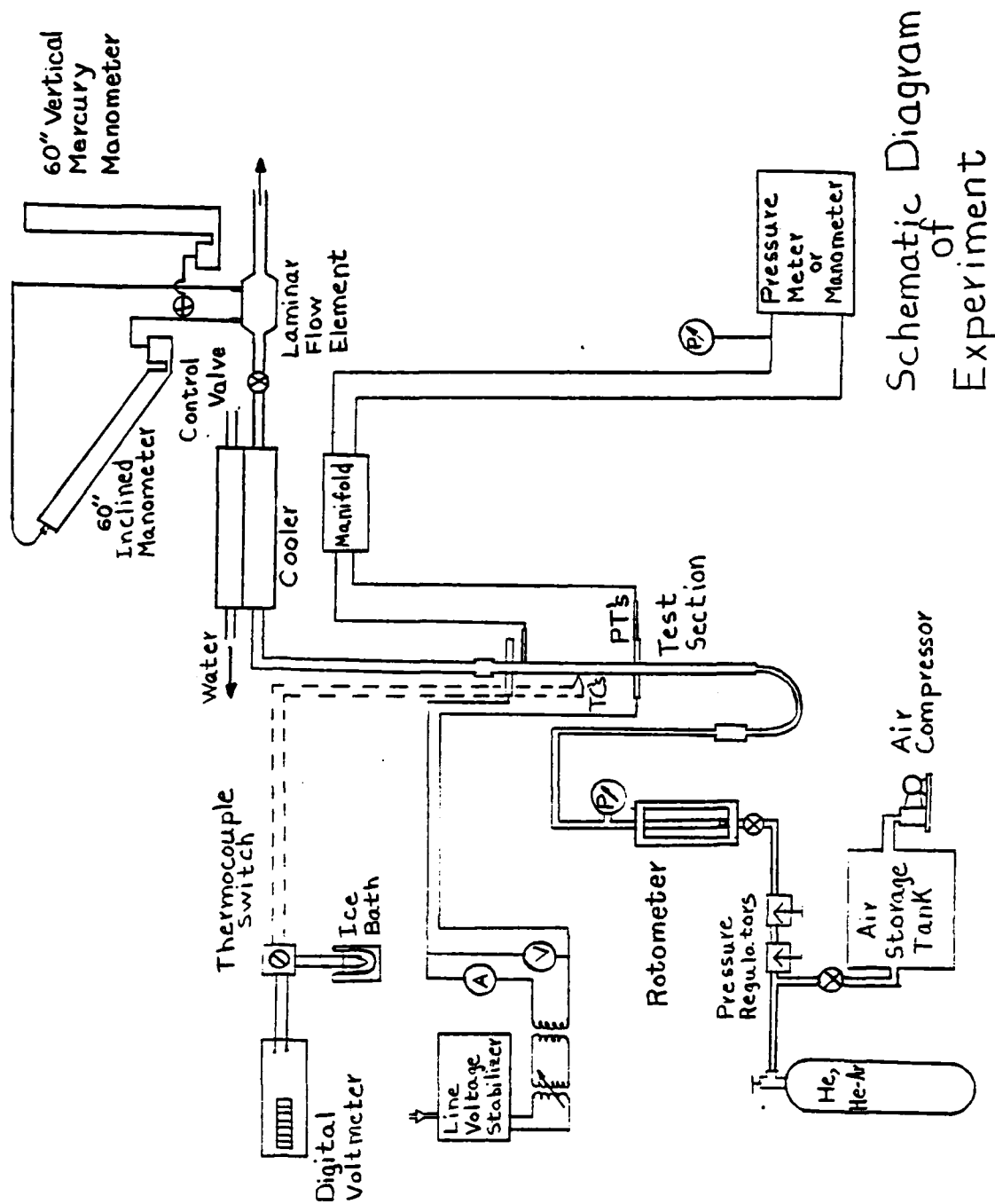
## APPENDIX B. EXPERIMENT

### Apparatus

A schematic diagram of the experiment is shown in Fig. B1. The helium and helium-argon mixtures were bought from manufacturers in high pressure bottles. The air was obtained from a large storage tank that was replenished by a compressor. Two regulators were used to reduce and stabilize the pressure. A Brooks rotometer was used to obtain a rough measurement of the flow rate. A Bourdon tube Heise gage measured the pressure just downstream of the rotometer. A small tank constructed to mix the gas, and instrumented with a thermocouple measured the inlet stagnation temperature. A sketch of the test section from the inlet to just below the outlet mixing tank, and displaying the location of thermocouples, pressure taps, electrodes, and voltage taps is shown in Fig. B2.

Power was measured using a Fluke differential voltmeter and Weston ammeter in the same manner as Perkins et al. [27]. Whenever possible the power supply described by Perkins et al. [27] was used. When it did not supply sufficient power an a.c. Lincoln welder (Model TM-500/500) was used. To determine a power factor when the welder was used, the power measured with a Weston watt meter was compared to that calculated from voltage (Fluke voltmeter)





Schematic Diagram  
of  
Experiment

Fig. B1.

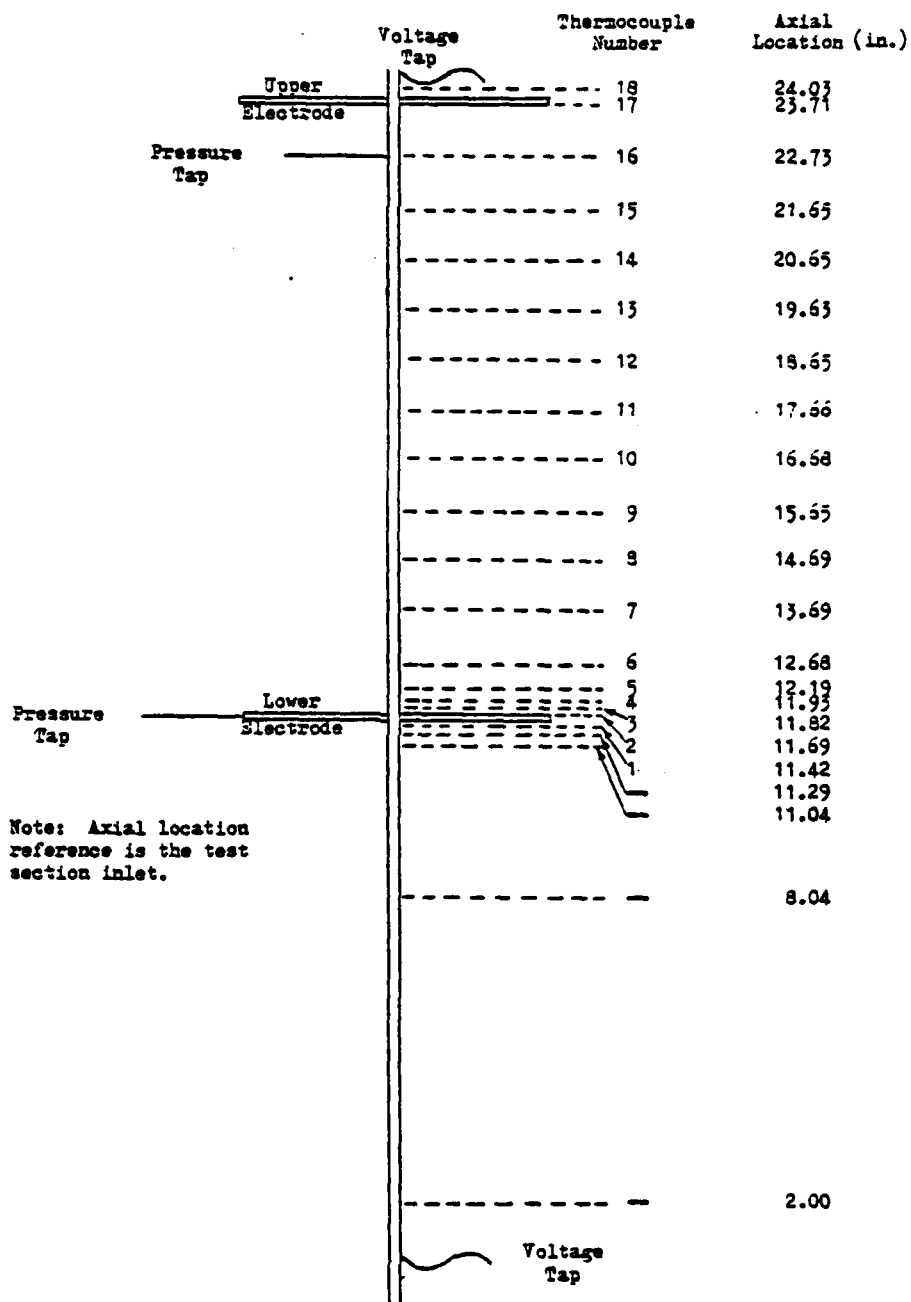


Fig. 32. Diagram of test section.

and current (Weston ammeter) measurements. A power factor of 1.0 was used since the two measurements agreed within 3.3 percent.

Thermocouple output was measured with a Hewlett Packard digital voltmeter. An ice bath was used as a reference for all of the thermocouples. Thermocouples were selected for measurement using a manual switch. The numbered thermocouples on Fig. B2 were used in the computer program that reduced the experimental data for the heated runs. This computer program is described by a number of people [30,31,32,44]. The unnumbered thermocouples were used to determine the amount of preheating of the gas before it entered the heated section.

Pressure drop in the test section was measured with Meriam 60 inch vertical water or mercury manometers. Inlet static pressure was measured with a Bourdon tube Heise gage.

After the gas passed through the test section, it was cooled by a chilled water counterflow heat exchanger. The valve used to control the flow rate was located just downstream of the heat exchanger. The heat exchanger was necessary in order that a Meriam laminar flow element could be used. The laminar flow element was used to obtain an accurate measurement of the flow rate. A Meriam 60 inch inclined water manometer with a 10 inch range was used to measure pressure drop across the laminar flow

element. The temperature of the gas in the flow element was measured with a thermocouple, and the pressure was measured with a Meriam 60 inch vertical mercury manometer. The accuracies of the instruments used in this investigation are listed in appendix C (Table C1).

#### Procedure

Before any experimental runs with gas flow were performed, the test section was heated without flow in order that the heat lost to the environment and the resistance of the test section could be determined. These items are discussed in detail in the following two sections.

The system was purged and all of the instruments zeroed before each set of experimental runs. The purging was done by pressurizing the system to approximately 100 psig with the gas to be used. The system was then allowed to blow down to approximately 10 psig. This sequence was performed four times.

The desired inlet Reynolds number was established by adjusting the pressure level and mass flow rate. Before power was supplied to the test section, measurements were taken so that calculation of the adiabatic friction coefficient was possible. The measured adiabatic friction coefficients were compared to the Drew, Koo, and McAdams correlation [34] (equation 11), and agreement ensured that the pressure measurements, mass flow rate measurements, and mixture molecular weights were correct.

The test section was then heated to the desired level. Since a small period of time elapsed while the thermocouples were manually recorded, pressure drop, pressure level, voltage, current, and mass flow rate measurements were taken before and after the thermocouple measurements. The average of the two measurements was used for data reduction. The inlet Reynolds number was maintained approximately constant while the test section wall temperature was varied by varying the power input. Measurements were taken for a number of different power inputs.

#### Heat Loss Calibration

In order to calculate the heat transfer coefficient, the heat addition to the gas,  $q'_{\text{gas}}$ , must be determined. If an energy balance for a small section of the tube is performed, the result is:

$$q'_{\text{gas}} = q'_{\text{gen}} - (q'_{\text{cond}} + q'_{\text{loss}}). \quad (\text{B1})$$

The heat generated in the small section of the tube,  $q'_{\text{gen}}$ , is:

$$q'_{\text{gen}} = I^2 R'. \quad (\text{B2})$$

The current was measured, and the calculation of the resistance per unit length is discussed in the next section. The axial heat loss due to conduction is:

$$q'_{\text{cond}} = -K A_{\text{cs}} d^2 T_w / dx^2. \quad (\text{B3})$$

The second derivative was determined using a numerical parabolic fit described by McEligot [31]. The variation of thermal conductivity with temperature for Hastelloy-X

was determined from data supplied by the manufacturer [46].

$$K = [5.1 + (0.00622)(T)](\text{Btu/hr-ft-F}) \quad (\text{B4})$$

(T in degrees Fahrenheit)

To determine the heat loss,  $q'_{\text{loss}}$ , the test section was heated at different levels without gas flow. A program described by Coon [32] was used to calculate the heat loss at each thermocouple. The heat loss was determined as a function of the tube wall and environment temperature difference. The environment temperature was measured with a thermocouple a few inches away from the test section. Figures B3, B4, B5, and B6 show the results for each thermocouple (thermocouple 4 is not included). Except for thermocouple three and four, the data for each thermocouple was fitted with an equation of the form:

$$q'_{\text{loss}} = C_1(T_w - T_\infty) + C_2(T_w - T_\infty)^2 + C_3(T_w - T_\infty)^3 \quad (\text{Btu/hr-ft}) \quad (\text{B5})$$

( $T_w - T_\infty$  in degrees Fahrenheit)

The numerical values of  $C_1$ ,  $C_2$ , and  $C_3$  are listed below.

Thermocouple	$C_1$	$C_2$	$C_3$
2	2.43E+00	9.43E-03	-2.53E-05
5	1.22E-01	1.84E-04	-1.64E-08
6	9.83E-02	2.30E-04	-6.57E-08
7	8.84E-02	1.66E-04	-3.79E-09
8	8.30E-02	1.35E-04	3.07E-08
9	8.16E-02	1.03E-04	6.04E-08
10	7.89E-02	1.12E-04	4.96E-08
11	7.70E-02	8.82E-05	7.13E-08
12	7.40E-02	1.03E-04	5.50E-08
13	7.54E-02	8.08E-05	7.59E-08
14	7.31E-02	9.77E-05	5.73E-08
15	8.09E-02	8.07E-05	7.46E-08
16	1.18E-01	1.59E-04	5.59E-08
17	2.76E-01	1.14E-03	1.19E-06

The data for thermocouple three was fitted with a straight line determined using the method of least squares.

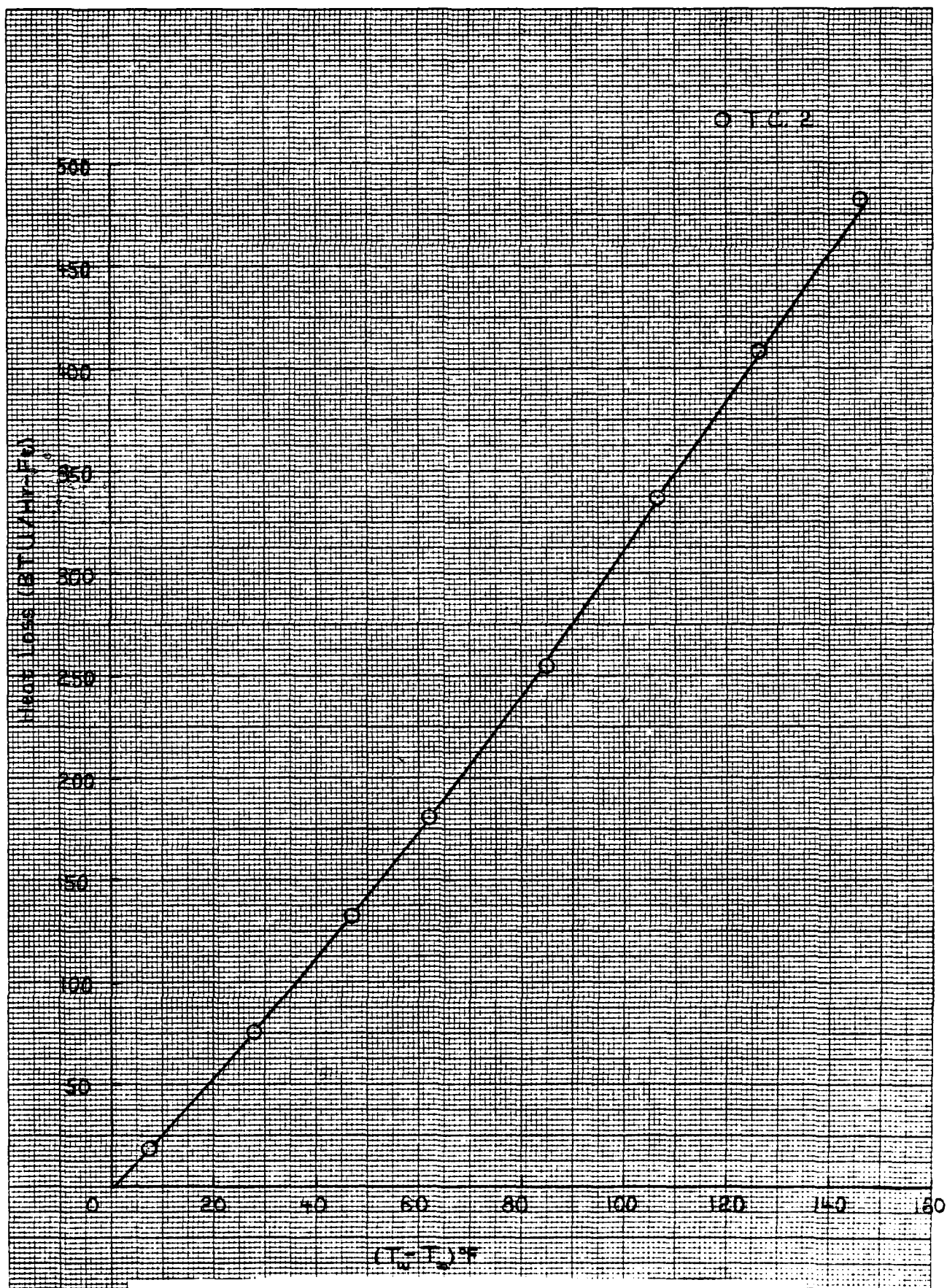


Fig. B3. Heat loss calibration for thermocouple 2.

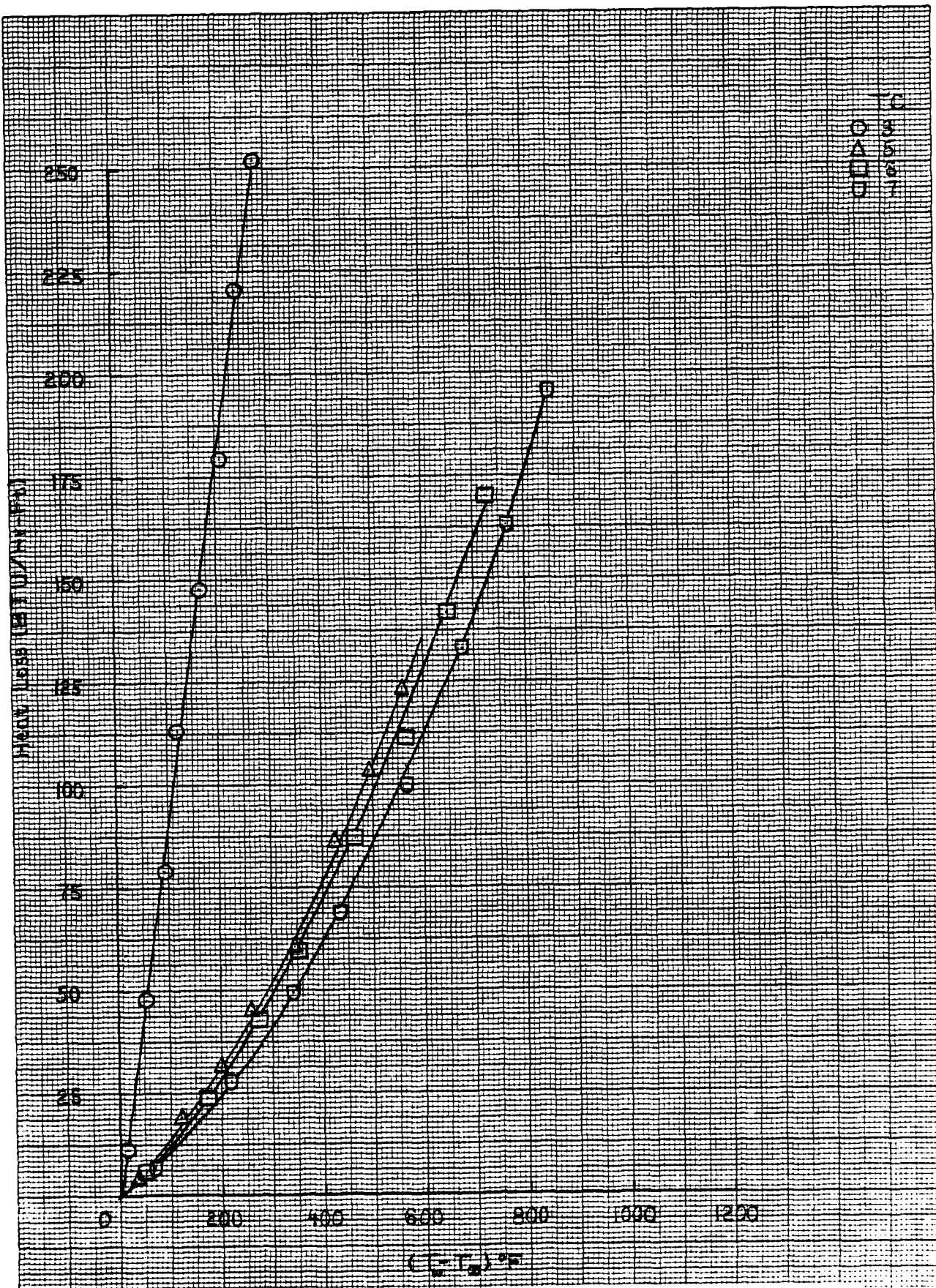


Fig. B4. Heat loss calibration for thermocouples 3, 5, 6, and 7.



K&E 10 X 10 TO THE CENTIMETER 46 1513  
MADE IN U.S.A.  
KEUFFEL & ESSER CO.

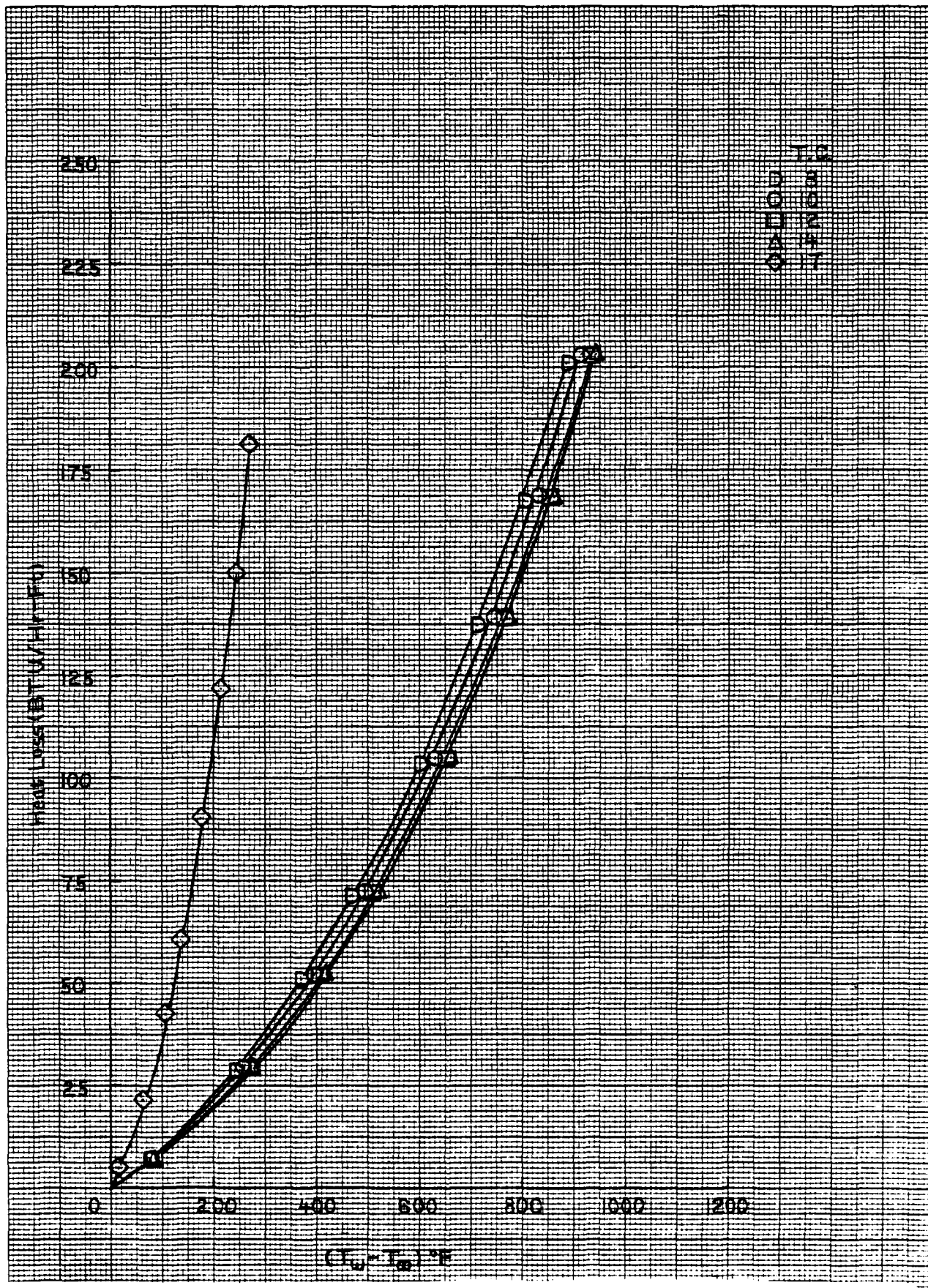


Fig. B5. Heat loss calibration for thermocouples 8, 10, 12, 14, and 17.

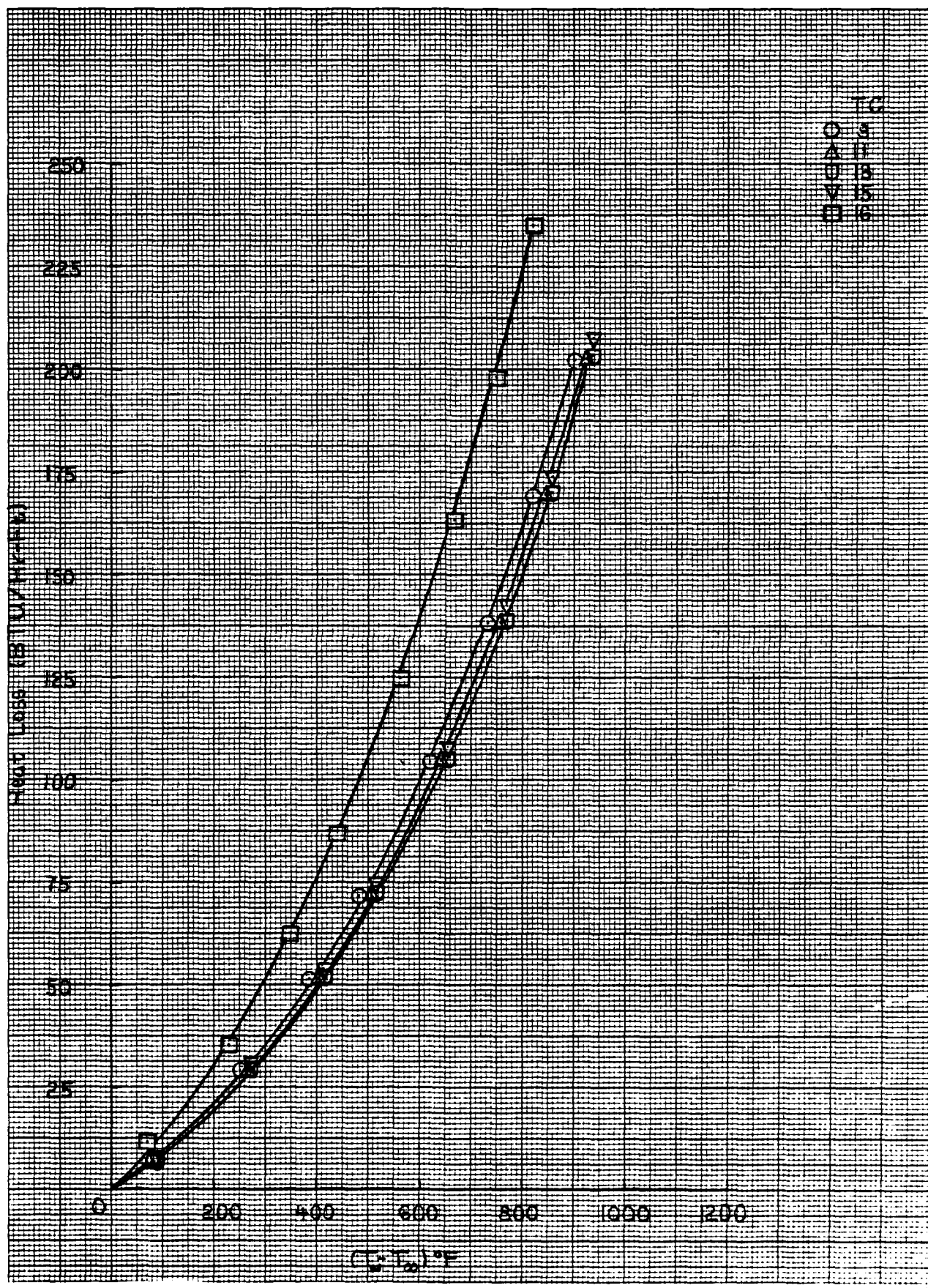


Fig. B6. Heat loss calibration for thermocouples 9, 11, 13, 15, and 16.

$$q'_{\text{loss}}(\text{T.C. 3}) = 0.91(T_w - T_\infty) - 2.20(\text{Btu/hr-ft}) \quad (\text{B6})$$

( $T_w - T_\infty$  in degrees Fahrenheit)

The data for thermocouple four was scattered and a representative curve could not be fitted. For this reason the heat loss at this thermocouple was neglected. This introduced only a small error since the heat loss for thermocouple four, even at the highest heating rates, was less than five percent of the heat added to the gas. The fitted curves are also shown on Figures B3, B4, B5, and B6.

#### Measurement of Test Section Resistance

The variation of resistance with temperature was measured by heating the test section without gas flow in the same manner as was done for the heat loss calibration. Using the thermocouple wires as voltage taps, a measurement of the voltage drop between thermocouple 14 and the lowermost thermocouple on the tube was taken. Another measurement of the voltage drop between thermocouple 12 and the lowermost thermocouple was taken. The difference between these two measurements gave the voltage drop between thermocouples 12 and 14. The section of the tube between thermocouples 12 and 14 was used since the wall temperature for this length was approximately constant.

For a particular power setting the voltage drop discussed in the previous paragraph, the current, and the average of the temperatures at thermocouples 12, 13, and

14 were recorded. Using these measurements the resistance per unit length was determined as a function of temperature. The results are shown on Fig. B7. Also shown on Fig. B7 is the line that was used to approximate the variation of resistance with temperature.

$$R' = [3.98 \times 10^{-4}(T) + 4.745] \text{ (m}\Omega/\text{in)} \quad (B7)$$

(T in degrees Fahrenheit)

#### Meriam Laminar Flow Element Calibration

The laminar flow element was calibrated using a Parkinson-Cowan Type D1 positive displacement flow meter as a standard. It is specified to have 1/2 percent accuracy at ambient conditions and was calibrated by Tucson Gas and Electric before being used. Meriam [45] suggests the following equation for the laminar flow element:

$$\Delta P = A'Q\mu L/D^4 + B'\rho Q^2/D^4. \quad (B8)$$

A' and B' are the constants to be determined by calibration. Since the length, L, and the hydraulic diameter, D, of the laminar flow element passages remain constant, they can be incorporated into new calibration constants, A and B.

$$A = A'L/D^4 \quad B = B'/D^4$$

Equation B8 now becomes:

$$\Delta P = A Q \mu + B \rho Q^2. \quad (B9)$$

If this equation is solved for Q the result is:

$$Q = [-A\mu/B + \sqrt{(A\mu/B)^2 + 4\rho\Delta P/B}]/2\rho. \quad (B10)$$

If both sides of this equation are multiplied by the density,  $\rho$ , the result is:

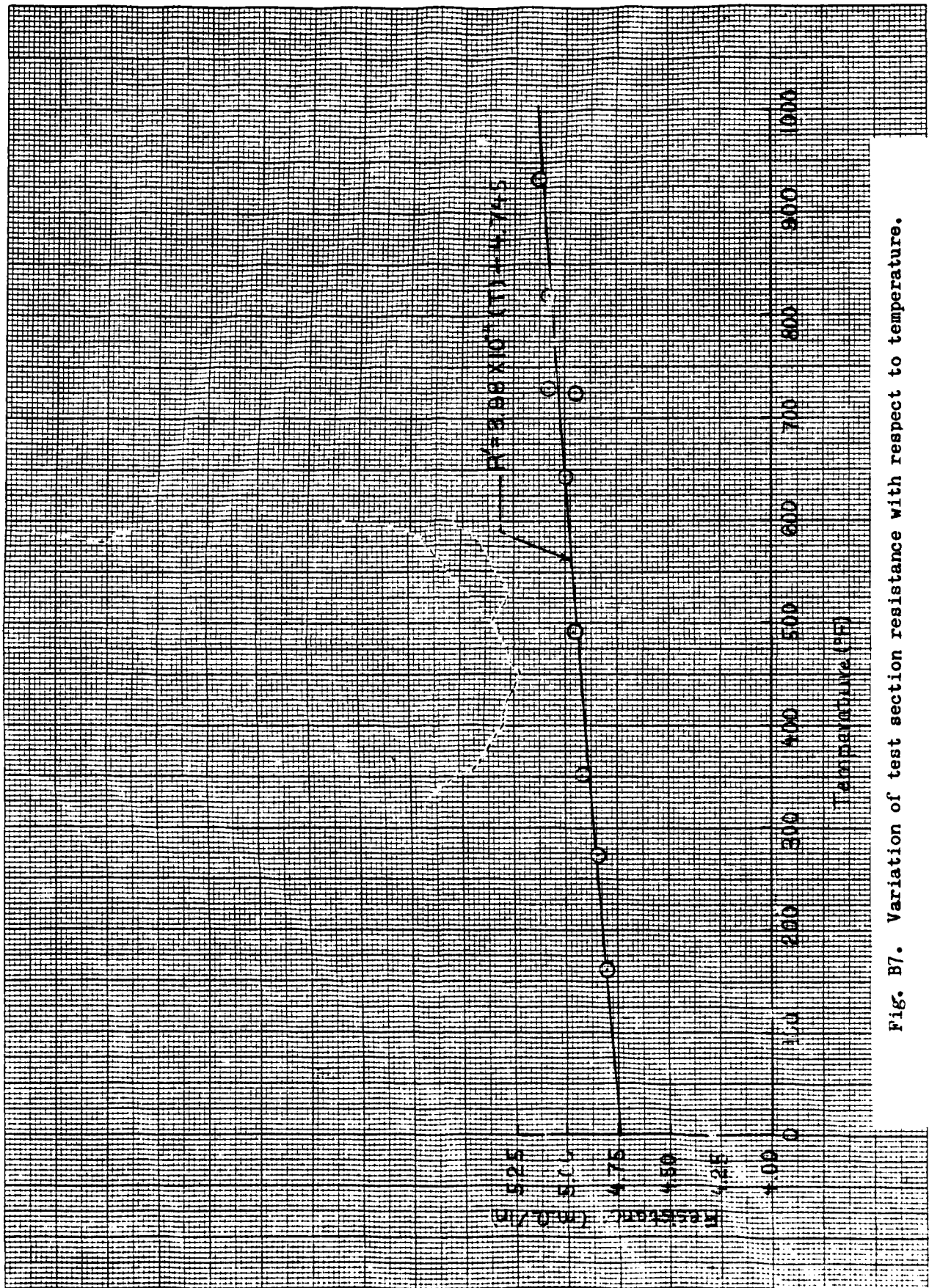


Fig. B7. Variation of test section resistance with respect to temperature.



$$\dot{m} = \rho Q = 1/2[-A\mu/B + \sqrt{(A\mu/B)^2 + 4\rho\Delta P/B}]. \quad (B11)$$

Mass flow rate measurements were taken simultaneously with the positive displacement flow meter and the laminar flow element. Both air and helium were used. These gases bound the range of helium-argon mixture molecular weights that were used. From these measurements, A and B were determined so that the maximum difference between the positive displacement flow meter measurements and the laminar flow element measurements was 1.5 percent. The numerical values of A and B were 1375 and 672, respectively, if the parameters in equation B11 have the following units.

m - lb/sec  
 $\mu$  - lb/hr-ft  
 $\rho$  - lb/ft<sup>3</sup>  
 $\Delta P$  - inches of water

## APPENDIX C Uncertainty Analysis

An analysis to determine the uncertainty of the results calculated from the measured experimental data was performed. The uncertainties of the directly measured quantities were determined from manufacturers' specifications and experience. Table C1 lists the uncertainties of the instruments used in this investigation. The error propagated to the calculated results from the uncertainties in the measured quantities was determined using a method described by Bottaccini [47]. The general equation used was

$$\begin{aligned} \sigma_Z^2 = & \left( \frac{\partial Z}{\partial Y_1} \right)^2 \sigma_{Y_1}^2 + \left( \frac{\partial Z}{\partial Y_2} \right)^2 \sigma_{Y_2}^2 + \dots \\ & + \left( \frac{\partial Z}{\partial a_1} \right)^2 \sigma_{a_1}^2 + \left( \frac{\partial Z}{\partial a_2} \right)^2 \sigma_{a_2}^2 + \dots \end{aligned} \quad (C1)$$

$\sigma_x$  is the variance or standard deviation of the xth quantity. Z is the calculated quantity, and  $Y_i$  and  $a_i$  are the measured values and system parameters used to calculate Z.

To illustrate the above technique, a simple example will be done. The power supplied to the tube can be determined using the relation (assuming a power factor of one)

$$P = E I. \quad (C2)$$

If equation C1 is applied, the error or variance in the power caused by uncertainties in the voltage and current measurements is

$$\sigma_P = \sqrt{(I)^2 \sigma_E^2 + (E)^2 \sigma_I^2} \quad (C3)$$

The result can be presented in the following form so that the percent of uncertainty can easily be determined.

$$\sigma_P/P = \sqrt{(\sigma_E/E)^2 + (\sigma_I/I)^2} \quad (C4)$$

TABLE C1  
Uncertainties of Measured Values

Measured quantity	Instrument	Uncertainty
Current	Weston 370 AC/DC ammeter	±0.25% of full scale
Voltage	Fluke 883AB differential voltmeter	±0.1% of input
Mass flow rate	Meriam 50MH10-1 laminar flow element	±1.5% of flow rate
Wall and inlet bulk temperature	Premium grade chromel-alumel thermocouples	±2°F, 3/8% of reading above 535°F
Thermocouple location Pressure tap location	Gaertner M911 Cathetometer	±0.1mm
Diameter	Manufacturers' specifications	±0.001 in.
Pressure	12 inch Heise gage	±0.15 psi
Pressure drop	60" Meriam 30EB25 vertical H <sub>2</sub> O manometer 60" Meriam 30EB25 vertical Hg manometer	±0.05 in-H <sub>2</sub> O ±0.05 in-Hg

Table C2 lists the percentage uncertainty in the measured bulk Nusselt numbers for two representative helium-argon runs. The dominant uncertainty in the bulk Nusselt number is the bulk stagnation temperature. For convenience no uncertainty was included for the gas properties. The values used were assumed to be precise.



TABLE C2  
Percentage Uncertainties in the Measured  
Bulk Nusselt Numbers of Helium-Argon

Run	126H	131H
Molecular weight	15.30	15.30
Re	56100	54700
$(T_w^1/T_b)_{MAX}$	1.17	1.77

x/D	Percentage Uncertainty	
1.17	13	10
2.07	8	6
4.14	6	4
8.13	5	3
24.52	4	3
40.79	4	3
56.88	4	3

APPENDIX D  
Helium-Argon Experimental Data

The headings and their definitions used in the listing of the adiabatic friction data are below.

<u>Heading</u>	<u>Definition</u>
Run	Experiment run number
Date	Date on which experimental run was made
Gas	Gas used in the experiment
Molec. wt.	Molecular weight
$T_i$	Inlet mixer temperature
$\dot{m}$	Gas flow rate
$Re_i$	Inlet Reynolds number
$P_1$	Static pressure at inlet pressure tap
$P_2$	Static pressure at outlet pressure tap
Static Mach <sub>1</sub>	Static mach number at inlet pressure tap
Static Mach <sub>2</sub>	Static mach number at outlet pressure tap
$f_{ad}$	Adiabatic friction factor

Table D-1 HELIUM-ARGON ADIABATIC FRICTION FACTOR DATA

Run	Date	Gas	Molec. Wt.	T <sub>i</sub> (°F)	m (lb/hr)	Re <sub>i</sub>	P <sub>1</sub> (psia)	P <sub>2</sub> (psia)	Static Mach <sub>1</sub>	Static Mach <sub>2</sub>	f <sub>ad</sub>
77A	8/27/75	He	4.003	71.5	3.8	9950	105.4	104.7	0.0521	0.0524	0.00796
81A	8/30/75	He	4.003	72.7	3.7	9660	102.0	101.3	0.0524	0.0527	0.00817
83A	8/30/75	He	4.003	78.0	12.7	32900	80.1	71.6	0.228	0.255	0.00582
85A	9/10/75	He	4.003	75.5	12.5	32500	76.4	67.6	0.235	0.265	0.00586
86A	9/12/75	He-Ar	15.83	72.3	12.3	27800	97.7	96.1	0.0916	0.0931	0.00619
87A	9/12/75	He-Ar	15.83	72.7	24.6	55400	76.0	68.6	0.233	0.258	0.00509
88A	10/ 8/75	He-Ar	15.83	73.0	26.5	59700	74.6	65.4	0.255	0.290	0.00515
91A	10/ 8/75	He-Ar	15.83	72.7	27.7	62400	83.0	74.4	0.240	0.267	0.00503
92A	10/13/75	He-Ar	15.83	72.3	14.1	31700	95.8	93.8	0.106	0.109	0.00607
95A	10/13/75	He-Ar	15.83	72.7	14.1	31800	95.5	93.5	0.107	0.110	0.00597
96A	10/20/75	He-Ar	15.83	72.7	38.3	86100	96.3	82.3	0.285	0.331	0.00468
99A	11/17/75	He-Ar	29.70	70.0	41.8	94200	74.5	63.1	0.293	0.344	0.00458
100A	11/17/75	He-Ar	29.70	70.0	29.9	67300	91.7	87.3	0.172	0.180	0.00493
101A	1/28/76	He-Ar	29.70	71.0	37.0	83200	110.5	105.5	0.176	0.185	0.00447
106A	1/28/76	He-Ar	29.70	72.7	13.9	31100	93.0	91.9	0.0790	0.0799	0.00614
110A	1/29/76	He-Ar	29.70	67.0	14.3	32400	93.4	92.2	0.0810	0.0819	0.00585
113A	2/ 6/76	He-Ar	27.53	73.0	13.5	30200	89.8	88.7	0.0828	0.0838	0.00588
114A	2/ 6/76	He-Ar	27.53	74.0	34.7	77500	110.2	105.0	0.173	0.181	0.00476
115A	2/21/76	He-Ar	27.53	70.5	43.8	98300	96.7	87.1	0.247	0.273	0.00457
121A	2/21/76	He-Ar	27.53	71.0	43.6	97800	95.3	85.5	0.249	0.277	0.00459
122A	3/ 1/76	He-Ar	15.30	70.5	24.7	55700	77.5	70.2	0.232	0.256	0.00497
123A	3/ 1/76	He-Ar	15.30	70.5	14.2	32200	92.8	90.7	0.113	0.115	0.00568

The headings and their definitions used in the listing of the heated flow data are below. The headings that are self-explanatory, or that were used in the listing of the adiabatic friction data are not included.

<u>Heading</u>	<u>Definition</u>
TIN	Inlet mixer temperature
TOUT	Outlet mixer temperature
I	Alternating current
E	Voltage drop between voltage taps
TC	Thermocouple number
X/D	Corresponds to x/D in text
TW	Inside tube wall temperature
TW/TB	Wall-to-bulk temperature ratio
QGAS	Wall heat flux
$Q^+$	Non-dimensional heat flux parameter. Corresponds to $q^+$ in text.
PT	Pressure tap: 1-inlet, 2-outlet
TB	Bulk static temperature

RUN 99HP, DATE 10/08/75, GAS HE-AR, MOLECULAR WT. = 15.83  
 PIN = 72.9 P, TOUT = 308.7 P, MASS FLOW RATE = 24.1 LB/HR, I = 100.2 AMPS, E = 5.765 VOLTS  
 PR,IN = .415, GR/RESQ = .725E-04, MACH(2) = .217, MACH(16) = .305, T, SURR = 75.5 P

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSLEIT	QGAS BTU/HR FT <sup>2</sup>	2*
2	.1	130.0	1.122	34772.2	.062	250.36	57729.3	.001195
3	1.2	194.6	1.239	54528.8	.105	116.28	5763.4	.001184
4	2.1	224.4	1.290	54334.4	.030	101.37	59976.7	.001231
5	4.1	256.0	1.336	53891.4	.020	36.42	60655.1	.001245
6	3.1	287.5	1.369	53073.3	.018	76.37	50965.9	.001251
7	15.4	319.1	1.374	51479.9	.016	71.00	61182.5	.001256
8	24.5	348.4	1.375	50042.2	.018	56.62	61233.2	.001257
9	32.4	366.7	1.360	48742.2	.017	65.88	61329.4	.001259
10	40.8	390.0	1.351	47451.1	.019	61.36	61308.0	.001253
11	48.7	407.1	1.336	46315.5	.019	51.70	61400.4	.001263
12	56.9	430.6	1.330	45229.9	.021	61.64	61359.4	.001259
13	64.9	448.1	1.318	44229.9	.022	51.42	61417.9	.001261
14	73.1	472.0	1.313	43249.9	.025	59.52	61349.9	.001259
15	81.3	487.3	1.298	42351.1	.027	60.07	61282.7	.001258
16	91.1	493.5	1.259	41452.1	.044	63.05	60274.0	.001237
17	99.0	435.6	1.165	40769.9	.198	32.24	52321.3	.001074

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	80.5	1.10	293.5	.0015E-02
2	90.1	67.8	1.27	291.4	.199E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 48129. AVERAGE WALL REYNOLDS 36951. AVERAGE FRICTION FACTOR .00554

RUN 90HP, DATE 10/08/75, GAS HE-AR, MOLECULAR WT. = 15.83  
 PIN = 72.8 P, TOUT = 547.4 P, MASS FLOW RATE = 25.1 LB/HR, I = 142.7 AMPS, E = 3.520 VOLTS  
 PR,IN = .415, GR/RESQ = .166E-03, MACH(2) = .204, MACH(16) = .340, T, SURR = 79.5 P

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSLEIT	QGAS BTU/HR FT <sup>2</sup>	2*
2	.1	109.2	1.248	36716.5	.073	230.87	116316.4	.002330
3	1.2	125.0	1.472	56221.1	.105	113.49	114231.9	.002255
4	2.1	144.4	1.472	55827.7	.031	101.37	122912.0	.002425
5	4.1	168.1	1.531	54951.1	.023	86.13	124446.7	.002497
6	3.1	193.1	1.523	53350.0	.023	86.13	124446.7	.002497
7	15.4	239.3	1.725	50410.0	.022	90.00	125787.1	.002483
8	24.5	255.3	1.708	47907.7	.025	90.00	125787.1	.002483
9	32.4	269.8	1.675	45769.9	.026	90.00	125787.1	.002493
10	40.8	282.2	1.642	43763.3	.029	90.00	125787.1	.002494
11	48.7	288.5	1.508	42033.3	.030	90.00	125787.1	.002497
12	56.9	297.8	1.584	40478.8	.034	90.00	125787.1	.002496
13	64.9	306.6	1.551	39108.8	.036	89.56	125787.1	.002497
14	73.1	312.2	1.512	37806.6	.036	89.56	125787.1	.002497
15	81.3	321.8	1.478	36650.0	.042	89.56	125787.1	.002497
16	91.1	328.3	1.422	35538.8	.066	51.93	123450.7	.002437
17	99.0	296.6	1.246	34792.2	.437	65.98	90759.6	.001792

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	88.7	1.19	67.6	.512E-02
2	90.4	71.5	1.42	516.7	.283E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 46161. AVERAGE WALL REYNOLDS 30486. AVERAGE FRICTION FACTOR .00549

RUN 93HF, DATE 10/13/75, GAS HE-AR, MOLECULAR WT. = 15.83  
 TIV = 72.3 F, TOUT = 348.8 F, MASS FLOW RATE = 14.1 LB/HR, I = 80.0 AMPS, E = 4.535 VOLTS  
 PR,IN = .419, GR/RESQ = .187E-03, MACH(2) = .107, MACH(16) = .134, T, SURR = 75.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT <sup>2</sup>	Q*
2	.1	120.3	1.091	31673.	.067	194.11	38616.7	.001289
3	.2	178.1	1.193	31523.	.140	83.56	38690.1	.001211
4	.3	209.2	1.246	31401.	.054	70.05	38739.7	.001151
5	.4	236.1	1.282	31125.	.026	96.97	38838.4	.001151
6	.5	257.7	1.313	30607.	.024	96.12	38855.7	.001151
7	.6	266.1	1.326	29597.	.024	86.48	38649.4	.001161
8	.7	271.1	1.346	28687.	.025	86.71	38705.0	.001161
9	.8	277.9	1.367	27872.	.026	86.13	38717.9	.001161
10	.9	288.8	1.388	27067.	.028	86.32	38702.5	.001161
11	1.0	293.3	1.407	26354.	.031	86.16	38687.9	.001162
12	1.1	297.1	1.425	25660.	.032	86.73	38674.3	.001162
13	1.2	300.9	1.442	24951.	.033	86.92	38668.4	.001162
14	1.3	304.7	1.458	24245.	.037	87.11	38659.9	.001162
15	1.4	308.5	1.473	23538.	.042	87.90	38648.1	.001162
16	1.5	312.3	1.487	22832.	.073	43.63	37399.8	.001161
17	1.6	316.1	1.501	22126.	.273	97.21	31339.4	.001103

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DIFF. (F)
1	.5	95.9	1.37	71.5	-.589E-02
2	90.1	92.3	1.21	328.7	-.197E+01

AVERAGE BULK REYNOLDS 27508.      AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 22429.      AVERAGE FRICTION FACTOR .00638

RUN 94HF, DATE 10/13/75, GAS HE-AR, MOLECULAR WT. = 15.83  
 TIV = 72.8 F, TOUT = 348.2 F, MASS FLOW RATE = 14.1 LB/HR, I = 118.6 AMPS, E = 7.395 VOLTS  
 PR,IN = .418, GR/RESQ = .407E-03, MACH(2) = .107, MACH(16) = .161, T, SURR = 73.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT <sup>2</sup>	Q*
2	.1	199.0	1.234	31584.	.093	158.74	79013.0	.002775
3	.2	322.9	1.449	31259.	.148	77.42	75890.4	.002607
4	.3	390.9	1.560	31001.	.053	66.89	83189.3	.002323
5	.4	462.5	1.652	30411.	.037	56.25	84907.8	.002333
6	.5	544.2	1.720	29343.	.036	47.47	85470.4	.002333
7	.6	635.2	1.721	27807.	.037	41.08	85947.1	.002333
8	.7	705.5	1.693	25803.	.041	37.37	85991.8	.002333
9	.8	754.9	1.644	24462.	.043	35.69	86094.4	.002333
10	.9	803.9	1.595	23203.	.048	34.25	85989.1	.002333
11	1.0	852.3	1.556	22169.	.052	33.00	85945.7	.002333
12	1.1	892.4	1.511	21237.	.057	32.47	85817.6	.002333
13	1.2	928.8	1.464	20417.	.059	32.62	85795.5	.002333
14	1.3	969.3	1.430	19640.	.066	32.01	85537.3	.002333
15	1.4	1006.2	1.395	18924.	.074	31.88	85360.9	.002333
16	1.5	1015.7	1.335	18282.	.119	33.33	81739.7	.002333
17	1.6	1031.7	1.130	17894.	.885	49.25	47896.7	.001683

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DIFF. (F)
1	.5	95.8	1.18	73.2	-.589E-02
2	90.4	90.4	1.33	545.4	.300E+01

AVERAGE BULK REYNOLDS 24956.      AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 17318.      AVERAGE FRICTION FACTOR .00655

RUN 98HP, DATE 10/20/75, GAS HE-AR, MOLECULAR WT. = 15.83  
 T<sub>IN</sub> = 73.2 F, T<sub>OUT</sub> = 570.4 F, MASS FLOW RATE = 30.8 LB/HR, I = 160.9 AMPS, E = 9.670 VOLTS  
 PR<sub>IN</sub> = .413, GR/RESQ = .213E-03, NACH(2) = .204, NACH(16) = .340, T<sub>SURR</sub> = 79.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT <sup>2</sup>	Q*
2	.1	235.9	1.259	39554.	.058	235.58	150418.8	.002417
3	1.2	353.4	1.517	68910.	.092	115.09	147299.2	.002365
4	2.1	418.9	1.631	68401.	.029	115.83	157043.5	.002523
5	4.1	490.3	1.729	67285.	.022	97.85	158341.7	.002522
6	8.1	559.8	1.787	65254.	.020	95.50	160013.2	.002571
7	16.4	641.1	1.791	61530.	.020	75.28	160388.0	.002585
8	24.6	705.7	1.772	58370.	.022	68.94	161295.5	.002591
9	32.5	759.6	1.744	55688.	.024	64.72	161519.6	.002597
10	40.9	809.6	1.707	53173.	.026	64.55	161776.6	.002599
11	49.9	859.9	1.680	51003.	.029	64.48	161951.1	.002602
12	59.0	894.6	1.636	49083.	.030	64.52	162139.9	.002605
13	68.4	931.1	1.601	47376.	.032	64.66	162339.4	.002605
14	77.9	970.6	1.568	45758.	.035	64.77	162549.3	.002605
15	87.4	996.8	1.527	44325.	.039	64.60	162789.9	.002605
16	90.4	1002.0	1.465	42947.	.059	57.99	158784.5	.002551
17	98.4	861.7	1.282	41994.	.407	71.18	118411.6	.001902

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	109.4	1.20	68.2	-.488E-02
2	90.4	88.7	1.46	537.9	.275E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 56296. AVERAGE WALL REYNOLDS 36396. AVERAGE FRICTION FACTOR .00517

RUN 97HP, DATE 10/20/75, GAS HE-AR, MOLECULAR WT. = 15.83  
 T<sub>IN</sub> = 72.3 F, T<sub>OUT</sub> = 298.2 F, MASS FLOW RATE = 35.3 LB/HR, I = 117.2 AMPS, E = 5.793 VOLTS  
 PR<sub>IN</sub> = .418, GR/RESQ = .336E-04, NACH(2) = .238, NACH(16) = .337, T<sub>SURR</sub> = 75.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT <sup>2</sup>	Q*
2	.1	131.5	1.129	80349.	.049	333.86	79933.4	.001124
3	1.2	199.2	1.253	80006.	.078	156.22	78204.2	.001099
4	2.1	231.6	1.309	79735.	.024	132.51	82555.1	.001160
5	4.1	264.6	1.359	79124.	.017	112.68	83345.5	.001171
6	8.1	291.3	1.385	77995.	.013	102.45	83824.7	.001179
7	16.4	321.0	1.389	75803.	.012	95.65	84077.0	.001181
8	24.6	351.3	1.396	73808.	.013	89.06	84153.5	.001192
9	32.5	368.9	1.379	71996.	.013	88.74	84332.6	.001194
10	40.9	390.2	1.373	70209.	.014	85.66	84338.8	.001194
11	49.9	408.9	1.361	68614.	.014	84.61	84433.8	.001186
12	59.0	433.9	1.360	67089.	.016	81.05	84434.7	.001185
13	68.4	458.9	1.352	65693.	.017	79.45	84436.5	.001187
14	77.9	483.9	1.314	64312.	.017	79.78	84511.9	.001187
15	87.4	488.9	1.324	63048.	.020	78.99	84428.2	.001186
16	90.4	488.9	1.295	61787.	.031	84.33	83568.6	.001173
17	98.4	447.8	1.213	60798.	.159	105.05	74055.2	.001040

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	106.9	1.10	63.5	-.473E-02
2	90.1	98.5	1.29	272.3	.193E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 71091. AVERAGE WALL REYNOLDS 53547. AVERAGE FRICTION FACTOR .00491

RUN 102H, DATE 01/23/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 T<sub>IN</sub> = 70.1 °F, T<sub>OUT</sub> = 573.9 °F, MASS FLOW RATE = 36.4 LB/HR, I = 127.8 AMPS, E = 7.670 VOLTS  
 PR<sub>IN</sub> = .486, GR/RESQ = .755E-03, HACH(2) = .173, HACH(16) = .258, I<sub>SURR</sub> = 77.0 F

TC	X/D	T <sub>W</sub> (F)	T <sub>W</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q+
2	1.1	197.7	1.246	82080.	.074	403.77	93352.5	.0022347
3	1.2	353.3	1.526	81162.	.157	171.51	87626.3	.0022250
4	2.1	429.7	1.650	80694.	.052	149.61	96930.4	.0022434
5	4.1	497.7	1.747	79114.	.034	129.60	99071.8	.0022543
6	9.1	573.3	1.815	76799.	.033	111.67	99727.5	.0022573
7	16.4	663.3	1.832	72178.	.034	96.47	100240.4	.0022573
8	24.8	726.4	1.807	68290.	.037	88.45	100391.2	.0022577
9	32.5	776.4	1.770	64994.	.040	83.42	100492.6	.0022585
10	40.9	820.5	1.723	61915.	.043	79.88	100454.8	.0022579
11	48.9	864.9	1.687	59322.	.046	76.59	100466.7	.0022573
12	57.0	903.3	1.646	56944.	.050	74.42	100362.5	.0022577
13	65.0	931.1	1.599	54893.	.052	74.06	100379.9	.0022577
14	73.4	969.6	1.505	52922.	.057	72.35	100186.0	.0022572
15	81.5	993.9	1.523	51138.	.062	72.78	99864.5	.0022564
16	90.4	999.8	1.458	49522.	.098	74.44	96564.4	.0022473
17	98.4	786.6	1.205	44437.	.568	114.98	66066.2	.0021712

PT	X/D	STATIC PRESS. (PSIA)	T <sub>W</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS DETECT
1	5	110.6	1.20	97.0	-.470E-02
2	90.4	97.1	1.46	341.2	.245E+01

RUN 103H, DATE 01/23/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 T<sub>IN</sub> = 71.0 °F, T<sub>OUT</sub> = 471.8 °F, MASS FLOW RATE = 36.2 LB/HR, I = 113.8 AMPS, E = 6.715 VOLTS  
 PR<sub>IN</sub> = .486, GR/RESQ = .593E-03, HACH(2) = .173, HACH(16) = .251, I<sub>SURR</sub> = 90.0 F

TC	X/D	T <sub>W</sub> (F)	T <sub>W</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q+
2	1.1	191.6	1.234	31602.	.109	326.29	71673.1	.0018447
3	1.2	399.7	1.428	31002.	.146	169.15	69860.6	.0018000
4	2.1	454.5	1.521	30522.	.046	150.74	76889.8	.001982
5	4.1	412.7	1.604	29421.	.035	127.99	77936.3	.002010
6	9.1	562.8	1.646	27393.	.029	114.59	78785.5	.002030
7	16.4	626.0	1.655	25587.	.029	101.97	79123.1	.002039
8	24.8	674.6	1.642	22993.	.031	94.48	79231.0	.002042
9	32.5	610.7	1.614	21433.	.032	90.55	79364.3	.002045
10	40.9	649.4	1.589	20701.	.035	86.49	79300.6	.002044
11	48.9	682.5	1.561	20360.	.037	83.90	79300.5	.002049
12	56.9	715.0	1.534	20196.	.040	81.57	79301.2	.002044
13	64.9	740.6	1.502	18258.	.041	80.88	79336.5	.002045
14	73.3	767.8	1.472	16404.	.045	80.13	79237.5	.002042
15	81.5	793.0	1.443	14743.	.050	79.75	79005.6	.002036
16	90.4	799.1	1.393	13137.	.082	82.02	76860.3	.001976
17	98.2	634.9	1.175	12034.	.382	144.05	59365.5	.0015330

PT	X/D	STATIC PRESS. (PSIA)	T <sub>W</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS DETECT
1	5	110.0	1.19	67.4	-.471E-02
2	90.3	98.3	1.39	444.1	.212E+01

AVERAGE BULK REYNOLDS 67411. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 45005. AVERAGE FRICTION FACTOR .00483



RUN 104H, DATE 01/29/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 TIN = 72.3 F, TOUT = 305.7 F, MASS FLOW RATE = 36.2 LB/HR, I = 87.4 AMPS, E = 5.020 VOLTS  
 PR,IN = .486, GR/RESQ = .348E-03, MACH(2) = .173, MACH(16) = .223, T, SURR = 80.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK MUSSELT	QGAS BTU/HR FT2	Q*
2	.1	149.3	1.153	81642.	.119	293.35	41733.4	.001072
3	1.2	203.3	1.259	91275.	.141	167.11	41120.4	.001036
4	2.1	237.7	1.309	30994.	.042	151.83	45115.1	.001139
5	4.1	264.5	1.347	80344.	.026	135.08	45339.1	.001130
6	8.1	293.3	1.377	79119.	.023	121.02	46169.9	.001136
7	16.4	329.5	1.390	76716.	.022	109.38	46304.3	.001130
8	24.5	355.5	1.397	74536.	.023	104.34	46353.7	.001131
9	32.4	374.3	1.374	72577.	.023	102.42	46423.2	.001193
10	40.8	393.9	1.368	70620.	.026	98.20	46481.5	.001192
11	48.7	421.0	1.361	68880.	.027	95.15	46416.0	.001192
12	56.3	439.4	1.348	67234.	.028	93.75	46338.9	.001192
13	64.7	455.6	1.333	65708.	.029	91.40	46417.5	.001192
14	73.1	475.9	1.323	64201.	.032	91.35	46346.5	.001191
15	81.2	492.0	1.303	62827.	.036	91.29	46244.0	.001188
16	90.0	496.1	1.278	61452.	.060	95.16	45192.4	.001161
17	93.0	414.5	1.142	60411.	.225	161.89	38851.3	.000998

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	110.1	1.12	98.0	-.471E-02
2	90.1	101.1	1.28	288.4	.162E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 71562. AVERAGE WALL REYNOLDS 53128. AVERAGE FRICTION FACTOR .00484

RUN 105H, DATE 01/28/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 TIN = 71.9 F, TOUT = 197.5 F, MASS FLOW RATE = 36.3 LB/HR, I = 64.9 AMPS, E = 3.585 VOLTS  
 PR,IN = .486, GR/RESQ = .193E-03, MACH(2) = .173, MACH(16) = .204, T, SURR = 79.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK MUSSELT	QGAS BTU/HR FT2	Q*
2	.1	118.1	1.096	81892.	.119	268.31	22971.1	.000590
3	1.2	147.5	1.149	81699.	.136	164.83	22683.3	.000582
4	2.1	161.3	1.173	81541.	.028	155.74	25079.0	.000648
5	4.1	177.1	1.146	81177.	.025	139.57	25186.9	.000647
6	8.1	189.7	1.208	80493.	.018	126.54	25482.8	.000692
7	16.4	207.6	1.216	79108.	.018	117.60	25418.4	.000693
8	24.5	221.9	1.218	77799.	.018	112.70	25428.0	.000693
9	32.4	233.2	1.215	76546.	.019	110.75	25442.0	.000693
10	40.8	246.7	1.215	75357.	.020	107.18	25419.6	.000693
11	48.7	257.9	1.212	74225.	.021	105.46	25412.2	.000693
12	56.3	269.2	1.209	73129.	.022	103.81	25414.1	.000693
13	64.7	278.2	1.202	72086.	.023	104.13	25412.3	.000693
14	73.1	290.3	1.200	71032.	.025	101.97	25385.4	.000693
15	81.2	298.9	1.133	70048.	.028	102.70	25328.5	.000693
16	90.0	300.7	1.175	69037.	.046	108.99	24336.6	.000693
17	97.9	262.1	1.098	68229.	.145	182.22	22286.8	.000582

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	110.5	1.08	87.2	-.471E-02
2	90.0	103.3	1.17	187.7	.110E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 75477. AVERAGE WALL REYNOLDS 61625. AVERAGE FRICTION FACTOR .00480

RUN 107H, DATE 01/28/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 T<sub>IN</sub> = 72.3 F, T<sub>OUT</sub> = 709.6 F, MASS FLOW RATE = 13.9 LB/HR, I = 90.0 AMPS, E = 5.370 VOLTS  
 PR<sub>IN</sub> = .486, GR/RESQ = .153E-02, MACH(2) = .3033, MACH(16) = .123, T<sub>SURR</sub> = 79.5 F

TC	X/D	T <sub>w</sub> (F)	T <sub>w</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR/FT <sup>2</sup>	Q*
2	.1	140.6	1.216	31054.	.115	209.01	48574.7	.002976
3	1.2	326.7	1.454	30713.	.273	86.07	39414.0	.003361
4	2.1	411.0	1.594	30439.	.118	74.00	4374.0	.003144
5	4.1	498.1	1.711	29799.	.077	61.68	47669.0	.003182
6	8.1	591.6	1.792	28843.	.073	51.69	47869.0	.003187
7	16.4	694.5	1.795	28570.	.084	41.69	47739.3	.003180
8	24.5	753.8	1.753	28380.	.090	37.63	47630.8	.003165
9	32.5	816.7	1.699	27208.	.099	36.47	47425.4	.003157
10	40.9	862.4	1.636	26155.	.105	35.71	47235.4	.003139
11	48.9	903.7	1.562	25133.	.114	34.94	47010.1	.003125
12	57.0	934.7	1.484	24193.	.122	34.84	4682.6	.003107
13	65.0	978.0	1.413	23366.	.131	34.74	46536.3	.003072
14	73.3	1043.3	1.394	22621.	.146	33.58	46017.3	.003043
15	81.6	1083.3	1.331	21947.	.239	33.66	45544.3	.0031401
16	90.4	1249.3	1.026	17003.	1.463	255.03	20977.5	

PT	X/D	STATIC PRESS. (PSIA)	T <sub>w</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS DEFECT
1	.5	89.1	1.18	74.0	-.591E-02
2	90.4	86.1	1.33	674.0	-.297E+01

AVERAGE BULK REYNOLDS 24213. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 16879. AVERAGE FRICTION FACTOR .00642

RUN 108H, DATE 01/28/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 T<sub>IN</sub> = 73.2 F, T<sub>OUT</sub> = 519.7 F, MASS FLOW RATE = 14.0 LB/HR, I = 75.1 AMPS, E = 4.320 VOLTS  
 PR<sub>IN</sub> = .486, GR/RESQ = .106E-02, MACH(2) = .0833, MACH(16) = .113, T<sub>SURR</sub> = 90.3 F

TC	X/D	T <sub>w</sub> (F)	T <sub>w</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR/FT <sup>2</sup>	Q*
2	.1	168.6	1.177	31204.	.180	168.79	29250.3	.001945
3	1.2	254.2	1.326	30974.	.255	84.41	27664.7	.002182
4	2.1	306.1	1.413	30783.	.102	75.72	31682.7	.002135
5	4.1	360.4	1.487	30329.	.066	64.54	32856.8	.002184
6	8.1	414.5	1.534	29489.	.056	56.27	33230.0	.002212
7	16.4	430.8	1.544	27915.	.058	49.23	33330.3	.002219
8	24.5	526.7	1.524	26566.	.062	45.93	33377.5	.002218
9	32.5	566.0	1.499	24407.	.066	43.74	33345.0	.002216
10	40.9	599.5	1.464	23312.	.072	42.58	33272.4	.002210
11	48.9	639.5	1.439	22377.	.076	41.14	33176.1	.002205
12	57.0	662.7	1.405	21520.	.082	40.90	33071.3	.002198
13	65.0	696.9	1.376	20754.	.086	40.67	33003.9	.002194
14	73.3	723.3	1.352	20130.	.096	39.93	32776.7	.002179
15	81.6	748.4	1.321	19384.	.103	40.59	32558.9	.002164
16	90.2	756.7	1.279	18770.	.191	40.47	30233.4	.002110
17	99.2	551.6	1.033	13389.	.759	243.12	20186.9	.001342

PT	X/D	STATIC PRESS. (PSIA)	T <sub>w</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS DEFECT
1	.5	88.9	1.14	73.6	-.330E-02
2	90.2	86.5	1.28	491.6	-.239E+01

AVERAGE BULK REYNOLDS 25502. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 18693. AVERAGE FRICTION FACTOR .00627

RUN 109H, DATE 01/29/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 PIN = 74.1 F, POUT = 361.3 F, MASS FLOW RATE = 13.9 LB/HR, I = 60.0 AMPS, E = 3.300 VOLTS  
 PR,IN = .486, GR/RESQ = .681E-03, MACH(2) = .083, MACH(16) = .103, T, SURR = 80.7 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q*
2	.1	119.2	1.121	31140.	.197	154.86	18371.4	.001222
3	1.2	190.3	1.211	30995.	.256	83.98	17579.7	.001159
4	2.1	220.8	1.262	30872.	.090	77.30	20293.9	.001349
5	4.1	251.5	1.305	30578.	.053	57.58	21571.6	.001401
6	8.1	296.3	1.340	30020.	.047	58.82	21225.7	.001411
7	16.4	340.3	1.345	28945.	.046	51.74	21244.1	.001417
8	24.5	377.7	1.337	27121.	.047	49.40	21255.5	.001419
9	32.5	409.7	1.339	26278.	.051	48.71	21255.5	.001414
10	40.7	423.3	1.300	25534.	.054	47.37	21255.5	.001411
11	48.7	442.2	1.293	24835.	.062	47.11	21170.1	.001408
12	56.3	460.0	1.255	24198.	.064	46.55	21139.7	.001407
13	64.7	473.1	1.237	23571.	.071	46.55	21055.1	.001400
14	73.1	490.0	1.217	23005.	.080	46.55	20999.9	.001390
15	80.0	504.0	1.203	22452.	.145	46.55	20930.0	.001312
16	90.1	534.0	1.187	22064.	.299	29.26	15665.4	.001042

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	89.1	1.10	73.9	-.591E-02
2	90.1	87.1	1.20	341.5	-.191E+01

AVERAGE BULK REYNOLDS 26805. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 21228. AVERAGE FRICTION FACTOR .30612

RUN 111H, DATE 01/29/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 PIN = 67.0 F, POUT = 247.1 F, MASS FLOW RATE = 14.2 LB/HR, I = 48.0 AMPS, E = 2.920 VOLTS  
 PR,IN = .486, GR/RESQ = .446E-03, MACH(2) = .084, MACH(16) = .097, T, SURR = 72.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q*
2	.1	101.7	1.067	32094.	.116	201.07	12579.6	.000813
3	1.2	139.0	1.134	31993.	.269	86.36	11587.4	.000734
4	2.1	160.0	1.170	31911.	.095	78.39	12874.2	.000852
5	4.1	179.7	1.199	31718.	.048	69.21	13474.3	.000892
6	8.1	201.9	1.223	31345.	.042	60.50	13576.4	.000899
7	16.4	227.2	1.234	30601.	.041	54.85	13637.2	.000901
8	24.5	245.2	1.233	29918.	.042	52.62	13639.9	.000901
9	32.5	251.4	1.229	29246.	.045	51.03	13639.9	.000900
10	40.7	256.3	1.223	28556.	.048	50.07	13639.9	.000898
11	48.7	262.1	1.218	27848.	.050	48.39	13639.9	.000897
12	56.3	267.0	1.212	27136.	.054	48.39	13639.9	.000895
13	64.7	273.3	1.203	26422.	.056	48.39	13639.9	.000894
14	73.1	284.4	1.194	25713.	.064	47.11	13639.9	.000890
15	80.0	298.0	1.171	25059.	.130	46.55	13639.9	.000834
16	90.1	334.0	1.151	24517.	.296	28.55	11048.9	.000731

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	89.4	1.05	68.5	-.587E-02
2	90.0	87.7	1.17	234.1	-.158E+01

AVERAGE BULK REYNOLDS 29839. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 24231. AVERAGE FRICTION FACTOR .30593

RUN 112H, DATE 01/29/76, GAS HE-AR, MOLECULAR WT. = 29.70  
 TIN = 67.9 °F, TOUT = 132.9 °F, MASS FLOW RATE = 14.2 LB/HR, I = 38.4 AMPS, E = 2.250 VOLTS  
 PR,IN = .486, GR/RESQ = .284E-03, MACH(2) = .084, MACH(16) = .093, T, SURR = 72.3 °F

TC	X/D	T4 (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT2	Q+
2	.1	95.6	1.054	32001.	.172	151.80	7658.6	.000507
3	1.2	116.4	1.091	31938.	.227	84.67	7331.5	.000546
4	2.1	129.6	1.114	31884.	.087	75.75	8281.5	.000544
5	3.1	142.5	1.133	31759.	.050	66.48	8533.1	.000568
6	4.1	153.9	1.144	31520.	.036	61.16	8703.5	.000577
7	5.1	170.7	1.154	31032.	.038	55.38	8702.2	.000576
8	6.1	182.5	1.155	30571.	.039	53.28	8698.6	.000576
9	7.1	192.1	1.153	30141.	.040	52.53	8693.5	.000576
10	8.1	202.5	1.151	29702.	.044	51.48	8670.3	.000574
11	9.1	211.7	1.147	29296.	.044	51.12	8670.3	.000574
12	10.1	222.9	1.143	28900.	.049	49.42	8636.6	.000572
13	11.1	230.6	1.142	28528.	.050	49.90	8633.2	.000572
14	12.1	240.0	1.139	28147.	.054	49.45	8603.6	.000573
15	13.1	249.9	1.137	27790.	.064	48.35	8550.4	.000565
16	14.1	259.5	1.135	27432.	.116	49.35	8516.6	.000565
17	15.1	260.1	1.027	27149.	.234	217.49	7332.2	.000566

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	89.3	1.04	87.1	-.347E-02
2	90.0	87.9	1.12	174.4	-.140E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 29720. AVERAGE WALL REYNOLDS 25498. AVERAGE FRICTION FACTOR .00590

RUN 116H, DATE 02/21/76, GAS HE-AR, MOLECULAR WT. = 27.53  
 TIN = 70.1 °F, TOUT = 154.2 °F, MASS FLOW RATE = 44.1 LB/HR, I = 65.2 AMPS, E = 3.76 VOLTS  
 PR,IN = .465, GR/RESQ = .908E-04, MACH(2) = .247, MACH(16) = .307, T, SURR = 73.3 °F

TC	X/D	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT2	Q+
2	.1	1.069	100497.	.057	430.23	24488.4	.000481
3	1.2	1.129	100309.	.130	188.90	23262.8	.000491
4	2.1	1.151	100162.	.027	174.52	23297.7	.000497
5	3.1	1.169	99822.	.018	154.26	23530.3	.000501
6	4.1	1.181	99179.	.014	142.00	23658.4	.000506
7	5.1	1.190	97897.	.014	131.66	23710.6	.000505
8	6.1	1.190	96690.	.014	128.76	23710.6	.000505
9	7.1	1.192	95548.	.015	124.98	23705.2	.000505
10	8.1	1.187	94370.	.015	123.98	23714.5	.000505
11	9.1	1.188	93303.	.016	122.87	23714.5	.000505
12	10.1	1.188	92249.	.017	120.28	23703.5	.000505
13	11.1	1.184	91243.	.017	120.46	23707.0	.000505
14	12.1	1.183	90219.	.018	119.31	23691.2	.000505
15	13.1	1.180	89269.	.021	119.52	23642.6	.000504
16	14.1	1.157	88285.	.035	126.47	23304.6	.000497
17	15.1	1.099	87476.	.096	225.52	23824.8	.000468

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	97.1	1.06	60.0	-.450E-02
2	90.0	84.2	1.17	147.3	-.137E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 94402. AVERAGE WALL REYNOLDS 78875. AVERAGE FRICTION FACTOR .00464

RUN 117H, DATE 02/21/76, GAS HE-AR, MOLECULAR WT. = 27.53  
 TIN = 70.1 F, TOUT = 287.8 F, MASS FLOW RATE = 44.2 LB/HR, I = 103.7 AMPS, E = 5.750 VOLTS  
 PR,IN = .465, GR/RESQ = .195E-03, MACH(2) = .246, MACH(16) = .352, T, SURR = 74.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK MUSSELT	QGAS BTU/HR FT2	Q*
2	1.1	131.7	1.136	100521.	.065	451.90	38156.6	.0011143
3	1.2	202.9	1.267	100069.	.114	206.43	35920.5	.0010996
5	2.1	235.7	1.324	99712.	.037	179.63	60203.2	.0011995
6	4.1	262.7	1.363	98903.	.020	160.09	61333.4	.0012002
7	9.1	292.1	1.393	97418.	.017	143.53	61607.4	.0012008
8	15.4	331.4	1.413	94475.	.018	128.26	61761.0	.0012111
9	24.5	356.1	1.409	91886.	.018	122.80	61965.7	.0012113
10	32.4	379.0	1.403	89457.	.019	118.39	61922.7	.0012114
11	40.8	398.6	1.389	87095.	.020	116.34	61944.0	.0012114
12	48.7	422.3	1.385	85011.	.021	112.17	61982.2	.0012115
13	56.8	439.1	1.371	83026.	.022	111.32	61981.4	.0012115
14	64.6	454.0	1.355	81207.	.022	111.68	62031.4	.0012116
15	73.1	473.8	1.346	79419.	.024	109.87	61931.5	.0012115
16	81.3	490.4	1.334	77779.	.027	109.50	61885.8	.0012113
17	90.1	491.8	1.300	76162.	.045	116.51	60861.7	.0011993
	98.0	415.6	1.170	74930.	.175	195.34	53799.3	.0010555

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	5	97.8	1.11	70.7	-.458E-02
2	90.1	80.5	1.30	272.1	.177E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 88371. AVERAGE WALL REYNOLDS 65677. AVERAGE FRICTION FACTOR .00453

RUN 118H, DATE 02/21/76, GAS HE-AR, MOLECULAR WT. = 27.53  
 TIN = 70.1 F, TOUT = 407.9 F, MASS FLOW RATE = 44.9 LB/HR, I = 123.4 AMPS, E = 7.220 VOLTS  
 PR,IN = .465, GR/RESQ = .354E-03, MACH(2) = .223, MACH(16) = .339, T, SURR = 78.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK MUSSELT	QGAS BTU/HR FT2	Q*
2	1.1	179.3	1.221	101647.	.084	382.46	36114.1	.0016662
3	1.2	278.0	1.400	100972.	.111	200.05	34677.3	.0015334
4	2.1	327.6	1.486	100431.	.036	174.60	10955.0	.0017388
5	4.1	375.2	1.534	99234.	.025	151.19	92425.3	.0017388
6	9.1	420.1	1.594	97016.	.021	135.21	91059.2	.0017388
7	15.4	475.1	1.605	92800.	.021	121.31	91442.4	.0018007
8	24.5	519.6	1.601	89109.	.022	112.57	93605.2	.0018007
9	32.4	554.4	1.584	85870.	.023	107.43	93754.0	.0018113
10	40.8	585.9	1.560	82755.	.025	103.88	93771.6	.0018113
11	48.7	613.3	1.535	80063.	.026	101.56	93909.9	.0018113
12	56.8	643.3	1.515	77558.	.028	98.75	93879.8	.0018112
13	64.6	670.7	1.494	75304.	.029	97.03	93934.6	.0018113
14	73.1	694.8	1.469	73127.	.032	96.28	93886.6	.0018112
15	81.4	713.5	1.441	71175.	.034	96.96	93761.3	.0018113
16	90.2	721.4	1.399	69273.	.057	99.87	91823.8	.0017772
17	98.2	605.4	1.227	67918.	.283	147.20	75005.9	.0014448

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	5	109.6	1.18	63.0	-.448E-02
2	90.2	90.6	1.40	384.6	.203E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 85507. AVERAGE WALL REYNOLDS 57344. AVERAGE FRICTION FACTOR .00456

RUN 119H, DATE 02/21/76, GAS HE-AR, MOLECULAR WT. = 27.53  
 TIN = 71.9 F, TOUT = 452.4 F, MASS FLOW RATE = 44.7 LB/HR, I = 130.3 AMPS, E = 7.720 VOLTS  
 PR,IN = .465, GR/RESQ = .392E-03, MACH(2) = .224, MACH(16) = .355, T,SURR = 91.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q+
2	.1	195.0	1.247	101063.	.088	379.79	96546.3	.001862
3	1.2	310.6	1.455	100308.	.116	194.69	94971.1	.001835
4	2.1	360.7	1.540	99719.	.033	175.36	102932.5	.001835
5	4.1	411.2	1.609	98383.	.024	152.65	104166.6	.002003
6	8.1	463.2	1.655	95949.	.022	135.40	104820.0	.002003
7	16.4	533.1	1.675	91248.	.022	119.03	105271.3	.002033
8	24.5	584.4	1.671	87330.	.024	109.16	105467.6	.002033
9	32.4	624.4	1.650	83833.	.023	103.80	105648.3	.002037
10	40.7	657.7	1.616	80532.	.027	100.70	105689.0	.002037
11	48.8	690.9	1.590	77699.	.028	97.66	105821.9	.002041
12	56.9	723.1	1.565	75087.	.031	94.94	105796.1	.002043
13	64.7	752.3	1.538	72748.	.032	93.43	105865.9	.002042
14	73.1	781.3	1.514	70509.	.035	91.64	105789.9	.002043
15	81.2	807.1	1.485	68517.	.039	91.62	105602.2	.002037
16	90.0	807.6	1.429	66592.	.061	96.25	103362.8	.001933
17	98.2	675.3	1.243	65258.	.329	137.89	81768.2	.001577

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	109.1	1.19	64.8	-.449E-02
2	90.3	88.5	1.43	427.0	.227E+01

AVERAGE BULK REYNOLDS 83880. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 54686. AVERAGE FRICTION FACTOR .00460

RUN 120H, DATE 02/21/76, GAS HE-AR, MOLECULAR WT. = 27.53  
 TIN = 71.9 F, TOUT = 208.2 F, MASS FLOW RATE = 43.7 LB/HR, I = 80.8 AMPS, E = 4.750 VOLTS  
 PR,IN = .465, GR/RESQ = .121E-03, MACH(2) = .249, MACH(16) = .330, T,SURR = 80.7 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q+
2	.1	131.0	1.132	99419.	.103	299.31	36159.9	.000713
3	1.2	165.5	1.195	99143.	.096	188.89	36484.6	.000722
4	2.1	185.4	1.230	98914.	.031	167.61	38836.4	.000766
5	4.1	204.1	1.258	98394.	.021	148.35	39274.5	.000775
6	8.1	217.9	1.269	97431.	.014	140.04	39555.2	.000780
7	16.4	242.7	1.285	95506.	.015	127.00	39501.2	.000781
8	24.5	262.5	1.292	93706.	.016	119.40	39614.7	.000781
9	32.4	272.0	1.281	92068.	.015	120.33	39678.3	.000783
10	40.7	289.6	1.283	90392.	.017	115.16	39645.0	.000782
11	48.8	302.7	1.279	88882.	.017	113.39	39631.8	.000783
12	56.9	316.8	1.276	87421.	.019	110.87	39661.3	.000782
13	64.7	327.3	1.269	86044.	.019	111.05	39634.3	.000783
14	73.1	341.4	1.266	84687.	.021	108.85	39648.9	.000782
15	81.2	352.0	1.259	83404.	.024	109.06	39585.8	.000781
16	90.0	353.9	1.237	82119.	.038	115.36	39029.6	.000773
17	97.9	316.2	1.161	81098.	.146	161.25	35272.3	.000696

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	95.3	1.11	61.7	-.451E-02
2	90.0	80.6	1.24	197.8	.151E+01

AVERAGE BULK REYNOLDS 90788. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 69459. AVERAGE FRICTION FACTOR .00464

RUN 124H, DATE 03/01/76, GAS HE-AR, MOLECULAR WT. = 15.33  
 PIN = 70.5 P, POUT = 183.2 P, MASS FLOW RATE = 14.2 LB/HR, I = 52.7 AMPS, E = 3.370 VOLTS  
 PR,IN = .419, GR/RESQ = .682E-04, MACH(2) = .113, MACH(16) = .127, T, SURR = 74.0 P

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QJAS BTU/HRFT2	Q*
2	.1	91.7	1.043	32217.	.057	183.33	15390.7	.003543
3	1.2	116.6	1.088	32152.	.145	73.76	14790.6	.000500
4	2.1	129.4	1.108	32102.	.040	70.71	16309.8	.003531
5	4.1	140.0	1.125	31984.	.023	61.57	16583.2	.000590
6	8.1	151.9	1.137	31758.	.018	55.39	16676.9	.003563
7	16.4	167.3	1.145	31301.	.019	50.77	16693.4	.000564
8	24.5	179.2	1.146	30867.	.019	48.72	16634.2	.003564
9	32.3	189.2	1.145	30465.	.020	47.73	16631.6	.003564
10	40.7	199.6	1.144	30051.	.022	46.80	16676.9	.003563
11	48.7	209.6	1.143	29668.	.023	45.92	16675.6	.003563
12	56.8	219.9	1.142	29294.	.025	44.97	16658.2	.000563
13	64.7	228.9	1.139	28939.	.026	44.68	16650.8	.003563
14	73.0	239.2	1.137	28576.	.028	43.84	16625.3	.000562
15	81.2	247.8	1.134	28236.	.032	43.78	16571.5	.003563
16	89.9	251.9	1.122	27888.	.055	45.84	16219.9	.000548
17	97.9	219.0	1.056	27604.	.148	93.90	14866.6	.003532

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DIFFERENTIAL
1	.5	92.7	1.03	68.2	-.585E-02
2	90.0	90.0	1.12	174.5	.140E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 30057. AVERAGE WALL REYNOLDS 26548. AVERAGE FRICTION FACTOR .00584

RUN 125H, DATE 03/01/76, GAS HE-AR, MOLECULAR WT. = 15.33  
 PIN = 71.0 P, POUT = 345.8 P, MASS FLOW RATE = 14.2 LB/HR, I = 51.5 AMPS, E = 4.335 VOLTS  
 PR,IN = .419, GR/RESQ = .163E-03, MACH(2) = .113, MACH(16) = .142, T, SURR = 75.5 P

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QJAS BTU/HRFT2	Q*
2	.1	126.4	1.106	32051.	.083	166.09	17434.2	.001267
3	1.2	182.3	1.205	31902.	.140	73.94	15721.2	.001209
4	2.1	210.9	1.253	31782.	.044	70.18	39079.5	.001323
5	4.1	239.1	1.292	31504.	.027	60.73	39823.1	.001348
6	8.1	269.3	1.320	30978.	.023	53.68	40054.8	.001356
7	15.4	307.3	1.332	29961.	.023	48.25	40154.4	.001359
8	24.5	335.2	1.327	29044.	.024	45.79	40192.7	.001360
9	32.3	358.5	1.316	28218.	.025	44.46	40223.7	.001361
10	40.7	382.3	1.305	27407.	.028	43.29	40192.0	.001360
11	48.7	405.4	1.295	26689.	.029	42.22	40217.4	.001361
12	56.8	428.4	1.285	26007.	.032	41.22	40165.1	.001359
13	64.7	448.2	1.272	25381.	.033	40.94	40176.9	.001360
14	73.0	470.4	1.261	24765.	.037	40.25	40101.7	.001357
15	81.2	491.3	1.250	24203.	.041	39.84	39978.7	.001353
16	89.9	502.1	1.225	23635.	.072	40.91	38357.9	.001315
17	98.0	421.0	1.093	23210.	.275	81.51	32487.7	.001100

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DIFFERENTIAL
1	.5	92.7	1.08	69.9	-.585E-02
2	90.1	89.0	1.22	325.8	.187E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 27853. AVERAGE WALL REYNOLDS 22239. AVERAGE FRICTION FACTOR .00599

RUN 126H, DATE 03/01/76, GAS HE-AR, MOLECULAR WT. = 15.33  
 TIN = 71.9 P, TOUT = 167.5 P, MASS FLOW RATE = 24.5 LB/HR, I = 68.2 AMPS, E = 3.955 VOLTS  
 PR,IN = .419, GR/RESQ = .273E-04, MACH(2) = .234, MACH(16) = .297, T,SURR = 76.3 F

TC	X/D	TR (F)	TR/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q+
2	.1	152.7	1.077	31735.	.071	194.39	28468.8	.000519
3	1.2	246.1	1.119	31502.	.090	114.68	28352.6	.000509
4	2.1	290.2	1.139	31316.	.024	102.74	27754.6	.000543
5	4.1	334.9	1.153	30630.	.014	92.56	28343.2	.000519
6	8.1	488.1	1.165	30256.	.012	84.37	28128.7	.000590
7	16.4	644.9	1.174	30509.	.012	78.11	28161.9	.000551
8	24.5	889.5	1.176	33802.	.012	75.05	28172.9	.000551
9	32.4	925.6	1.175	33134.	.013	71.75	28180.6	.000551
10	40.7	970.4	1.174	32458.	.014	72.53	28176.2	.000551
11	48.7	1015.1	1.174	31836.	.014	70.88	28181.5	.000551
12	56.8	1060.0	1.174	31221.	.015	69.59	28173.7	.000551
13	64.7	1104.6	1.171	30638.	.016	69.27	28174.0	.000551
14	73.0	1149.0	1.170	30053.	.017	68.55	28150.4	.000551
15	81.2	1193.8	1.167	29498.	.020	68.24	28108.0	.000551
16	89.9	1238.6	1.153	28925.	.031	72.99	27790.9	.000543
17	97.9	1283.7	1.107	28460.	.106	103.78	25883.9	.000506

PT	X/D	STATIC PRESS. (PSIA)	TR/TB	TB (F)	PRESS DEFECT
1	.5	76.7	1.06	62.8	-.514E-02
2	90.0	66.8	1.15	159.8	-.142E+01

AVERAGE BULK REYNOLDS 52481. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 44157. AVERAGE FRICTION FACTOR .00504

RUN 127H, DATE 03/01/76, GAS HE-AR, MOLECULAR WT. = 15.33  
 TIN = 73.2 P, TOUT = 510.4 P, MASS FLOW RATE = 14.1 LB/HR, I = 102.2 AMPS, E = 5.990 VOLTS  
 PR,IN = .419, GR/RESQ = .256E-03, MACH(2) = .112, MACH(16) = .156, T,SURR = 78.5 F

TC	X/D	TR (F)	TR/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HRFT2	Q+
2	.1	152.7	1.149	31735.	.074	184.51	29526.6	.002016
3	1.2	246.1	1.113	31502.	.146	80.63	56131.8	.001901
4	2.1	290.2	1.185	31316.	.046	71.05	6137.6	.002091
5	4.1	334.9	1.443	10885.	.029	61.06	62919.0	.002131
6	8.1	488.1	1.484	30094.	.027	53.20	61302.9	.002144
7	16.4	644.9	1.492	28608.	.027	46.97	61534.8	.002152
8	24.5	889.5	1.476	27325.	.029	43.95	61620.6	.002155
9	32.4	925.6	1.451	26210.	.031	42.31	61695.6	.002158
10	40.7	970.4	1.423	25151.	.034	41.16	61651.5	.002156
11	48.7	1015.1	1.399	24240.	.035	40.21	61739.0	.002159
12	56.8	1060.0	1.391	23383.	.041	37.65	61552.0	.002153
13	64.7	1104.6	1.367	22626.	.043	37.22	61530.9	.002154
14	73.0	1149.0	1.344	21909.	.047	36.90	61462.2	.002150
15	81.2	1193.8	1.321	21258.	.053	36.71	61232.0	.002142
16	89.9	1238.6	1.291	20629.	.090	47.92	51124.7	.002079
17	97.9	1283.7	1.106	20199.	.455	73.31	45405.6	.001538

PT	X/D	STATIC PRESS. (PSIA)	TR/TB	TB (F)	PRESS DEFECT
1	.5	92.7	1.12	72.8	-.588E-02
2	90.2	88.1	1.28	480.4	-.216E+01

AVERAGE BULK REYNOLDS 26198. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 19810. AVERAGE FRICTION FACTOR .00605



RUN 129H, DATE 03/01/76, GAS HE-A2, MOLECULAR WT. = 15.30  
 TIN = 74.1 F, TOUT = 688.6 F, MASS FLOW RATE = 14.1 LB/HR, I = 121.2 AMPS, Z = 7.280 VOLTS  
 PR,IN = .419, GR/RESQ = .355E-03, MACH(2) = .113, MACH(16) = .171, T, SURR = 31.5 F

TC	X/D	TW	TW/TB	BULK	HL/QGAS	BULK	QGAS	Q+
		(F)		REYNOLDS		NUSSELT	BTU/HRFT2	
2	.1	198.0	1.229	31682.	.082	163.34	833.33	.002816
3	1.2	226.6	1.453	31357.	.143	77.17	798.70	.002888
4	2.1	395.6	1.564	31095.	.051	67.10	870.37	.002940
5	4.1	469.0	1.559	30495.	.036	56.17	887.38	.002997
6	3.1	548.2	1.723	29427.	.014	47.83	898.61	.003021
7	16.4	647.6	1.735	27484.	.036	40.66	899.74	.003035
8	24.4	717.2	1.704	25876.	.040	37.13	899.73	.003039
9	32.4	771.0	1.660	24527.	.043	35.15	900.49	.003041
10	40.9	821.7	1.611	23266.	.048	33.63	899.39	.003037
11	48.7	867.3	1.567	22229.	.051	32.63	899.46	.003038
12	57.0	911.3	1.525	21293.	.056	31.84	897.11	.003032
13	65.0	945.9	1.480	20470.	.060	31.78	895.99	.003029
14	73.1	970.2	1.425	19694.	.061	32.82	897.44	.003030
15	81.3	1026.5	1.408	18974.	.074	31.14	889.44	.003034
16	90.4	1037.3	1.449	18330.	.117	32.38	855.89	.002890
17	98.4	848.1	1.139	17941.	.075	46.57	50360.7	.001701

PT	X/D	STATIC	TW/TB	TB	PRESS
		PRESS. (PSIA)		(F)	DEFECT
1	.5	92.7	1.18	74.4	-.588E-02
2	90.4	87.0	1.35	650.4	.290E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 25029. AVERAGE WALL REYNOLDS 17357. AVERAGE FRICTION FACTOR .00616

RUN 129H, DATE 03/01/76, GAS HE-A2, MOLECULAR WT. = 15.30  
 TIN = 75.4 F, TOUT = 306.3 F, MASS FLOW RATE = 24.4 LB/HR, I = 102.4 AMPS, Z = 5.925 VOLTS  
 PR,IN = .419, GR/RESQ = .609E-04, MACH(2) = .233, MACH(16) = .335, T, SURR = 82.0 F

TC	X/D	TW	TW/TB	BULK	HL/QGAS	BULK	QGAS	Q+
		(F)		REYNOLDS		NUSSELT	BTU/HRFT2	
2	.1	145.2	1.148	55262.	.079	204.06	59450.1	.001162
3	1.2	202.0	1.289	55020.	.096	113.76	53758.9	.001189
4	2.1	229.0	1.295	54830.	.026	101.31	53852.8	.001229
5	4.1	256.0	1.333	54396.	.018	88.79	63512.7	.001242
6	3.1	284.9	1.361	53582.	.015	79.42	63791.5	.001247
7	16.4	321.9	1.376	51992.	.015	71.72	63959.8	.001261
8	24.4	349.3	1.375	50553.	.016	61.93	64045.7	.001262
9	32.4	371.8	1.367	49261.	.017	65.87	64119.4	.001262
10	40.9	394.6	1.358	47980.	.018	64.05	64126.6	.001264
11	48.7	416.7	1.350	46841.	.019	62.36	64191.1	.001264
12	57.0	437.9	1.342	45765.	.020	61.05	64179.8	.001265
13	65.0	456.3	1.331	44778.	.021	60.53	64179.8	.001265
14	73.1	476.6	1.321	43798.	.023	59.33	64122.3	.001266
15	81.3	495.8	1.311	42908.	.026	57.71	64189.6	.001266
16	90.4	500.3	1.281	42019.	.042	59.21	64093.8	.001266
17	98.0	447.0	1.183	41340.	.194	62.50	63112.9	.001234
						86.43	54878.2	.001073

PT	X/D	STATIC	TW/TB	TB	PRESS
		PRESS. (PSIA)		(F)	DEFECT
1	.5	76.7	1.12	67.0	-.515E-02
2	90.1	63.3	1.28	289.7	.194E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 48657. AVERAGE WALL REYNOLDS 36411. AVERAGE FRICTION FACTOR .00516

RUN 130R, DATE 03/01/76, GAS HE-AR, MOLECULAR WT. = 15.33  
 T<sub>IN</sub> = 76.3 F, T<sub>OUT</sub> = 451.5 F, MASS FLOW RATE = 24.3 LB/HR, I = 126.0 AMPS, E = 7.440 VOLTS  
 PR,IN = .419, GR/RESQ = .143E-03, MACH(2) = .186, MACH(16) = .272, T<sub>SURR</sub> = 34.7 F

TC	X/D	T <sub>W</sub> (F)	T <sub>W</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR/FT <sup>2</sup>	Q*
2	.1	176.9	1.196	4594.	.074	219.25	90625.1	.001775
3	.2	209.7	1.360	3432.	.100	113.25	39109.7	.001747
4	.3	238.8	1.432	2942.	.130	93.83	95469.5	.001871
5	.4	264.4	1.489	2581.	.160	78.74	96646.5	.001894
6	.5	289.1	1.530	2269.	.190	68.53	97152.0	.001908
7	.6	314.6	1.545	1978.	.220	60.78	97522.1	.001912
8	.7	340.2	1.534	1770.	.250	54.48	97719.8	.001915
9	.8	365.9	1.514	1613.	.280	48.84	97982.1	.001913
10	.9	391.1	1.491	1432.	.310	43.65	97913.1	.001913
11	1.0	417.3	1.472	1258.	.340	38.74	98031.1	.001913
12	1.1	443.7	1.450	1096.	.370	34.49	98031.1	.001913
13	1.2	469.7	1.424	925.1	.400	30.18	98127.1	.001913
14	1.3	495.9	1.405	795.6	.430	26.06	98054.4	.001913
15	1.4	521.7	1.381	719.5	.460	22.19	97928.1	.001913
16	1.5	547.5	1.338	695.4	.490	18.62	96081.1	.001883
17	1.6	635.8	1.199	3620.1	.299	77.10	77413.0	.001517

PT	X/D	STATIC PRESS. (PSIA)	T <sub>W</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS DEFECT
1	.5	96.3	1.15	71.9	-.516E-02
2	90.2	84.1	1.34	426.8	.222E+01

AVERAGE BULK REYNOLDS 45799. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 32455. AVERAGE FRICTION FACTOR .00524

RUN 131R, DATE 03/01/76, GAS HE-AR, MOLECULAR WT. = 15.33  
 T<sub>IN</sub> = 76.8 F, T<sub>OUT</sub> = 623.6 F, MASS FLOW RATE = 24.2 LB/HR, I = 151.1 AMPS, E = 9.100 VOLTS  
 PR,IN = .419, GR/RESQ = .206E-03, MACH(2) = .186, MACH(16) = .305, T<sub>SURR</sub> = 37.0 F

TC	X/D	T <sub>W</sub> (F)	T <sub>W</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR/FT <sup>2</sup>	Q*
2	.1	216.8	1.268	5434.5	.067	228.80	131587.2	.002582
3	.2	354.1	1.509	3822.	.101	113.99	129787.5	.002527
4	.3	421.2	1.618	3404.	.133	98.69	138017.9	.002709
5	.4	489.8	1.707	3246.5	.164	84.12	139860.7	.002745
6	.5	563.7	1.767	3078.4	.194	72.77	140826.2	.002754
7	.6	658.6	1.783	2769.5	.224	62.50	141568.8	.002778
8	.7	725.6	1.758	2511.1	.254	54.26	141910.9	.002785
9	.8	779.4	1.722	2297.	.284	48.00	142163.9	.002790
10	.9	829.3	1.678	2088.8	.314	41.60	142237.3	.002791
11	1.0	879.3	1.640	1914.9	.344	36.69	142391.6	.002794
12	1.1	917.6	1.601	1760.3	.374	32.40	142387.7	.002794
13	1.2	955.6	1.556	1624.1	.404	28.16	142450.1	.002795
14	1.3	988.8	1.519	1494.6	.434	24.63	142406.5	.002795
15	1.4	1022.2	1.482	1380.1	.464	21.56	142263.1	.002793
16	1.5	1049.4	1.421	1264.9	.494	18.63	138833.6	.002725
17	1.6	981.1	1.237	3194.0	.504	61.94	97324.7	.001920

PT	X/D	STATIC PRESS. (PSIA)	T <sub>W</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS DEFECT
1	.5	96.3	1.21	73.1	-.517E-02
2	90.4	80.9	1.42	588.0	.280E+01

AVERAGE BULK REYNOLDS 43534. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 28483. AVERAGE FRICTION FACTOR .00526

RUN 133H, DATE 03/10/76, GAS HE, MOLECULAR WT. = 4.0026  
 TIN = 78.1 F, TOUT = 174.0 F, MASS FLOW RATE = 11.6 LB/HR, I = 87.1 AMPS, E = 4.925 VOLTS  
 PR,IN = .667, GR/RESQ = .112E-04, MACH(2) = .162, MACH(16) = .188, T, SUBR = 75.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT2	Q+
2	.1	99.5	1.048	30117.	.040	240.47	444.47	.000476
3	1.2	131.1	1.105	30065.	.072	95.70	4322.2	.000463
4	2.1	142.1	1.124	30036.	.114	45.18	4545.2	.000490
5	3.1	152.4	1.138	29936.	.162	35.53	4558.4	.000493
6	4.1	162.4	1.148	29785.	.008	69.88	4608.2	.000494
7	5.1	172.4	1.154	29425.	.008	64.99	4613.8	.000495
8	6.1	182.4	1.154	29100.	.008	61.20	4616.3	.000495
9	7.1	192.4	1.153	28791.	.008	62.70	4618.5	.000495
10	8.1	202.4	1.149	28476.	.008	62.70	4619.8	.000495
11	9.1	211.1	1.149	28184.	.009	61.46	4621.3	.000495
12	10.1	220.0	1.148	27894.	.009	60.91	4621.9	.000495
13	11.1	227.7	1.144	27616.	.009	60.94	4622.3	.000495
14	12.1	236.6	1.143	27337.	.010	60.09	4622.3	.000495
15	13.1	242.2	1.137	27070.	.011	61.24	4619.9	.000495
16	14.1	248.4	1.125	26791.	.018	66.07	4590.2	.000492
17	15.1	250.6	1.088	26556.	.064	91.05	4385.4	.000470

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	103.1	1.04	73.9	-.536E-02
2	90.0	96.3	1.12	166.8	.151E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 28457. AVERAGE WALL REYNOLDS 25098. AVERAGE FRICTION FACTOR .00622

RUN 134H, DATE 03/10/76, GAS HE, MOLECULAR WT. = 4.0026  
 TIN = 77.7 F, TOUT = 320.1 F, MASS FLOW RATE = 11.6 LB/HR, I = 135.4 AMPS, E = 7.390 VOLTS  
 PR,IN = .667, GR/RESQ = .272E-04, MACH(2) = .162, MACH(16) = .211, T, SUBR = 78.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT2	Q+
2	.1	142.6	1.129	30140.	.051	192.97	10672.1	.0011143
3	1.2	211.1	1.250	30016.	.063	92.70	10602.4	.0011135
4	2.1	238.1	1.295	29919.	.016	84.70	11114.2	.0011190
5	3.1	263.0	1.328	29705.	.011	73.62	11191.7	.0011138
6	4.1	289.3	1.351	29303.	.009	66.50	11227.7	.0011102
7	5.1	322.0	1.360	28516.	.009	61.00	11236.5	.0011106
8	6.1	346.7	1.354	27799.	.009	58.80	11274.1	.0011107
9	7.1	366.9	1.343	27188.	.010	57.50	11288.1	.0011108
10	8.1	386.1	1.328	26497.	.010	56.92	11296.6	.0011109
11	9.1	407.8	1.321	25914.	.011	55.67	11309.7	.0011111
12	10.1	427.7	1.310	25358.	.012	54.63	11319.7	.0011111
13	11.1	444.8	1.297	24841.	.012	54.52	11326.4	.0011111
14	12.1	464.7	1.287	24327.	.013	53.92	11329.5	.0011111
15	13.1	481.9	1.274	23854.	.015	53.99	11327.1	.0011111
16	14.1	483.6	1.240	23340.	.023	58.76	11237.9	.0011203
17	15.1	452.4	1.169	22896.	.119	74.49	10246.2	.0011047

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	103.3	1.10	74.1	-.536E-02
2	90.1	94.2	1.24	301.4	.199E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 26749. AVERAGE WALL REYNOLDS 20976. AVERAGE FRICTION FACTOR .00634

RUN 135H, DATE 03/10/76, GAS H<sub>2</sub>, MOLECULAR WT. = 4.0026  
 T<sub>IN</sub> = 77.7 F, T<sub>OUT</sub> = 47.7 F, MASS FLOW RATE = 11.6 LB/HR, I = 171.2 AMPS, E = 10.170 VOLTS  
 PR,IN = .667, GR/RESQ = .435E-04, NACH(2) = .163, NACH(16) = .235, T, SURR = 32.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT <sup>2</sup>	Q*
2	.1	190.3	1.215	300091.	.055	178.442	170678.3	.001827
3	1.2	230.3	1.398	29894.	.061	31.306	170966.3	.001830
4	2.1	338.5	1.471	29741.	.017	91.300	178844.3	.001915
5	4.1	379.5	1.523	29402.	.012	122.300	180275.3	.001930
6	8.1	423.6	1.557	28772.	.011	166.300	181742.3	.001938
7	16.4	479.8	1.563	27586.	.011	230.300	182174.3	.001946
8	24.6	520.2	1.545	26536.	.012	300.300	182624.3	.001950
9	32.5	552.4	1.518	25616.	.012	393.300	182624.3	.001954
10	40.9	583.9	1.483	24399.	.012	500.300	183059.3	.001956
11	48.3	648.0	1.467	23394.	.013	649.300	183324.3	.001962
12	55.0	703.3	1.413	22484.	.015	849.300	183324.3	.001964
13	65.0	733.2	1.396	21861.	.017	1099.300	183324.3	.001969
14	73.4	728.5	1.371	21295.	.019	1415.300	183324.3	.001971
15	81.6	731.1	1.321	20735.	.028	1833.300	181637.3	.001947
16	90.4	680.5	1.224	20303.	.183	64.29	157443.3	.001686

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	103.1	1.16	74.7	-.596E-02
2	90.3	91.6	1.32	442.3	.253E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 25428. AVERAGE WALL REYNOLDS 18139. AVERAGE FRICTION FACTOR .00652

RUN 136H, DATE 03/10/76, GAS H<sub>2</sub>, MOLECULAR WT. = 4.0026  
 T<sub>IN</sub> = 76.8 F, T<sub>OUT</sub> = 618.7 F, MASS FLOW RATE = 11.6 LB/HR, I = 199.6 AMPS, E = 12.015 VOLTS  
 PR,IN = .667, GR/RESQ = .598E-04, NACH(2) = .162, NACH(16) = .258, T, SURR = 36.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/QGAS	BULK NUSSELT	QGAS BTU/HR FT <sup>2</sup>	Q*
2	.1	230.2	1.289	30055.	.050	179.34	21338.9	.002510
3	1.2	369.2	1.533	29786.	.060	94.75	21338.9	.002511
4	2.1	434.9	1.640	29578.	.019	81.37	24484.9	.002525
5	4.1	493.7	1.711	29117.	.013	70.94	24484.9	.002549
6	8.1	559.9	1.760	28281.	.013	62.43	24484.9	.002562
7	16.4	642.3	1.760	26735.	.013	55.00	24484.9	.002577
8	24.6	699.2	1.725	25427.	.014	51.41	25002.9	.002586
9	32.5	744.2	1.682	24303.	.015	49.27	25002.9	.002592
10	40.9	787.0	1.633	23201.	.016	47.77	25112.9	.002596
11	48.3	829.0	1.594	22265.	.017	46.40	25112.9	.002601
12	55.0	867.2	1.554	21460.	.018	45.68	25112.9	.002605
13	65.0	899.8	1.513	20737.	.019	45.58	25223.9	.002608
14	73.4	938.4	1.479	20042.	.021	45.15	25223.9	.002611
15	81.6	977.9	1.446	19419.	.024	45.11	25223.9	.002617
16	90.4	977.2	1.382	18413.	.035	48.57	24977.0	.002681
17	93.4	997.4	1.258	18368.	.260	57.04	204094.9	.0022191

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DEFECT
1	.5	103.2	1.22	74.5	-.596E-02
2	90.4	89.2	1.38	579.3	.309E+01

AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE BULK REYNOLDS 24454. AVERAGE WALL REYNOLDS 16195. AVERAGE FRICTION FACTOR .00669

RUN 1494, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 29.97  
 TIN = 74.5 F, TOUT = 153.5 F, MASS FLOW RATE = 35.6 LB/MR, I = 64.244PS, E = 3.555 VOLTS  
 PR.IN = .72C, GR/RESO = .162E-03, MACH(2) = .225, MACH(16) = .250, T-SURR = 75.7 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/2GAS	BULK NUSSLEIT	2TC/4RFT2	Q+
2	.1	103.3	1.064	100225	.074	530.0	2333.0	.000417
3	.2	137.0	1.126	100098	.145	224.0	2100.0	.000332
4	.3	143.0	1.148	39947	.031	223.0	244.0	.000336
5	.4	160.9	1.164	39657	.019	204.0	247.0	.000441
6	.5	171.1	1.176	33137	.015	193.0	246.0	.000443
7	.6	183.0	1.189	30056	.015	175.0	246.0	.000444
8	.7	195.9	1.198	97025	.015	153.0	246.0	.000444
9	.8	203.3	1.186	96050	.015	158.0	246.0	.000445
10	.9	211.1	1.183	93284	.016	153.0	246.0	.000444
11	.1	220.2	1.183	94151	.016	150.0	246.0	.000445
12	.2	223.3	1.183	93284	.017	157.0	246.0	.000444
13	.3	233.5	1.180	92382	.016	153.0	246.0	.000444
14	.4	242.7	1.174	91449	.016	153.0	246.0	.000444
15	.5	249.9	1.175	90324	.022	156.0	246.0	.000443
16	.6	256.8	1.175	89740	.033	166.0	246.0	.000443
17	.7	262.1	1.186	89022	.092	304.0	2317.0	.000443

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DIFF. (PSI)
1	.5	92.1	1.05	60.6	-0.45
2	90.0	84.4	1.16	151.7	-0.17

AVERAGE BULK REYNOLDS 94992. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 80621. AVERAGE FRICTION FACTOR .00451

RUN 1504, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 29.97  
 TIN = 75.9 F, TOUT = 235.5 F, MASS FLOW RATE = 35.4 LB/MR, I = 69.144PS, E = 5.720 VOLTS  
 PR.IN = .72C, GR/RESO = .386E-03, MACH(2) = .224, MACH(16) = .293, T-SURR = 79.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/2GAS	BULK NUSSLEIT	2TC/4RFT2	Q+
2	.1	151.5	1.150	39494	.092	204.0	3501.0	.000493
3	.2	230.0	1.203	33120	.137	240.0	3314.0	.000493
4	.3	295.0	1.204	28227	.341	215.0	3274.0	.000493
5	.4	305.0	1.204	33164	.005	191.0	3274.0	.000493
6	.5	337.9	1.204	34418	.001	174.0	3274.0	.000493
7	.6	333.5	1.204	34448	.003	163.0	3274.0	.000493
8	.7	337.9	1.204	32278	.020	152.0	3274.0	.000493
9	.8	338.8	1.204	30227	.020	143.0	3274.0	.000493
10	.9	413.1	1.204	33145	.022	143.0	3274.0	.000493
11	.1	437.7	1.204	36299	.022	140.0	3274.0	.000493
12	.2	455.0	1.204	34540	.024	139.0	3274.0	.000493
13	.3	470.9	1.204	32926	.024	135.0	3274.0	.000493
14	.4	485.6	1.204	31338	.026	134.0	3274.0	.000493
15	.5	502.0	1.204	33850	.029	133.0	3274.0	.000493
16	.6	501.8	1.204	73341	.047	139.0	3274.0	.000493
17	.7	508.5	1.163	77201	.166	244.0	3251.0	.000493

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PRESS DIFF. (PSI)
1	.5	92.1	1.12	71.5	-0.65
2	90.1	82.0	1.33	270.7	-0.15

AVERAGE BULK REYNOLDS 88342. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 65447. AVERAGE FRICTION FACTOR .00452

RUN 1514, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 77.2 F, TOUT = 404.9 F, MASS FLOW RATE = 35.3 LB/HR, I = 122.7 AMP, E = 7.260 VOLTS  
 PR. IN = .720, GR/RESO = .589E-03, MACH(2) = .224, MACH(16) = .324, T. SURR = 32.0 F

TC	X/D	T <sub>1</sub> (F)	TW/TB	BULK REYNOLDS	HL/CGAS	BULK NUSSELT	CGAS BTU/HRFT <sup>2</sup>	Q+
2	.1	107.9	1.233	98836.	.100	482.0	339.9	.0019
3	.2	132.0	1.453	93806.	.161	233.0	117.6	.0015
4	.3	173.3	1.344	97806.	.061	211.3	146.3	.0016
5	.4	222.3	1.013	46803.	.023	185.7	112.3	.0013
6	.5	268.8	1.033	44937.	.023	166.8	110.7	.0013
7	.6	322.3	1.060	41413.	.023	143.4	92.3	.0013
8	.7	380.0	1.090	35599.	.023	133.3	92.7	.0013
9	.8	400.0	1.090	32063.	.023	133.3	92.7	.0013
10	.9	400.0	1.090	30314.	.023	133.3	92.7	.0013
11	1.0	400.0	1.090	27308.	.023	117.0	92.7	.0013
12	1.1	400.0	1.090	73001.	.023	117.0	92.7	.0013
13	1.2	400.0	1.090	74301.	.023	114.4	92.7	.0013
14	1.3	400.0	1.090	72334.	.023	114.4	92.7	.0013
15	1.4	400.0	1.090	70338.	.023	114.4	92.7	.0013
16	1.5	400.0	1.090	59364.	.023	114.4	92.7	.0013
17	1.6	400.0	1.090	59364.	.023	114.4	92.7	.0013

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	DETECT
1	.5	91.9	1.13	73.3	.001
2	90.3	79.3	1.44	381.5	.001

AVERAGE BULK REYNOLDS 84755. AVERAGE WALL REYNOLDS 55947. AVERAGE FRICTION FACTOR .00462

RUN 1524, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 77.7 F, TOUT = 527.6 F, MASS FLOW RATE = 35.2 LB/HR, I = 143.2 AMP, E = 8.635 VOLTS  
 PR. IN = .719, GR/RESO = .806E-03, MACH(2) = .223, MACH(16) = .354, T. SURR = 67.0 F

TC	X/D	T <sub>1</sub> (F)	TW/TB	BULK REYNOLDS	HL/CGAS	BULK NUSSELT	CGAS BTU/HRFT <sup>2</sup>	Q+
2	.1	247.4	1.322	39212.	.098	469.4	1151.4	.0020
3	.2	413.8	1.514	37433.	.141	233.0	1120.6	.0020
4	.3	483.3	1.747	36817.	.064	207.5	1332.0	.0021
5	.4	559.5	1.843	35422.	.033	180.0	1332.0	.0021
6	.5	623.4	1.902	33390.	.029	159.3	1332.0	.0021
7	.6	709.9	1.911	33346.	.029	140.1	1332.0	.0021
8	.7	766.6	1.885	30830.	.032	129.1	1270.8	.0021
9	.8	811.1	1.848	30833.	.032	122.2	1272.7	.0021
10	.9	853.5	1.807	27883.	.036	115.6	1272.7	.0021
11	1.0	893.2	1.770	26436.	.038	110.8	1272.7	.0021
12	1.1	932.7	1.732	22383.	.041	107.3	1272.7	.0021
13	1.2	961.0	1.689	20357.	.043	105.4	1272.7	.0021
14	1.3	994.1	1.652	17495.	.046	102.7	1272.7	.0021
15	1.4	1015.1	1.507	16031.	.050	102.7	1272.7	.0021
16	1.5	1009.6	1.535	14208.	.057	103.4	1272.7	.0021
17	1.6	790.8	1.266	52993.	.405	159.4	434.0	.0017

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	DETECT
1	.5	91.9	1.25	74.3	.002
2	90.4	76.7	1.53	497.7	.001

AVERAGE BULK REYNOLDS 81264. AVERAGE WALL REYNOLDS 48907. AVERAGE FRICTION FACTOR .00453

RUN 1544, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 29.07  
 TIN = 77.7 F, TOUT = 171.2 F, MASS FLOW RATE = 29.3 LB/HR, I = 35.5 AIPS, E = 3.260 VOLTS  
 PR, IN = .719, GR/RESO = .239E-03, MACH(2) = .170, MACH(16) = .185, T, SUP = 32.0 F

TC	X/D	T <sub>4</sub> (F)	T <sub>w</sub> /T <sub>8</sub>	BULK REYNOLDS	HL/OGAS	BULK NUSSLELT	OGAS BTU/HRFT <sup>2</sup>	Q+
2	.1	109.1	1.063	3110	.083	441	2017	.000437
3	.2	141.8	1.123	3105	.100	231	3729	.000437
4	.4	158.7	1.145	3092	.094	172	4983	.000437
5	.6	170.1	1.174	3068	.092	129	6419	.000437
7	.8	190.1	1.181	3023	.091	101	8223	.000437
9	1.0	201.1	1.132	7423	.017	143	9456	.000437
11	1.2	224.5	1.180	7575	.017	117	10777	.000437
13	1.4	227.7	1.179	7548	.019	113	10760	.000437
14	1.5	233.3	1.177	7518	.020	113	10760	.000437
15	1.6	243.3	1.174	7444	.021	112	10760	.000437
16	1.7	251.1	1.172	7366	.022	110	10760	.000437
17	1.8	253.3	1.168	7291	.026	110	10760	.000437
18	1.9	259.3	1.153	7215	.042	117	10760	.000437
19	2.0	220.1	1.077	7152	.109	261	10760	.000431

PT	X/D	STATIC PRESS. (PSIA)	T <sub>w</sub> /T <sub>8</sub>	T <sub>8</sub> (F)	PRESS DIFF. (PSIA)
1	.5	99.9	1.05	75.0	-0.47
2	90.0	95.2	1.15	163.8	-0.11

AVERAGE BULK REYNOLDS 76666. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 69395. AVERAGE FRICTION FACTOR .00459

RUN 1554, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 29.07  
 TIN = 76.6 F, TOUT = 238.5 F, MASS FLOW RATE = 29.1 LB/HR, I = 90.6 AIPS, E = 5.220 VOLTS  
 PR, IN = .719, GR/RESO = .544E-03, MACH(2) = .170, MACH(16) = .212, T, SUP = 33.0 F

TC	X/D	T <sub>4</sub> (F)	T <sub>w</sub> /T <sub>8</sub>	BULK REYNOLDS	HL/OGAS	BULK NUSSLELT	OGAS BTU/HRFT <sup>2</sup>	Q+
2	.1	191.4	1.139	4106	.099	432	4567	.000990
3	.2	225.4	1.274	8076	.156	204	6744	.000990
4	.4	262.4	1.336	8051	.051	182	9711	.000990
5	.6	293.0	1.381	7997	.029	161	10000	.000990
7	.8	321.3	1.409	7893	.024	146	10433	.000990
9	1.0	354.2	1.420	7694	.023	134	10760	.000990
11	1.2	373.0	1.415	7510	.023	124	10760	.000990
13	1.4	397.7	1.405	7339	.023	120	10760	.000990
15	1.6	413.3	1.396	7166	.025	117	10760	.000990
17	1.8	437.7	1.386	7015	.026	114	10760	.000990
19	2.0	457.7	1.376	6866	.028	114	10760	.000990
21	2.2	471.0	1.360	6738	.031	112	10760	.000990
23	2.4	489.4	1.349	6609	.034	111	10760	.000990
25	2.6	503.2	1.334	6483	.038	111	10760	.000990
27	2.8	506.0	1.302	6357	.044	114	10760	.000990
29	3.0	403.0	1.140	6265	.169	216	10760	.000990

PT	X/D	STATIC PRESS. (PSIA)	T <sub>w</sub> /T <sub>8</sub>	T <sub>8</sub> (F)	PRESS DIFF. (PSIA)
1	.5	99.9	1.11	76.6	-0.47
2	90.1	93.7	1.30	262.0	-0.15

AVERAGE BULK REYNOLDS 72340. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 54080. AVERAGE FRICTION FACTOR .00475

RUN 1564, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 79.0 F, TOUT = 423.3 F, MASS FLOW RATE = 29.0 LB/HR, I = 112.3 A, E = 6.665 VOLTS  
 PR. IN = .719, GR/RESQ = .542E-03, MACH(2) = .170, MACH(10) = .231, T. SURF = 92.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/GAS	BULK NUSSELT	GAS BTU/HR FT <sup>2</sup>	Q+
2	.1	105.2	1.213	30768.	.108	413.54	70446.6	.001529
1	.2	312.7	1.633	30207.	.161	200.53	47435.3	.001471
4	.4	383.3	1.522	74623.	.050	193.37	75253.7	.001633
6	.6	477.3	1.541	74074.	.033	134.31	76617.0	.001566
8	.8	549.5	1.634	77528.	.029	141.55	77402.1	.001679
10	1.0	609.0	1.665	74557.	.023	127.21	77745.0	.001684
12	1.2	666.9	1.532	71532.	.029	113.86	77376.0	.001639
14	1.4	722.3	1.568	69723.	.030	114.18	75002.3	.001642
16	1.6	783.3	1.533	63313.	.033	104.49	77460.9	.001643
18	1.8	833.3	1.501	53313.	.033	100.14	75061.0	.001643
20	2.0	883.3	1.533	43338.	.036	102.50	77483.6	.001642
22	2.2	933.3	1.500	33370.	.037	101.60	75046.2	.001643
24	2.4	983.3	1.484	23134.	.040	99.82	77445.7	.001643
26	2.6	1033.3	1.456	13357.	.044	96.44	77760.6	.001647
28	2.8	1083.3	1.427	8335.	.047	92.21	75046.2	.001647
30	3.0	1133.3	1.398	3333.	.049	88.36	73490.3	.001647
32	3.2	1183.3	1.369	3333.	.051	84.22	71934.4	.001647
34	3.4	1233.3	1.340	3333.	.051	80.08	70378.5	.001647
36	3.6	1283.3	1.311	3333.	.051	75.94	68822.6	.001647
38	3.8	1333.3	1.282	3333.	.051	71.80	67266.7	.001647
40	4.0	1383.3	1.253	3333.	.051	67.66	65710.8	.001647
42	4.2	1433.3	1.224	3333.	.051	63.52	64154.9	.001647
44	4.4	1483.3	1.195	3333.	.051	59.38	62599.0	.001647
46	4.6	1533.3	1.166	3333.	.051	55.24	61043.1	.001647
48	4.8	1583.3	1.137	3333.	.051	51.10	59487.2	.001647
50	5.0	1633.3	1.108	3333.	.051	46.96	57931.3	.001647
52	5.2	1683.3	1.079	3333.	.051	42.82	56375.4	.001647
54	5.4	1733.3	1.050	3333.	.051	38.68	54819.5	.001647
56	5.6	1783.3	1.021	3333.	.051	34.54	53263.6	.001647
58	5.8	1833.3	0.992	3333.	.051	30.40	51707.7	.001647
60	6.0	1883.3	0.963	3333.	.051	26.26	50151.8	.001647
62	6.2	1933.3	0.934	3333.	.051	22.12	48595.9	.001647
64	6.4	1983.3	0.905	3333.	.051	17.98	47040.0	.001647
66	6.6	2033.3	0.876	3333.	.051	13.84	45484.1	.001647
68	6.8	2083.3	0.847	3333.	.051	9.70	43928.2	.001647
70	7.0	2133.3	0.818	3333.	.051	5.56	42372.3	.001647
72	7.2	2183.3	0.789	3333.	.051	1.42	40816.4	.001647
74	7.4	2233.3	0.760	3333.	.051	0.28	39260.5	.001647
76	7.6	2283.3	0.731	3333.	.051	0.14	37704.6	.001647
78	7.8	2333.3	0.702	3333.	.051	0.00	36148.7	.001647
80	8.0	2383.3	0.673	3333.	.051	0.00	34592.8	.001647
82	8.2	2433.3	0.644	3333.	.051	0.00	33036.9	.001647
84	8.4	2483.3	0.615	3333.	.051	0.00	31481.0	.001647
86	8.6	2533.3	0.586	3333.	.051	0.00	29925.1	.001647
88	8.8	2583.3	0.557	3333.	.051	0.00	28369.2	.001647
90	9.0	2633.3	0.528	3333.	.051	0.00	26813.3	.001647
92	9.2	2683.3	0.499	3333.	.051	0.00	25257.4	.001647
94	9.4	2733.3	0.470	3333.	.051	0.00	23701.5	.001647
96	9.6	2783.3	0.441	3333.	.051	0.00	22145.6	.001647
98	9.8	2833.3	0.412	3333.	.051	0.00	20589.7	.001647
100	10.0	2883.3	0.383	3333.	.051	0.00	19033.8	.001647
102	10.2	2933.3	0.354	3333.	.051	0.00	17477.9	.001647
104	10.4	2983.3	0.325	3333.	.051	0.00	15922.0	.001647
106	10.6	3033.3	0.296	3333.	.051	0.00	14366.1	.001647
108	10.8	3083.3	0.267	3333.	.051	0.00	12810.2	.001647
110	11.0	3133.3	0.238	3333.	.051	0.00	11254.3	.001647
112	11.2	3183.3	0.209	3333.	.051	0.00	9698.4	.001647
114	11.4	3233.3	0.180	3333.	.051	0.00	8142.5	.001647
116	11.6	3283.3	0.151	3333.	.051	0.00	6586.6	.001647
118	11.8	3333.3	0.122	3333.	.051	0.00	5030.7	.001647
120	12.0	3383.3	0.093	3333.	.051	0.00	3474.8	.001647
122	12.2	3433.3	0.064	3333.	.051	0.00	1918.9	.001647
124	12.4	3483.3	0.035	3333.	.051	0.00	363.0	.001647
126	12.6	3533.3	0.006	3333.	.051	0.00	0.00	.001647
128	12.8	3583.3	0.000	3333.	.051	0.00	0.00	.001647
130	13.0	3633.3	0.000	3333.	.051	0.00	0.00	.001647
132	13.2	3683.3	0.000	3333.	.051	0.00	0.00	.001647
134	13.4	3733.3	0.000	3333.	.051	0.00	0.00	.001647
136	13.6	3783.3	0.000	3333.	.051	0.00	0.00	.001647
138	13.8	3833.3	0.000	3333.	.051	0.00	0.00	.001647
140	14.0	3883.3	0.000	3333.	.051	0.00	0.00	.001647
142	14.2	3933.3	0.000	3333.	.051	0.00	0.00	.001647
144	14.4	3983.3	0.000	3333.	.051	0.00	0.00	.001647
146	14.6	4033.3	0.000	3333.	.051	0.00	0.00	.001647
148	14.8	4083.3	0.000	3333.	.051	0.00	0.00	.001647
150	15.0	4133.3	0.000	3333.	.051	0.00	0.00	.001647

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TS (F)	PRESS DIFF. (PSI)
1	.5	90.7	1.17	77.3	.47
2	90.3	92.1	1.40	149.4	1.16

AVERAGE BULK REYNOLDS 69032. AVERAGE WALL REYNOLDS 46754. AVERAGE FRICTION FACTOR .00479

RUN 1574, DATE 04/02/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 79.5 F, TOUT = 553.5 F, MASS FLOW RATE = 28.9 LB/HR, I = 132.2 A, E = 7.960 VOLTS  
 PR. IN = .719, GR/RESQ = .116E-02, MACH(2) = .170, MACH(10) = .250, T. SURF = 88.7 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/GAS	BULK NUSSELT	GAS BTU/HR FT <sup>2</sup>	Q+
2	.1	243.2	1.305	30324.	.109	408.61	37116.6	.002112
1	.2	401.4	1.584	73677.	.161	200.50	33379.3	.002038
4	.4	479.5	1.715	73162.	.051	179.87	13417.9	.002006
6	.6	549.2	1.809	74001.	.037	156.22	10500.2	.002006
8	.8	619.3	1.863	74053.	.033	135.27	10702.3	.002006
10	1.0	689.8	1.865	72030.	.036	121.73	10752.3	.002006
12	1.2	749.5	1.834	53674.	.033	112.42	10777.1	.002006
14	1.4	792.6	1.792	53646.	.037	107.22	10794.8	.002006
16	1.6	834.9	1.749	53119.	.041	101.60	10788.3	.002006
18	1.8	877.1	1.708	60837.	.043	97.47	10788.3	.002006
20	2.0	903.6	1.667	53173.	.046	93.21	10788.3	.002006
22	2.2	933.3	1.619	56839.	.047	84.22	10788.3	.002006
24	2.4	963.3	1.581	55036.	.051	75.94	10777.1	.002006
26	2.6	993.3	1.543	53430.	.056	67.66	10777.1	.002006
28	2.8	1023.3	1.479	51888.	.088	43.62	10777.1	.002006
30	3.0	1053.3	1.407	50863.	.443	153.42	77331.0	.002006

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TS (F)	PRESS DIFF. (PSI)
1	.5	90.5	1.24	78.3	.47
2	90.4	90.6	1.43	233.8	1.22

AVERAGE BULK REYNOLDS 66150. AVERAGE WALL REYNOLDS 41168. AVERAGE FRICTION FACTOR .00479



RUN 159H, DATE 04/05/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 73.7 F, TOUT = 175.5 F, MASS FLOW RATE = 20.1 LB/HR, I = 52.2 A, E = 2.33C VOLTS  
 PR.IN = .72C, GR/RESS = .214E-33, MACH(2) = .157, MACH(10) = .174, T, SUR = 76.0 F

TC	X/D	T4 (F)	TW/TB	BULK REYNOLDS	HL/2GAS	BULK NUSSELT	2GAS STU/HR FT2	Q+
2	.1	103.0	1.160	55552.0	.106	3451.6	3425.2	.001083
3	.2	135.9	1.110	50645.6	.200	3451.6	3425.2	.001111
4	.4	151.6	1.110	50645.6	.400	3451.6	3425.2	.001161
5	.6	163.6	1.110	50645.6	.600	3451.6	3425.2	.001177
6	.8	177.3	1.110	50645.6	.800	3451.6	3425.2	.001189
7	1.0	192.3	1.110	50645.6	1.000	3451.6	3425.2	.001193
8	1.2	203.2	1.110	50645.6	1.200	3451.6	3425.2	.001196
9	1.4	222.2	1.110	50645.6	1.400	3451.6	3425.2	.001196
10	1.6	232.2	1.110	50645.6	1.600	3451.6	3425.2	.001196
11	1.8	240.7	1.110	50645.6	1.800	3451.6	3425.2	.001196
12	2.0	243.3	1.110	50645.6	2.000	3451.6	3425.2	.001196
13	2.2	253.7	1.110	50645.6	2.200	3451.6	3425.2	.001196
14	2.4	263.3	1.110	50645.6	2.400	3451.6	3425.2	.001196
15	2.6	266.8	1.110	50645.6	2.600	3451.6	3425.2	.001196
16	2.8	266.8	1.110	50645.6	2.800	3451.6	3425.2	.001196
17	3.0	215.0	1.110	44284.4	3.000	2477.1	3123.3	.001196

PT X/D STATIC PRESS. (PSIA) TW/TB TB (F) PRESS. DIFF. (PSI) T, SUR  
 1 .5 74.5 1.05 71.5  
 2 .0 90.0 1.15 248.5

AVERAGE BULK REYNOLDS 53146. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 45344. AVERAGE FRICTION FACTOR .00509

RUN 160H, DATE 04/08/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 74.5 F, TOUT = 315.2 F, MASS FLOW RATE = 20.1 LB/HR, I = 79.2 A, E = 4.49C VOLTS  
 PR.IN = .720, GR/RESS = .491E-33, MACH(2) = .157, MACH(10) = .198, T, SUR = 76.0 F

TC	X/D	T4 (F)	TW/TB	BULK REYNOLDS	HL/2GAS	BULK NUSSELT	2GAS STU/HR FT2	Q+
2	.1	144.6	1.134	56288.8	.119	340.8	3425.2	.001083
3	.2	219.3	1.126	56003.3	.205	340.8	3425.2	.001111
4	.4	250.1	1.133	55882.2	.407	340.8	3425.2	.001161
5	.6	292.2	1.133	55464.4	.604	340.8	3425.2	.001177
6	.8	322.2	1.133	54673.3	.803	340.8	3425.2	.001189
7	1.0	353.3	1.133	53151.1	1.002	340.8	3425.2	.001193
8	1.2	384.4	1.133	51753.3	1.202	340.8	3425.2	.001196
9	1.4	404.4	1.133	50471.1	1.403	340.8	3425.2	.001196
10	1.6	425.1	1.133	49135.5	1.603	340.8	3425.2	.001196
11	1.8	446.6	1.133	47800.0	1.803	340.8	3425.2	.001196
12	2.0	466.6	1.133	46464.4	2.003	340.8	3425.2	.001196
13	2.2	486.6	1.133	45128.8	2.203	340.8	3425.2	.001196
14	2.4	506.6	1.133	43793.3	2.403	340.8	3425.2	.001196
15	2.6	526.6	1.133	42457.7	2.603	340.8	3425.2	.001196
16	2.8	546.6	1.133	41122.2	2.803	340.8	3425.2	.001196
17	3.0	400.0	1.133	43259.4	3.003	147.0	3123.3	.001196

PT X/D STATIC PRESS. (PSIA) TW/TB TB (F) PRESS. DIFF. (PSI) T, SUR  
 1 .5 74.5 1.11 72.4  
 2 .0 90.1 1.29 248.5

AVERAGE BULK REYNOLDS 49783. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 37493. AVERAGE FRICTION FACTOR .00513

RUN 1514, DATE 04/08/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 75.4 F, TOUT = 443.3 F, MASS FLOW RATE = 20.0 LB/HR, I = 97.6 A, E = 5.725 VOLTS  
 PR. IN = .720, GR/RESQ = .753E-03, MACH(2) = .156, MACH(10) = .214, T. SUR = 30.3 F

TC	X/D	T <sub>w</sub> (F)	TW/TS	BULK REYNOLDS	HL/GAS	BULK NUSSELT	GGAS BTU/HR FT <sup>2</sup>	Q+
2	.1	238.3	1.213	333800.	.138	3155.0	5134.0	.001227
3	.2	299.3	1.410	333800.	.138	1532.0	4629.0	.001244
4	.3	337.7	1.586	333800.	.138	1335.0	3527.0	.001231
5	.4	411.1	1.980	333800.	.138	1135.0	3073.0	.001246
6	.5	460.0	1.980	333800.	.138	1066.0	3733.0	.001288
7	.6	533.3	1.980	333800.	.138	944.0	3766.0	.001285
8	.7	594.4	1.980	333800.	.138	833.0	3766.0	.001285
9	.8	622.2	1.980	333800.	.138	777.0	3766.0	.001285
10	.9	655.5	1.980	333800.	.138	711.0	3766.0	.001285
11	1.0	688.8	1.980	333800.	.138	644.0	3766.0	.001285
12	1.1	722.2	1.980	333800.	.138	577.0	3766.0	.001285
13	1.2	755.5	1.980	333800.	.138	511.0	3766.0	.001285
14	1.3	788.8	1.980	333800.	.138	444.0	3766.0	.001285
15	1.4	822.2	1.980	333800.	.138	377.0	3766.0	.001285
16	1.5	855.5	1.980	333800.	.138	311.0	3766.0	.001285
17	1.6	888.8	1.980	333800.	.138	244.0	3766.0	.001285
18	1.7	922.2	1.980	333800.	.138	177.0	3766.0	.001285
19	1.8	955.5	1.980	333800.	.138	111.0	3766.0	.001285
20	1.9	988.8	1.980	333800.	.138	44.0	3766.0	.001285

PT	X/D	STATIC PRESS. (PSIA)	TW/TS	T <sub>B</sub> (F)	PERCENT DEFECT
1	.5	76.7	1.17	74.3	.02
2	90.3	69.5	1.34	419.8	.01

AVERAGE BULK REYNOLDS 47355. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 32532. AVERAGE FRICTION FACTOR .00525

RUN 1624, DATE 04/08/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 76.8 F, TOUT = 536.5 F, MASS FLOW RATE = 20.0 LB/HR, I = 114.8 A, E = 6.390 VOLTS  
 PR. IN = .719, GR/RESQ = .103E-02, MACH(2) = .157, MACH(10) = .234, T. SUR = 34.7 F

TC	X/D	T <sub>w</sub> (F)	TW/TS	BULK REYNOLDS	HL/GAS	BULK NUSSELT	GGAS BTU/HR FT <sup>2</sup>	Q+
2	.1	235.8	1.298	53787.	.138	338.3	7131.0	.002251
3	.2	383.5	1.366	53319.	.208	151.0	3784.0	.002143
4	.3	470.7	1.704	54440.	.072	135.0	7648.0	.002330
5	.4	549.7	1.813	54073.	.553	115.0	7883.0	.002649
6	.5	624.9	1.875	52541.	.546	101.0	7974.0	.002817
7	.6	710.4	1.945	49627.	.347	88.0	3014.0	.003331
8	.7	770.3	1.945	47167.	.350	81.0	3022.0	.003322
9	.8	815.8	1.799	45112.	.063	76.0	3022.0	.003322
10	.9	850.0	1.751	43155.	.058	72.0	3014.0	.003322
11	1.0	884.1	1.705	41502.	.061	70.0	3014.0	.003322
12	1.1	918.2	1.661	40009.	.063	63.0	3014.0	.003322
13	1.2	952.3	1.613	38674.	.064	53.0	7044.0	.003322
14	1.3	986.4	1.570	37336.	.073	56.0	7044.0	.003322
15	1.4	1020.5	1.527	36020.	.081	55.0	7044.0	.003322
16	1.5	1054.6	1.484	34724.	.126	57.0	7508.0	.003322
17	1.6	1088.7	1.439	33429.	.522	131.0	5127.0	.001637

PT	X/D	STATIC PRESS. (PSIA)	TW/TS	T <sub>B</sub> (F)	PERCENT DEFECT
1	.5	74.6	1.24	75.2	.02
2	90.4	64.3	1.45	553.9	.01

AVERAGE BULK REYNOLDS 45515. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 28654. AVERAGE FRICTION FACTOR .00530

RUN 163H, DATE 04/08/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 76.8 F, TCUT = 345.4 F, MASS FLOW RATE = 11.3 LB/HR, I = 64.4 AMPS, E = 3.635 VOLTS  
 PR. IN = .719, GR/RESS = .572E-03, MACH(2) = .116, MACH(16) = .145, T. SURR = 93.0 F

TC	X/D	T <sub>W</sub> (F)	T <sub>W</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/2GAS	BULK NUSSELT	2GAS BTU/HR FT <sup>2</sup>	3+
2	.1	192.0	1.121	32277.0	.201	104.33	211.13	.001133
3	1.2	213.0	1.125	32277.0	.252	90.70	169.31	.001077
4	2.1	233.0	1.133	32277.0	.304	80.77	131.63	.001022
5	4.1	292.0	1.147	32277.0	.403	70.01	106.10	.001000
6	8.1	323.0	1.154	32277.0	.500	61.30	94.63	.001000
7	16.4	365.0	1.161	32277.0	.640	54.42	84.66	.001000
8	24.8	402.0	1.167	32277.0	.784	49.22	77.77	.001000
9	32.6	415.0	1.170	32277.0	.901	45.56	72.27	.001000
10	40.8	438.0	1.173	32277.0	1.051	42.52	68.66	.001000
11	48.6	462.0	1.175	32277.0	1.227	40.08	65.52	.001000
12	56.0	483.0	1.177	32277.0	1.433	37.77	62.77	.001000
13	64.0	509.0	1.178	32277.0	1.673	35.52	60.00	.001000
14	73.3	539.0	1.179	32277.0	1.971	33.21	57.77	.001000
15	84.0	574.0	1.180	32277.0	2.333	31.00	55.52	.001000
16	98.2	633.0	1.181	32277.0	2.765	28.77	53.21	.001000

PT	X/D	STATIC PRESS. (PSIA)	T <sub>W</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS CORRECT
1	.5	59.2	1.12	79.3	.333E+02
2	90.1	57.1	1.28	329.6	.133E+01

AVERAGE BULK REYNOLDS 28730. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS 21742. AVERAGE WALL REYNOLDS 21742. AVERAGE FRICTION FACTOR .00612

RUN 164H, DATE 04/08/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 77.2 F, TCUT = 473.1 F, MASS FLOW RATE = 11.9 LB/HR, I = 79.0 AMPS, E = 4.565 VOLTS  
 PR. IN = .719, GR/RESS = .644E-03, MACH(2) = .117, MACH(16) = .159, T. SURR = 84.0 F

TC	X/D	T <sub>W</sub> (F)	T <sub>W</sub> /T <sub>B</sub>	BULK REYNOLDS	HL/2GAS	BULK NUSSELT	2GAS BTU/HR FT <sup>2</sup>	3+
2	.1	170.9	1.190	32277.0	.175	219.43	325.30	.001734
3	1.2	280.5	1.136	32277.0	.291	102.21	206.50	.001502
4	2.1	333.2	1.140	32277.0	.406	93.49	184.40	.001400
5	4.1	395.6	1.154	32277.0	.509	80.22	163.33	.001300
6	8.1	443.1	1.159	32277.0	.657	70.86	146.46	.001200
7	16.4	509.0	1.160	32277.0	.857	62.80	130.00	.001100
8	24.8	550.0	1.162	32277.0	1.054	58.65	120.00	.001077
9	32.6	585.0	1.163	32277.0	1.262	55.22	112.00	.001077
10	40.8	613.0	1.164	32277.0	1.488	52.22	106.00	.001077
11	48.6	643.0	1.165	32277.0	1.730	50.00	101.00	.001077
12	56.0	670.0	1.166	32277.0	1.979	48.00	97.00	.001077
13	64.0	703.0	1.167	32277.0	2.244	46.00	94.00	.001077
14	73.3	731.0	1.168	32277.0	2.524	44.00	91.00	.001077
15	84.0	754.0	1.169	32277.0	2.816	42.00	88.00	.001077
16	98.2	753.0	1.170	32277.0	3.116	40.00	86.00	.001077

PT	X/D	STATIC PRESS. (PSIA)	T <sub>W</sub> /T <sub>B</sub>	T <sub>B</sub> (F)	PRESS CORRECT
1	.5	59.1	1.16	77.2	.333E+02
2	90.3	56.6	1.33	451.3	.232E+01

AVERAGE BULK REYNOLDS 27706. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS 19706. AVERAGE WALL REYNOLDS 19706. AVERAGE FRICTION FACTOR .00590

RUN 1654, DATE 04/04/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 77.7 F, TOUT = 523.1 F, MASS FLOW RATE = 11.3 LB/HR, I = 53.0 A, E = 5.535 VOLTS  
 PR. IN = .719, GR/RES = .116E-02, MACH(2) = .117, MACH(16) = .171, T. SUR = 55.5 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/OGAS	BULK NUSSLETT	OGAS BTU/HR FT <sup>2</sup>	Q+
2	.1	220.1	1.262	3328.5	.174	133.5	1.5309.1	.00224.20
3	.2	361.7	1.510	3328.5	.300	133.5	1.5309.1	.00224.20
4	.4	443.3	1.547	3328.5	.1100	133.5	1.5309.1	.00224.20
5	.8	533.3	1.752	3328.5	.0800	133.5	1.5309.1	.00224.20
6	1.1	612.3	1.338	3328.5	.0700	133.5	1.5309.1	.00224.20
7	1.4	705.4	1.341	3328.5	.0722	133.5	1.5309.1	.00224.20
8	1.7	763.3	1.798	3328.5	.0777	133.5	1.5309.1	.00224.20
9	2.0	809.5	1.746	3328.5	.081	133.5	1.5309.1	.00224.20
10	2.3	855.1	1.991	3328.5	.0833	133.5	1.5309.1	.00224.20
11	2.6	899.9	1.933	3328.5	.101	133.5	1.5309.1	.00224.20
12	2.9	932.3	1.933	3328.5	.1114	133.5	1.5309.1	.00224.20
13	3.2	953.4	1.906	3328.5	.1103	133.5	1.5309.1	.00224.20
14	3.5	973.4	1.906	3328.5	.125	133.5	1.5309.1	.00224.20
15	3.8	1011.9	1.402	3328.5	.204	133.5	1.5309.1	.00224.20
16	4.1	1011.9	1.402	3328.5	.204	133.5	1.5309.1	.00224.20
17	4.4	707.4	1.073	3328.5	.967	133.5	1.5309.1	.00224.20

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PERCENT DEFECT
1	.5	59.1	1.22	78.2	-.53
2	.4	56.0	1.40	55.5	-.53

AVERAGE BULK REYNOLDS 26540. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 17482. AVERAGE FRICTION FACTOR .00013

RUN 1674, DATE 04/03/76, GAS AIR, MOLECULAR WT. = 28.97  
 TIN = 75.4 F, TOUT = 177.1 F, MASS FLOW RATE = 11.3 LB/HR, I = 39.3 A, E = 2.310 VOLTS  
 PR. IN = .720, GR/RES = .216E-03, MACH(2) = .117, MACH(16) = .127, T. SUR = 90.0 F

TC	X/D	TW (F)	TW/TB	BULK REYNOLDS	HL/OGAS	BULK NUSSLETT	OGAS BTU/HR FT <sup>2</sup>	Q+
2	.1	99.9	1.047	3312.4	.108	247.28	57.1.1	.00046.8
3	.2	125.0	1.094	3312.4	.273	105.44	7547.3	.00046.8
4	.4	140.6	1.120	3312.4	.091	96.19	57.1.1	.00046.8
5	.8	154.6	1.141	3272.2	.051	83.70	9210.3	.00046.8
6	1.1	166.5	1.154	3272.2	.037	75.53	3353.6	.00050.1
7	1.4	180.1	1.151	3233.3	.035	71.44	9375.0	.00050.1
8	1.7	190.3	1.151	3193.7	.036	69.66	9375.0	.00050.1
9	2.0	193.3	1.159	3159.2	.037	69.30	9375.0	.00050.1
10	2.3	207.5	1.156	3126.4	.039	67.40	9375.0	.00050.1
11	2.6	219.6	1.154	3093.2	.041	66.33	9375.0	.00050.1
12	2.9	229.8	1.154	3059.2	.044	66.72	9375.0	.00050.1
13	3.2	233.3	1.149	3026.7	.045	66.71	9375.0	.00050.1
14	3.5	234.3	1.148	3008.1	.049	63.35	9375.0	.00050.1
15	3.8	255.1	1.145	3008.1	.056	63.00	9375.0	.00050.1
16	4.1	255.2	1.133	2994.7	.108	63.07	9375.0	.00050.1
17	4.4	149.4	1.027	2994.7	.174	317.76	274.1	.00046.8

PT	X/D	STATIC PRESS. (PSIA)	TW/TB	TB (F)	PERCENT DEFECT
1	.5	59.0	1.04	74.4	-.53
2	.4	57.5	1.13	154.4	-.13

AVERAGE BULK REYNOLDS 31175. AVERAGE PARAMETERS BETWEEN PRESSURE TAPS  
 AVERAGE WALL REYNOLDS 27258. AVERAGE FRICTION FACTOR .00541

APPENDIX E.  
 Thermocouple Conduction Error  
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 Aerospace and Mechanical Engineering  
 University of Arizona

A thermocouple attached to the outside surface of a heated tube acts as a fin or extended surface which lowers the temperature at the point of attachment. Since this point also serves as the thermocouple junction, it measures a wall temperature lower than the value which would occur without its presence. The difference is known as "thermocouple conduction error." Consequently, in an experiment such as the present study, the deduced Nusselt number is systematically increased unless corrected for this effect.

Analyses

Based on extended surface analyses, the normalized thermocouple conduction error  $\theta$  has been shown by Schneider [48] to be approximately

$$\theta = \frac{t_w - t_{TC}}{t_w - t_\infty} = \left[ 1 + \frac{2\pi k_{tube} \delta_{tube}}{h_{TC} A_s} \lambda r_o \frac{K_1(\lambda r_o)}{K_0(\lambda r_o)} \right]^{-1} \quad (E1)$$

where  $t_w$  is the temperature of the undisturbed tube,  $h_{TC} A_s$  is the thermocouple conductance and  $r_o$  is the effective radius of the thermocouple attachment.  $K_0$  and  $K_1$  are modified Bessel functions of the second kind of order zero and one, respectively [49,50]. The quantity  $\lambda$  is defined as

$$\lambda = \frac{h_o + h_i}{k_{tube} \delta_{tube}}$$

and the thermocouple conductance is defined by the equation

$q_{TC} = h_{TC} A_s (t_{TC} - t_{\infty})$ . Thus, in this approximation  $\theta$  is a function of the non-dimensional parameters  $\lambda r_o$  and  $M = k_{tube} \delta_{tube} / (h_{TC} A_s)$ .

Using approximations to the Bessel functions, valid at small values of the argument, one may reduce equation (E1) further so that it takes the form

$$\theta \approx - \ln(\lambda r_o) / 2\pi M \quad (E2)$$

when  $2\pi M \gg 1$ . This form is useful for estimates of the magnitude of  $\theta$  when desiring to determine whether it is significant in a given case. It is presented as Figure E1.

In calibration for thermocouple conduction error data are normally obtained without flow so a probe can be used to measure the tube wall temperature in the vicinity of the thermocouple. In this case,  $h_i = 0$ . Examining Figure E1, one can see that the effect of flow (i.e., non zero value of  $h_i$ ) is to increase  $\lambda r_o$  and reduce  $\theta$  for the same thermocouple attachment and environment.

Hess [29] extended and improved Schneider's analysis for application to electrically heated tubes with internal flow such as the present experiment. His representation takes the form

$$\theta = \frac{h_i + h_o}{h_{TC}} \frac{(1 - h_o / h_{TC})}{1 + \frac{2k_w \delta}{h_{TC} r_o^2} \frac{\lambda r_o K_1(\lambda r_o)}{K_o(\lambda r_o)}} \quad (E3)$$

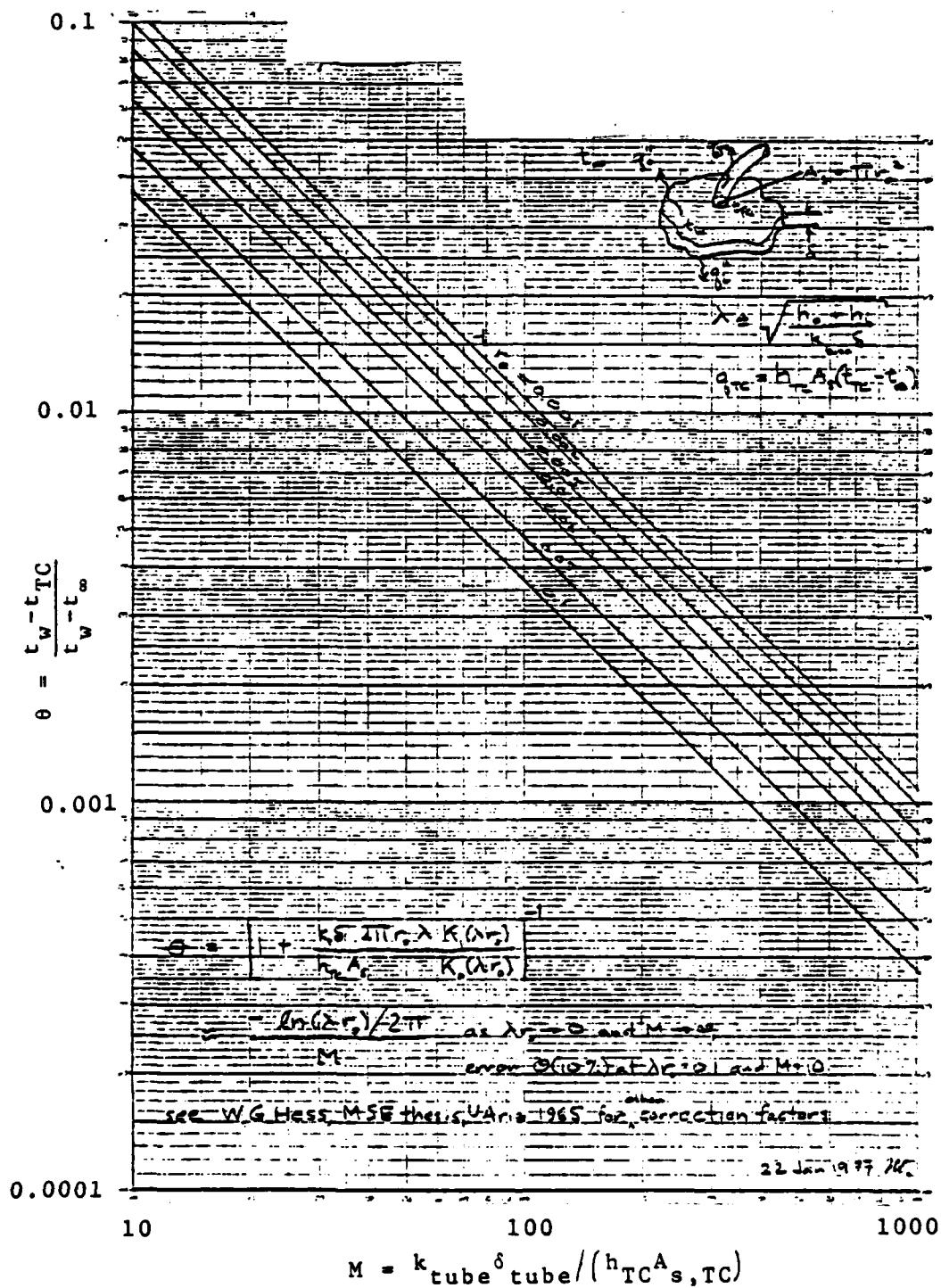


Fig. E1. Approximation to thermocouple conduction error for large values of parameter  $M = k_{\text{tube}} \delta_{\text{tube}} / (h_{TC} A_{s, TC})$ .

Evaluation of thermocouple conductance,  $h_{TC}A_s$

For fine wire thermocouples in an environment at atmospheric pressure, free convection dominates as the mechanism for heat loss from the thermocouple compared to radiation. As an approximation, one may consider the total heat transfer coefficient and properties to be constant for the thermocouple wire and derive

$$q_{TC} = \sqrt{(h_r + h_{NC})Pk_{TC}A_s} (t_{TC} - t_\infty) \tanh ml \quad (E4)$$

as by Schneider [48]. For long wires, i.e.,  $ml = \sqrt{2 hP/kA} \gg 5$ ,  $\tanh ml$  approaches unity; then  $h_{TC}A_s$  becomes  $\sqrt{(h_r + h_{NC})Pk_{TC}A_s}$ .

The wire can be considered a small body in large surroundings so

$$h_r \approx \epsilon \sigma [T_{TC}^4 - T_\infty^4] / (T_{TC} - T_\infty) \quad (E5)$$

The heat transfer coefficient for natural convection can be determined from a correlation of the form  $Nu_f = f_n(Gr_f Pr)$ . The Grashof number is typically small for wires of the size of our thermocouples. For the range  $10^{-3} < GrPr < 10^{-1}$  the curve recommended by Kreith [51, Fig.7-3] can be represented as

$$Nu_f = \frac{h_{NC}d}{K_f} = 0.315 + 0.8 [Gr_f Pr_f]^{0.18} \quad (E6)$$

In an unpublished note, Hess, Deardorff and McEligot [52, included herein as Appendix F] examined available calibration data for radiating thermocouples attached in the parallel junction form of Moen [28]. From comparisons be-



tween predictions and measurements, they concluded that the effective radius of the thermocouple attachment,  $r_o$ , was approximately equal to the actual radius of the thermocouple wire. Consequently,  $A_s = \pi r_o^2 \approx A_{CS} = \pi d^2/4$ . The calibration data of Campbell [53] for an atmospheric environment are also in approximate agreement with the choice of  $d/2$  as  $r_o$ .

#### Application to present experiment

The heat transfer coefficient from the outside of the tube,  $h_o$ , may be deduced from the heat loss calibration equation (B5), to be

$$h_o = [C_1 + C_2(t_w - t_\infty) + C_3(t_w - t_\infty)^2]/\pi D \quad (E7)$$

For  $h_i$  either a correlation such as equation (19) or tabular data from the initial data reduction can be employed. In this experiment  $h_i$  is typically of the order of 200 Btu/hrft<sup>2</sup>°F or more.

As an example of the magnitude of thermocouple conduction error to be expected, Figure E2 has been plotted for thermocouple 10. The value of  $h_i$  was taken as 200 Btu/hrft<sup>2</sup>°F and the environmental temperature was assumed to be about 70°F for this presentation. The reduction in  $\theta$  with flow is clear and it is also seen that in the heat loss runs (no flow)  $\theta$  decreases slightly as the wall temperature increases.

For the tabular results of Appendix D the thermocouple conduction error was calculated from equations (E3) through (E7) and correlations (19) and (B5). Material and fluid

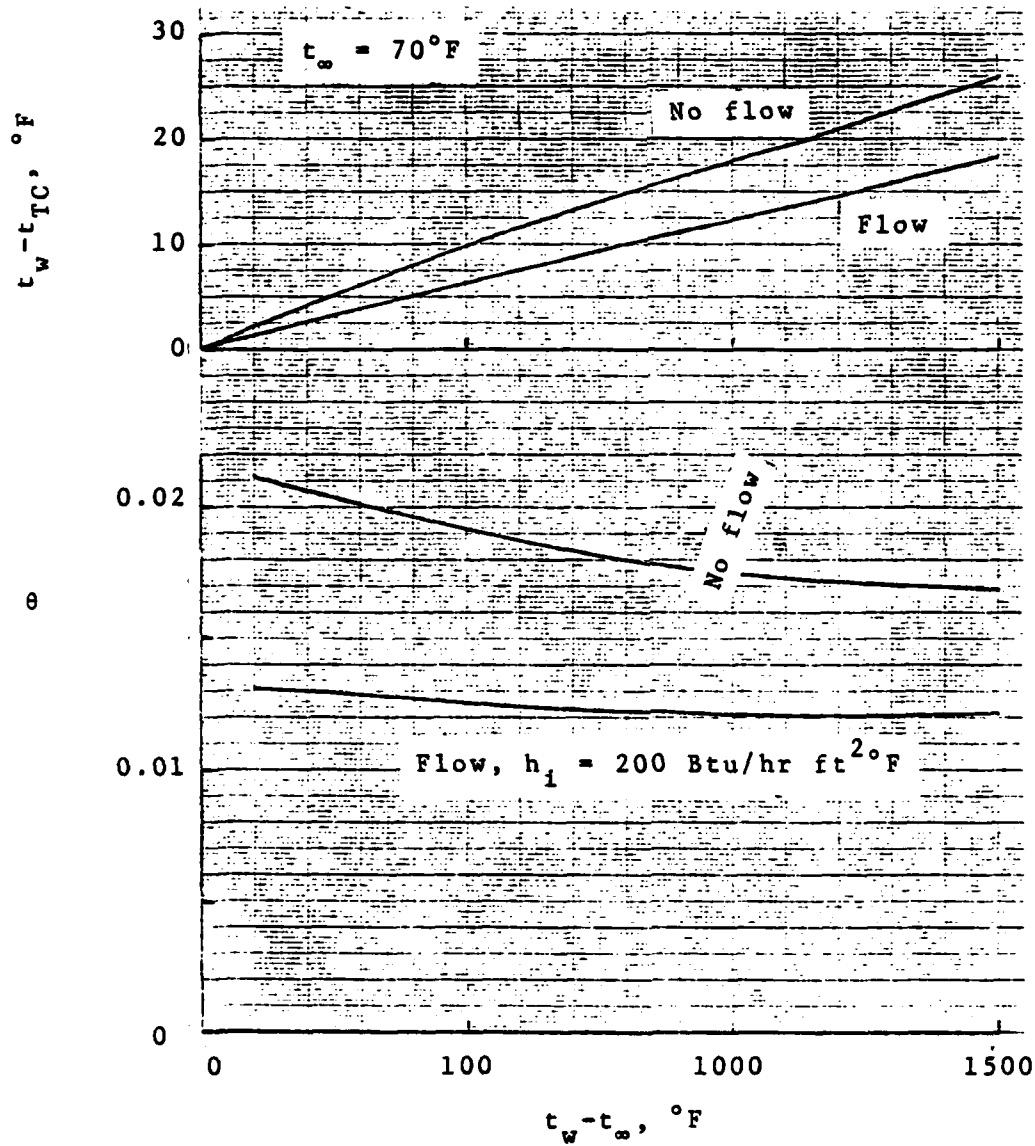


Fig. E2. Predicted thermocouple conduction error for thermocouple 10.

properties used in evaluating the thermocouple conductance were based on the temperature at the junction and its resulting film temperature,  $t_f = (t_{TC} + t_\infty)/2$ , as appropriate. While a numerical solution could be applied to improve the analysis predicting the thermocouple conductance, such sophistication does not appear warranted due to the uncertain knowledge of several quantities and the small magnitude of  $\theta$ .

#### APPENDIX F.

##### Radiating Thermocouple Conduction Error

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In space environments and space simulation chambers, temperatures are often measured with thermocouples attached to exposed surfaces. The primary means of energy exchange then are conduction through the solid material and thermal radiation. In our Laboratory, we also often use a vacuum environment to minimize and/or localize the heat loss from thin-walled tubes in which we perform internal convective heat transfer measurements [38]. In these situations the thermocouple attachment usually acts as a radiating fin which reduces the local surface temperature near the point of measurement. This systematic effect may be called the radiating thermocouple conduction error.

Schneider [48] presents an analysis to predict the thermocouple conduction error in a convective environment by idealizing the thermocouple as a cylinder mounted perpendicular to the surface at a single point.

1. Now with Pratt and Whitney Aircraft Company, West Palm Beach, Florida.
2. Now with Gulf General Atomics, La Jolla, California.

Including energy generation in the wall by electrical resistive heating and energy transfer from the surface opposite the idealized thermocouple, one may extend Schneider's result to

$$\frac{T_{TC} - T_{w,u}}{T_{w,u} - T_{\infty}} = \frac{(h_o - h_{TC})r K_o(\lambda r)}{(h_i + h_{TC})r K_o(\lambda r) + 2\lambda k_w \delta K_1(\lambda r)} \quad (F1)$$

where the heat transfer coefficients may represent convective or radiative processes as appropriate. In the case of infinite radiating thermocouple leads, the effective heat transfer coefficient over the contact area of the thermocouple may be shown to be

$$h_{TC} = \frac{k_{TC} \left[ \frac{2R}{5} (T_{TC}^5 - 5T_{TC}T_{\infty}^4 + 4T_{\infty}^5) \right]^{1/2}}{T_{TC} - T_{\infty}} \quad (f2)$$

if its emissivity and thermal conductivity are constant. Thus, provided that the material properties are known, prediction of the radiating thermocouple conduction error reduces to the problem of determining the effective thermocouple radius,  $r$ .

For many applications the parallel type thermocouple junction, shown in the insert of Figure F1, is more accurate than the more common cross type junction because the location of the measuring plane is effectively on the tube surface rather than being spread perpendicular to it [28].

Rather than satisfying the idealization of a single cylindrical interface between the thermocouple and the surface, the attachment region for the parallel junction consists of two roughly elliptical areas slightly separated from each other. Accordingly, the objectives of the present work were taken to be (1) to determine  $r$  for a parallel junction configuration and (2) to investigate the reproducibility of the conduction error when such thermocouples are produced by using normal laboratory standards for equipment construction.

Measurements were conducted on three circular test sections of 0.010 inch thick Inconel 600, two feet long. Premium grade bare Chromel and Alumel thermocouple wires of 0.005 inch diameter were spot welded to the test section by the electrical discharge technique. Circumferential distance between the two wires was approximately  $1/8$  inch and the attached area of each covered approximately one to two wire diameters. Tests included about fourteen such thermocouples with all wires taken from the same spools.

These resistively heated test sections were mounted in glass vacuum chambers. With no internal flow,  $h_i$  equals zero and  $h_o$  can be determined from the tube emissivity which one also deduces from the tests. "Undisturbed"

tube wall temperatures,  $T_{w,u}$ , were determined with a traveling internal thermocouple probe, also of premium grade Chromel-Alumel, which measured the wall temperature profile axially between the thermocouples. Calculations show the maximum temperature drop through the wall to be less than  $0.01^\circ\text{F}$  so the thin wall idealization is valid. Readings were accepted without correction for deviation from standard N.B.S. emf tables since Hoskins Manufacturing Company certified the deviation as less than  $1^\circ\text{F}$ .

Results are demonstrated on Figure F1. The dashed curves are predictions based on equations (F1) and (F2) in conjunction with manufacturers' information for emissivities and thermal conductivities of the thermocouple wires and the tube. The solid curve represents predictions based on the measured emissivity of the Inconel tube used by Hess and on an effective thermocouple radius equal to the actual wire diameter; otherwise the bases are the same.

Hess' data points are averages of the thermocouple readings for the central portion of the tube and they show the effective radius to be approximately equal to the wire diameter or slightly less. The measurements of Swearingen and of Reynolds and Deardorff are from test sections with different thermal histories, hence

emissivities, but of the same materials and dimensions. Their calibrations suggest that  $r$  is about one-half the wire diameter. Different welding jigs were used for each and, consequently, the region of attachment varied from test section to test section but would be approximately uniform for different thermocouples on the same test section. Accordingly, one would expect the level of the thermocouple conduction error to vary from test section to test section as it does in Figure F1.

We conclude that the effective radius of the thermocouple attachment is approximately one-half to one wire diameter when constructed in the manner described. One may use this observation with manufacturers' information and equations (F1) and (F2) to determine whether the systematic error will be significant in his specific application. (For the results shown, in an internal convective heating experiment with  $T_w \approx 1000^\circ\text{F}$  and  $T_b \approx 900^\circ\text{F}$ , the resulting error in Nusselt number would be 5 to 10 per cent.) If such predictions indicate that the errors would be important, we recommend individual calibration since the values of a number of the pertinent input variables are not readily available.



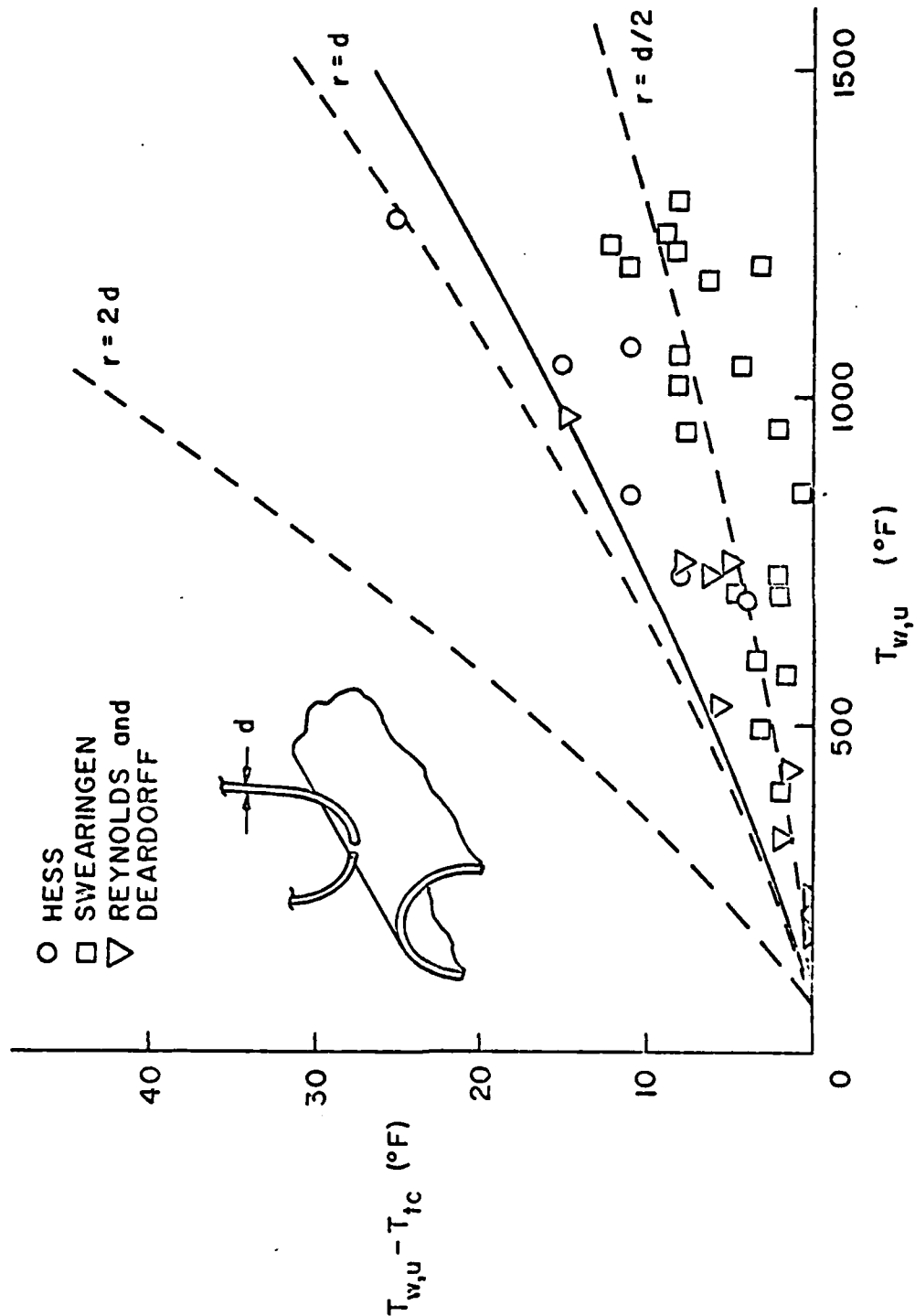


Figure F1. RADIATING THERMOCOUPLE CONDUCTION ERROR FOR PARALLEL TYPE JUNCTION

# NOMENCALTURE

$h$	Heat transfer coefficient; $h_i$ , inner surface: (thermocouple) surface.
$k$	thermal conductivity
$K_0, K_1$	Bessel functions
$r$	effective thermocouple attachment radius
$T_{TC}$	temperature measured by thermocouple
$T_{w,u}$	"undisturbed" wall temperature
$\beta$	thermocouple heat transfer constant, $2\sigma\epsilon/(k_{TC}r)$
$\delta$	wall thickness
$\epsilon$	emissivity
$\lambda$	wall heat transfer constant, $[h_o + h_i]/(k_w r)^{1/2}$
$\sigma$	Stefan-Boltzman constant

## ACKNOWLEDGEMENT:

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